XXIV. *On the nature of the function expressive of the law of human mortality, and on a new mode of determining the value of Life Contingencies. In a Letter to* Francis Baily, *Esq. F.R.S. &c. By* Benjamin Gompertz, *Esq. F.R.S.*

Read June 16, 1825.

Dear Sir,

The frequent opportunities I have had of receiving pleasure from your writings and conversation, have induced me to prefer offering to the Royal Society through your medium, this Paper on Life Contingencies, which forms part of a continuation of my original paper on the same subject, published among the valuable papers of the Society, as by passing through your hands it may receive the advantage of your judgment.

I am, Dear Sir, yours with esteem,

Benjamin Gompertz.

9th June 1825.

CHAPTER I.

Article 1. In continuation of Art. 2. of my paper on the valuation of life contingencies, published in the Philosophical Transactions of this learned Society, in which I observed the near agreement with a geometrical series for a short period of time, which must pervade the series which expresses the number of living at ages in arithmetical progression, proceeding by small intervals of time, whatever the law of mortality may be, provided the intervals be not greater than certain limits: I now call the reader's attention to a law observable in the tables of mortality, for equal intervals of long periods; and adopting the notation of my former paper, considering L_x to express the number of living at the age x, and using λ for the characteristic of the common logarithm; that is, denoting by $\lambda(L_x)$ the common logarithm of the number of persons living at the age of x, whatever x may be, I observe that if $\lambda(L_n) - \lambda(L_{n+m})$, $\lambda(L_{n+m}) - \lambda(L_{n+2m})$ $\lambda(L_{n+2m}) - \lambda(L_{n+3m})$, &c. be all the same; that is to say, if the differences of the logarithms of the living at the ages n, $n+m$; $n+m$, $n+2m$; $n+2m$, $n+3m$; &c. be constant, then will the numbers of living corresponding to those ages form a geometrical progression; this being the fundamental principle of logarithms.

Art. 2. This law of geometrical progression pervades, in an approximate degree, large portions of different tables of mortality; during which portions the number of persons living at a series of ages in arithmetical progression, will be nearly in geometrical progression; thus, if we refer to the mortality of DEPARCIEUX, in Mr. BAILY's life annuities, we shall have the logarithm of the living at the ages 15, 25, 35, 45, and 55 respectively, 2,9285; 2,88874; 2,84136; 2,79379; 2.72099, for $\lambda(L_{15})$; $\lambda(L_{25})$; $\lambda(L_{35})$; &c. and we find $\lambda(L_{25}) - \lambda(L_{35}) =$, 04738 $\lambda(L_{35}) - \lambda(L_{45}) =$, 04757, and consequently these being nearly equal (and considering that for small portions of time the geometrical progression takes place very nearly) we observe that in those tables the numbers of living in each yearly increase of age are from 25 to 45 nearly, in geometrical progression. If we refer to Mr. MILNE's table of Carlisle, we shall find that according to that table of mortality, the number of living at each successive year, from 92 up to 99, forms very nearly a geometrical progression, whose common ratio is $\frac{3}{4}$; thus setting out with 75 for the number of living at 92, and diminishing continually by $\frac{1}{4}$, we have to the nearest integer 75, 56, 42, 32, 24, 18, 13, 10, for the living at the respective ages 92, 93, 94, 95, 96, 97, 98, 99, which in no part differs from the table by $\frac{1}{37}$th part of the living at 92.

Art. 3. The near approximation in old age, according to some tables of mortality, leads to an observation, that if the law of mortality were accurately such that after a certain age the number of living corresponding to ages increasing in arithmetical progression, decreased in geometrical progression, it would follow that life annuities, for all ages beyond that period, were of equal value; for if the ratio of the number of persons living from one year to the other be constantly the same, the chance of a person at any proposed age living to a given number of years would be the same, whatever that age might be; and therefore the present worth of all the payments would be independent of the age, if the annuity were for the whole life; but according to the mode of calculating tables from a limited number of persons at the commencement of the term, and only retaining integer numbers, a limit is necessarily placed to the tabular, or indicative possibility of life; and the consequence may be, that the value of life annuities for old age, especially where they are deferred, should be deemed incorrect, though indeed for immediate annuities, where the probability of death is very great, the limit of the table would not be of so much consequence, for the present value of the first payment would be nearly the value of the annuity.

Such a law of mortality would indeed make it appear that there was no positive limit to a person's age; but it would be easy, even in the case of the hypothesis, to show that a very limited age might be assumed to which it would be extremely improbable that any one should have been known to attain.

For if the mortality were, from the age of 92, such that $\frac{1}{4}$ of the persons living at the commencement of each year were to die during that year, which I have observed is nearly the mortality given in the Carlisle tables between the ages 92 and 99,* it would be above one million to one that out of three millions of persons, whom history might name to have reached the age of 92, not one would have attained to the age of 192, notwithstanding the value of life annuities of all ages above 92 would be of the same value. And though the limit to the possible duration of life is a subject not likely ever to be determined, even should it exist, still it appears interesting to dwell on a consequence which would follow, should the mortality of old age be as above described. For, it would follow that the non-appearance on the page of history of a single circumstance of a person having arrived

* If from the Northampton tables we take the numbers of living at the age of 88 to be 83, and diminish continually by $\frac{1}{4}$ for the living, at each successive age, we should have at the ages 88, 89, 90, 91, 92, the number of living 83; 61.3; 45.9; 34.4; 25.8; almost the same as in the Northampton table.

at a certain limited age, would not be the least proof of a limit of the age of man; and further, that neither profane history nor modern experience could contradict the possibility of the great age of the patriarchs of the scripture. And that if any argument can be adduced to prove the necessary termination of life, it does not appear likely that the materials for such can in strict logic be gathered from the relation of history, not even should we be enabled to prove (which is extremely likely to be the state of nature) that beyond a certain period the life of man is continually becoming worse.

Art. 4. It is possible that death may be the consequence of two generally co-existing causes; the one, chance, without previous disposition to death or deterioration; the other, a deterioration, or an increased inability to withstand destruction. If, for instance, there be a number of diseases to which the young and old were equally liable, and likewise which should be equally destructive whether the patient be young or old, it is evident that the deaths among the young and old by such diseases would be exactly in proportion of the number of young to the old; provided those numbers were sufficiently great for chance to have its play; and the intensity of mortality might then be said to be constant; and were there no other diseases but such as those, life of all ages would be of equal value, and the number of living and dying from a certain number living at a given earlier age, would decrease in geometrical progression, as the age increased by equal intervals of time; but if mankind be continually gaining seeds of indisposition, or in other words, an increased liability to death (which appears not to be an unlikely supposition with respect to a great part of life, though the contrary appears to take place at certain periods) it would follow that the number of living out of a given number of persons at a given age, at equal successive increments of age, would decrease in a greater ratio than the geometrical progression, and then the chances against the knowledge of any one having arrived to certain defined terms of old age might increase in a much faster progression, notwithstanding there might still be no limit to the age of man.

Art. 5. If the average exhaustions of a man's power to avoid death were such that at the end of equal infinitely small intervals of time, he lost equal portions of his remaining power to oppose destruction which he had at the commencement of those intervals, then at the age x his power to avoid death, or the intensity of his mortality might be denoted by aq^x, a and q being constant quantities; and if L_x be the number of living at the age x, we shall have $a L_x \times \overset{x}{q} \cdot \dot{x}$ for the fluxion of the number of deaths $= -(L_x)^{\bullet}$; $\therefore abq^x = -\frac{\dot{L}_x}{L_x}$, $\therefore abq^x = -$ hyp. log. of $b \times$ hyp. log. of L_x, and putting the common logarithm of $\frac{1}{b} \times$ square of the hyperbolic logarithm of $10 = c$, we have $c.q^x =$ common logarithm of $\frac{L_x}{d}$; d being a constant quantity, and therefore L_x or the number of persons living at the age of $x = d.\overline{g|}^{q^x}$; g being put for the number whose common logarithm is c. The reader should be aware that I mean $\overline{g|}^{q^x}$ to represent g raised to the power q^x and not g^q raised to the x power; which latter I should have expressed by $\overline{g^{q}|}^{x}$, and which would evidently be equal to g^{qx}. I take this opportunity to make this observation, as algebraists are sometimes not sufficiently precise in their notation of exponentials.

This equation between the number of the living, and the age, becomes deserving of attention, not in consequence of its hypothetical deduction, which in fact is congruous with many natural effects, as for instance, the exhaustions of the receiver of an air pump by strokes repeated at equal intervals of time, but it is deserving of attention, because it appears corroborated during a long portion of life by experience; as I derive the same equation from various published tables of mortality during a long period of man's life, which experience therefore proves that the hypothesis approximates to the law of mortality during the same portion of life; and in fact the hypothesis itself was derived from an analysis of the experience here alluded to.

Art. 6. But previously to the interpolating the law of mortality from tables of experience, I will premise that if, according to our notation, the number of living at the age x be denoted by L_x, and λ be the characteristic of a logarithm, or such that $\lambda(L_x)$ may denote the logarithm of that number, that if $\lambda(L_a) - \lambda(L_{a+r}) = m$, $\lambda(L_{a+r}) - \lambda(L_{a+2r}) = mp$, $\lambda(L_{a+2r}) - \lambda(L_{a+3r}) = m^2 p$; and generally $\lambda(L_{a+\overline{n-r}}) - \lambda(L_{a+n}) = m \,.\, p^{\frac{n}{r}-1}$; that by continual addition we shall have $\lambda(L_a) - \lambda(L_{a+n}) = m(1 + p + p^2 + p^3 + \ldots p^{\frac{n}{r}-1}) = m \,.\, \frac{1-p^{\frac{n}{r}}}{1-p}$; and therefore if $p^{\frac{1}{r}} = q$, and ε be put equal to the number whose common logarithm is $\frac{m}{1-q^n}$, we shall have $\lambda(L_{a+n}) = \lambda(L_a) - \lambda(\varepsilon) \times (1 - q^n) = \lambda\left(\frac{L_a}{\varepsilon}\right) + \lambda(\varepsilon) . q^n$; $\therefore L_{a+n} = \frac{L_a}{\varepsilon} \times \varepsilon\rceil^{q^n}$; and this equation, if for $a + n$ we write x, will give $L_x = \frac{L_a}{\varepsilon} . \varepsilon\rceil^{q^{-a} \times q^x}$; and consequently if $\frac{L_a}{\varepsilon}$ be put

$= d$, and $\overline{\varepsilon}|^{q^{-a}} = g$, the equation will stand $L_x = d \,.\, \overline{g}|^{q^x}$, and $\lambda(g) = \lambda(\varepsilon) \times q^{-a} = \frac{m\, q^{-a}}{1 - q^r}$; and I observe that when q is affirmative, and $\lambda(\varepsilon)$ negative, that $\lambda(g)$ is negative. The equation $L_x = d \,.\, \overline{g}|^{q^x}$ may be written in general $\lambda(L_x) = \lambda(d) \pm$ the positive number whose common logarithm is $\{\lambda^2(g) + x\,\lambda(g)\}$, the upper or under sign to be taken according as the logarithm of g is positive or negative, λ^2 standing for the characteristic of a second logarithm; that is, the logarithm of a logarithm, $\lambda(q) = \frac{1}{r} \times \lambda(p)$, $\lambda^2(g) = \lambda^2(\varepsilon) - a.\lambda(q) = \lambda\left(\frac{m}{1-p}\right) - a\,.\,\lambda(q) = \lambda(m) - \lambda(1-p) - a\,\lambda(q)$; also $\lambda(d) = \lambda(L_a) - \frac{m}{1-p}$.

Art. 7. Applying this to the interpolation of the Northampton table, I observe that taking $a = 15$ and $r = 10$ from that table, I find $\lambda(L_a) - \lambda(L_{a+r}) = ,0566 = m$, $\lambda(L_{a+r}) - \lambda(L_{a+2r}) = ,0745$, $\lambda(L_{a+2r}) - \lambda(L_{a+3r}) = ,0915$, and $\lambda(L_{a+3r}) - \lambda(L_{a+4r}) = ,1228$; now if these numbers were in geometrical progression, whose ratio is p, we should have respectively $m = ,0566$; $mp = ,0745$; $mp^2 = ,0915$; $mp^3 = ,1228$. No value of p can be assumed which will make these equations accurately true; but the numbers are such that p may be assumed, so that the equation shall be nearly true; for resuming the first and last equations we have $p^3 = \frac{1228}{566}$; $\therefore$ logarithm of $p = \frac{1}{3}$(logarithm of 1228 — logarithm of 566) $= ,11213$, $\therefore \lambda(q) = ,011213$ and $p = 1,2944$. And to examine how near this is to the thing required, continually to the logarithm of ,0566 namely $\bar{2},75282$, adding ,11213 which is the logarithm of p, we have respectively for the logarithms of mp, of mp^2, of mp^3 the values $\bar{2},8649$, $\bar{2},9771$, $\bar{1},0892$; the numbers corresponding to which are ,07327; ,09486; ,1228; and consequently m, mp, mp^2, and mp^3 respectively equal to ,0566; ,07327; ,09486, and ,1228 which do not differ much from the proposed series ,0566; ,07327; ,09486, and ,1228; and according to our form for interpolation, taking $m = ,0566$ and $p = 1,2944$; we have $\frac{m}{1-p} = -\frac{,0566}{,2944} = -,1922$; and $\lambda(L_{15})$ agreeably to the Northampton tables, being $= 3,7342$ we have $\lambda(d) = 3,7342 + ,1922 = 3,9264$, $d = 8441$, $\lambda^2(q)$, that is to say, the logarithm of the logarithm of $q = \lambda\left(\frac{m}{1-p}\right) - a\,\lambda(q) = \bar{1},28375 - ,16819 = \bar{1},1156$, $\lambda(g) = -,130949 = \bar{1},8695$, the negative sign being taken because $\lambda(g) = \lambda(\varepsilon) \times q^{-a} = \frac{m}{1-q} \cdot q^{-a}$, and $g = ,7404$. And therefore x being taken between the limits, we are to examine the degree of proximity of the equation $L_x = 8441 \times \overline{7404}|^{1,0261^x}$ or $\lambda(L_x)$, that is, the logarithm of the number of living at the age $x = 3,9264$ — number whose logarithm is ($\bar{1},11556 + x \times .011213$), as the logarithm of g is negative. The table constructed according to this formula, which I shall lay before the reader, will enable him to judge of the proximity it has to the Northampton table; but previously thereto shall show that the same formula, with different constants, will serve for the interpolations of other tables.

Art. 8. To this end let it be required to interpolate Deparcieux's tables, in Mr. Baily's life annuities, between the ages 15 and 55.

The logarithms of the living at the age of

15 are	2,92840	differences = ,03966	$= \lambda(L_{15}) - \lambda(L_{25})$
25	2,88874	,04738	$= \lambda(L_{25}) - \lambda(L_{35})$
35	2,84136	,04757	$= \lambda(L_{35}) - \lambda(L_{45})$
45	2,79379	,07280	$= \lambda(L_{45}) - \lambda(L_{55})$
55	2,72099		

Here the three first differences, instead of being nearly in geometrical progression are nearly equal to each other, showing from a remark above, that the living, according to these tables, are nearly in geometrical progression; and the reader might probably infer that this table will not admit of being expressed by a formula similar to that by which the Northampton table has been expressed between the same limits, but putting,

on the supposition of the possibility, though the thing cannot be accurately true,

$$\left\{\begin{array}{ll} \lambda(L_{15}) = \quad \ldots\ldots & = 2{,}92840 \\ \lambda(L_{25}) = \lambda(L_{15}) - m \quad \ldots & = 2{,}88874 \\ \lambda(L_{35}) = \lambda(L_{15}) - m - mp \quad \ldots & = 2{,}84136 \\ \lambda(L_{45}) = \lambda(L_{15}) - m - mp - mp^2 \quad . & = 2{,}79379 \\ \lambda(L_{55}) = \lambda(L_{15}) - m - mp - mp^2 - mp^3 & = 2{,}72099 \end{array}\right\}$$

and we shall have

$\lambda(L_{15}) - \lambda(L_{35})$ or its equal $m + mp = {,}08704$, and $\lambda(L_{35}) - \lambda(L_{55})$ or its equal $p^2 \times \overline{m + pm} = {,}12037$; $\therefore p^2 = \frac{12037}{8704}$ and the log. of $p = \frac{\text{log. of } 12037 - \text{log. of } 8704}{2} = {,}0703997$ and $p = 1{,}176$, $m = \frac{{,}08704}{1+p} = \frac{{,}08704}{2{,}176} = {,}04$. And to see how these values of m and p will answer for the approximate determination of the logarithms above set down of the numbers of living at the ages 15, 25, 35, 45, and 55, we have the following easy calculation by continually adding the logarithm of p

Logarithm of $m = \bar{2},6020600$
Log. of $p = 0,0703997$
therefore $mp = ,047039$
Log. of $mp = \bar{2},6724597$ $\quad mp^2 = ,055317$
Log. of $mp^2 = \bar{2},7428594$ $\quad mp^3 = ,065051$
Log. of $mp^3 = \bar{2},8128591$

$$
\begin{array}{rl}
\lambda\left(L_{15}\right) = & 2,92840 \\
-m = & -\ ,04 \\
\hline
\lambda\left(L_{25}\right) = & 2,88840 \\
-mp = & -\ ,04704 \\
\hline
& 2,84136 \\
-mp^2 = & -,05532 \\
\hline
& 2,78604 \\
-mp^3 = & -\ ,06505 \\
\hline
& 2,72099
\end{array}
$$

These logarithms of the approximate number of living at the ages 15, 25, 35, 45 and 55, are extremely near those proposed, and the numbers corresponding to these give the number of living at the ages 15, 25, 35, 45 and 55, respectively, 848; 773,4; 694; 612,3; and 526; differing very little from the table in Mr. Baily's life annuities; namely, 848; 774; 694; 622 and 526. And we have $a = 15$, $r = 10$, $m = ,04$; $\lambda(m) = \bar{2},60206$; $1 - p = -\ ,176$; $\lambda\, q = \frac{1}{10}\lambda\,(p) =$ $,00703997$; $\lambda(g) = \frac{m\,q^{-a}}{1-p} = -\frac{,04 \times q^{-a}}{,176}$, and is negative; $\lambda\,\lambda\,(g) = \lambda\,(,04) - 15 \times ,00704 - \lambda\,(,176) = \bar{1},25095$; $\lambda\,(d) = \lambda(L_a) - \frac{m}{1-p} = 2,9284 + ,22727 = 3,1557$; $\therefore \lambda\,(L_x) =$ $3,1557 -$ number whose log. is $(\bar{1},25095 + ,00704\,x)$, for the logarithm of living in Deparcieux' table in Mr. Baily's annuities, between the limits of age 15 and 55. The table which we shall insert will afford an opportunity of appreciating the proximity of this formula to the table.

Art. 9. To interpolate the Swedish mortality among males between the ages of 10 and 50, from the table in Mr. Baily's annuities:

Here $\lambda\left(L_{10}\right) = 3{,}779091$

$\lambda\left(L_{20}\right) = 3{,}746868$ to be assumed $= \lambda\left(L_{10}\right) - m$

$\lambda\left(L_{30}\right) = 3{,}703205 \quad . \quad . \quad = \lambda\left(L_{10}\right) - m - mp$

$\lambda\left(L_{40}\right) = 3{,}648165 \quad . \quad . \quad = \lambda\left(L_{10}\right) - m - mp - mp^2$

$\lambda\left(L_{50}\right) = 3{,}564192 \quad . \quad . \quad = \lambda\left(L_{10}\right) - m - mp - mp^2 - mp^3$

Consequently $m + mp = \lambda\left(L_{10}\right) - \lambda\left(L_{30}\right) = {,}075886$, and $\lambda\left(L_{30}\right) - \lambda\left(L_{50}\right) = p^2 \times \overline{m + mp} = {,}139013$; therefore $p^2 = \frac{139013}{75886}$, and $\lambda(p) = {,}1314468$; $\therefore p = 1{,}3535$; $m = \frac{{,}075886}{1+p} = \frac{{,}075886}{2{,}3535}$; $\lambda(m) = \bar{2}{,}5084775$; $m = {,}032244$; $a = 10$; $r = 10$; $\lambda(q) = {,}01314468$; $\lambda g = \frac{m \cdot q^{-10}}{-{,}3535}$, negative; $\lambda\lambda(g) = \lambda(m) - 10\,\lambda(q) - \lambda({,}3535) = \bar{2}{,}82861$; $\lambda(d) = \lambda L_a - \frac{m}{1-p} = 3{,}779091 + 091218, = 3{,}8703$; consequently this will give between the ages 10 and 50 of Swedish males,

$\lambda\left(L_x\right)$ or the logarithm of the living at the age of $x = 3{,}8703 -$ number, whose logarithm is $(\bar{2}{,}82861 + {,}013145\,x)$.

A table will also follow to show the proximity of this with Mr. BAILY's table.

Art. 10. For Mr. MILNE's table of the Carlisle mortality we have, as given by that ingenious gentleman,

$$\lambda\left(L_{10}\right) = 3{,}81023$$
$$\lambda\left(L_{20}\right) = 3{,}78462$$
$$\lambda\left(L_{30}\right) = 3{,}75143$$
$$\lambda\left(L_{40}\right) = 3{,}70544$$
$$\lambda\left(L_{50}\right) = 3{,}64316$$
$$\lambda\left(L_{60}\right) = 3{,}56146$$

And the difference of these will form a series nearly in geometrical progression, whose common ratio is $\frac{4}{3}$, and in consequence of this, the first method may be adopted for the interpolations. Thus because $\lambda\left(L_{10}\right)-\left(L_{20}\right)=,02561$, the first term of the differences, and $\lambda\left(L_{50}\right)-\lambda\left(L_{60}\right)=,0817$, the fifth term of the differences: take the common ratio $=\overline{\frac{817}{256}}\Big|^{\frac{1}{4}}$, and $m=,0256$; $\therefore\ \lambda(m)=\bar{2},40824$. These will give $\lambda(p)=,126$; $p=1,3365$; $a=10$, $r=10$, $\lambda(q)=,0126$, $\lambda(\varepsilon)=\frac{m}{1-p}=-\frac{,0256}{,3365}$; $\therefore\ \lambda(g)$ negative; $\lambda\lambda g=2,40824-\lambda(,3365)-,126=\bar{2},75526$; and $\lambda(d)=\lambda\left(L_{10}\right)+\frac{,0256}{,3365}=3,88631$, and accordingly, to interpolate the Carlisle table of mortality for the ages between 10 and 60, we have for any age x,

$$\lambda\left(L_x\right)=3,88631-\text{number whose logarithm is }(\bar{2},88126+,0126\,x).$$

Here we have formed a theorem for a larger portion of time than we had previously done. If by the second method the theorem should be required from the data of a larger portion of life, we must take r accordingly larger; thus if a be taken 10, $r=12$, then the interpolation would be formed from an extent of life from 10 to 58 years; and referring to Mr. MILNE's tables, our second method would give $\lambda\left(L_x\right)=3,89063-$ the number whose logarithm is $(\bar{2},784336+,0120948\,x)$; this differs a little from the other, which ought to be expected.

If the portion between 60 and 100 years of Mr. MILNE's Carlisle table be required to be interpolated by our second method, we shall find $p=1,86466$; $\lambda(m)=\bar{1},30812$; $m=,20329$, &c. and we shall have $\lambda\left(L_x\right)=3,79657-$ the number whose logarithm is $(\bar{3},74767+,02706\,x)$.

This last theorem will give the numbers corresponding to the living at 60, 80, and 100, the same as in the table; but for the ages 70 and 90, they will differ by about one year:

the result for the age of 70 agreeing nearly with the living corresponding to the age 71; and the result for the age 90, agreeing nearly with the living at the age 89 of the Carlisle tables.

Art. 11. Lemma. If according to a certain table of mortality, out of a, persons of the age of 10, there will arrive b, c, d, &c. to the age 20, 30, 40, &c.; and if according to the tables of mortality, gathered from the experience of a particular society, the decrements of life between the intervals 10 and 20, 20 and 30, 30 and 40, &c. is to the decrements in the aforesaid table between the same ages, proportioned to the number of living at the commencement of those intervals respectively, as 1 to n, 1 to n', 1 to n'', &c. it is required to construct a table of mortality of that society, or such as will give the above data.

Solution. According to the first table, the decrements of life from 10 to 20, 20 to 30, 30 to 40, &c. respectively, will be found by multiplying the number of living at the commencement of each period by $\frac{a-b}{a}$, $\frac{b-c}{b}$, $\frac{c-d}{c}$, &c., and therefore, in the Society proposed, the corresponding decrements will be found by multiplying the number of living at those ages by $\frac{a-b}{a}n$; $\frac{b-c}{b}n'$; $\frac{c-d}{c}n''$ &c.; and the number of persons who will arrive at the ages 20, 30, 40, &c. will be the numbers respectively living at the ages 10, 20, 30, &c. multiplied respectively by $\frac{\overline{1-n}.a+nb}{a}$, $\frac{\overline{1-n'}.b+n'c}{b}$, $\frac{\overline{1-n''}.c+n''d}{c}$, &c.; hence out of the number a, living at the age 10, there will arrive at the age 10, 20, 30, 40, 50, &c. the numbers $\overline{\overline{1-n}.a+nb}$; $\overline{\overline{1-n}.a+nb} \times \frac{\overline{1-n'}.b+nc}{b}$; $\overline{\overline{1-n}.a+nb} \times \frac{\overline{1-n'}.b+nc}{b} \times \frac{\overline{1-n''}.c+n''.d}{c}$; &c. and the numbers for the intermediate ages must be found by interpolation.

In the ingenious Mr. MORGAN'S sixth edition of PRICE'S Annuities, p. 183, vol. i. it is stated, that in the Equitable Assurance Society, the deaths have differed from the Northampton tables; and that from 10 to 20, 20 to 30, 30 to 40, 40 to 50, 50 to 60, and 60 to 80, it appears that the deaths in the Northampton tables were in proportion to the deaths which would be given by the experience of that society respectively, in the ratios of 2 to 1; 2 to 1; 5 to 3; 7 to 5, and 5 to 4. According to this, the decrements in 10 years of those now living at the ages 10, 20, 30, and 40, will be the number living at those ages multiplied respectively by ,0478; ,0730; ,1024; ,1284; and the deaths in twenty years of those now living at the age of 60, would be the number of those living multiplied by ,3163. And also, taking, according to the Northampton table, the living at the age of 10 years equal to 5675, I form a table for the number of persons living at

the ages	10	20	30	40	50	60	70	80
being	5675	5403,5	5010	4496	3919	3116	*	1197
and the log. of the number of persons living	3,75612	3,73268	3,69984	3,65283	3,59318	3,49360	*	

Consequently, if $a = 20$, $r = 10$, we have $\lambda\left(\mathrm{L}_{20}\right) = 3,73268$; $\lambda\left(\mathrm{L}_{40}\right) = \lambda\left(\mathrm{L}_{20}\right) - m - mp = 3,65283$; $\lambda\left(\mathrm{L}_{60}\right) = \mathrm{L}_{20} - m - mp - mp^2 - mp^3 = 3,49360$; $m.\overline{1+p} = ,07985$; and $mp^2 \times \overline{1+p} = 3,65283 - 3,49360 = ,15923$; hence $\lambda(p) = \frac{1}{2}\lambda\left(\frac{,15923}{,07985}\right) = ,149875$; and $p = 1,412131$; $\lambda(m) = \lambda(,07985) - \lambda(2,41243) = \bar{2},519874$; and $m = ,033013$; $\therefore \lambda(\varepsilon) = \frac{-m}{,412131}$ negative; $\therefore \lambda(g)$ is negative; $\lambda\lambda(g) = \lambda m - \lambda,412131 - ,0149875 \times 20 = \bar{2},6051$; $\lambda(d) = \lambda\left(\mathrm{L}_{20}\right) - \lambda(\varepsilon) = 3.73268 - ,080302 = 3,813$ sufficiently near; and our formula for the mortality between the ages of 20 and 60, which appears to me to be the experience of the Equitable Society, is $\lambda\left(L_x\right) =$ 3,813 —the number whose log. is $(\bar{2}.6051 + ,0149875\,x)$.

This formula will give

At the ages .	10	20	30	40	50	60	70	80
No. of living .	5703,2	5403,5	5007	4496	3862	3116	*	1500
Differs from the proposed by	28,2	0	+ 3	0	— 57	0	*	303

In the table of Art. 12, the column marked 1, represents the age; column marked 2, represents the number of persons living at the corresponding age; column marked 3, the error to be added to the number of living deduced from the formula, to give the number of living of the table for which the formula is constructed; column marked 4, gives the error in age, or the quantity to be added to the age in column 1, that would give the number of living in the original table, the same as in column 2. It may be proper to observe, that where the error in column 3 and 4 is stated to be 0, it is not meant to indicate that a perfect coincidence takes place, but that the difference is too small to be worth noticing.

Art. 12. $\lambda\left(\underset{x}{\mathrm{L}}\right) = \lambda(d) -$ number whose logarithm is $(\lambda^2(g) + x\,\lambda\,q)$.

	Northampton.			Deparcieux.			Sweden.			Carlisle.			Formula of supposed experience of the Equitable, Compared with supposed exp.		Formula of supposed experience of the Equitable, Compared with Carlisle.			
1	2	3	4	2	3	4	2	3	4	2	3	4	2	3	2	3	4	1
10							6013	0		6460	0	0	5703	−28	6460			
11							5974	−16	$-\frac{1}{3}$	6427	+4	$+\frac{1}{8}$	5677		6431			
12							5935	−22	$-\frac{1}{2}$	6393	+7	$+\frac{1}{4}$	5650		6400			
13							5894	−26	$-\frac{2}{3}$	6358	+10	$+\frac{1}{3}$	5622		$6368\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{16}$	
14							$5852\frac{1}{2}$	$-24\frac{1}{2}$	$-\frac{3}{8}$	6322	+13	$+\frac{1}{8}$	5594		6336	−1	$-\frac{1}{35}$	14
15	5423			848	0	0	5810	$-22\frac{1}{2}$	$-\frac{3}{8}$	6286	+14	$+\frac{1}{3}$	5564	not compared.	6302	−2	$-\frac{1}{21}$	15
16	5360	+13	$+\frac{1}{4}$	841	+1	$+\frac{1}{6}$	5767	−18	$-\frac{1}{2}$	6248	+13	$+\frac{4}{13}$	5534		$6268\frac{1}{2}$	$-7\frac{1}{2}$	$-\frac{1}{6}$	16
17	5297	+23	$+\frac{1}{2}$	$833\frac{1}{2}$	$+1\frac{1}{2}$	$+\frac{1}{4}$	5722	−12	$-\frac{1}{3}$	6210	+9	$+\frac{1}{5}$	5503		6233	−14	$-\frac{1}{3}$	17
18	5233	+29	$+\frac{1}{2}$	826	+2	$+\frac{1}{3}$	5677	−6	$-\frac{1}{7}$	6171	+5	$+\frac{1}{9}$	5470		$6196\frac{1}{2}$	$-20\frac{1}{2}$	$-\frac{1}{2}$	18
19	5168	+31	$+\frac{1}{2}$	819	+2	$+\frac{1}{3}$	5630	−3	$-\frac{1}{14}$	6131	+2	$+\frac{1}{21}$	5437		6159	−26	$-\frac{3}{5}$	19
20	5102	+30	$+\frac{1}{2}$	811	+3	$+\frac{1}{3}$	5583	−0	0	6090	0	0	5403	0	$6120\frac{1}{2}$	$-30\frac{1}{2}$	$-\frac{5}{7}$	20
21	5036	+24	$+\frac{1}{3}$	804	+2	$+\frac{1}{4}$	5534	−1	0	6048	−1	0	5368		6081	−34	$-\frac{5}{6}$	21
22	4969	+16	$+\frac{1}{5}$	796	+2	$+\frac{1}{4}$	5484	−1	0	6005	+0	0	5333		$6040\frac{1}{2}$	$-35\frac{1}{2}$	$-\frac{5}{6}$	22
23	4899	+11	$+\frac{1}{7}$	789	+1	$+\frac{1}{8}$	5434	−1	0	5962	+1	0	5295		$5998\frac{1}{2}$	$-35\frac{1}{2}$	$-\frac{5}{6}$	23
24	4830	+5	$+\frac{1}{13}$	781	+1	$+\frac{1}{8}$	5382	−4	$-\frac{1}{18}$	5917	+4	$+\frac{1}{10}$	5258		$5955\frac{1}{2}$	$-34\frac{1}{2}$	$-\frac{5}{6}$	24
25	4762	−2	$-\frac{1}{37}$	774	+0	0	5329	−6	$-\frac{1}{9}$	$5870\frac{1}{2}$	$+8\frac{1}{2}$	$+\frac{1}{5}$	5218	not compared.	5911	−32	$-\frac{5}{7}$	25
26	4689	−4	$-\frac{1}{19}$	766	+0	0	5275	−7	$-\frac{1}{8}$	5825	+11	$+\frac{1}{4}$	5178		5866	−30	$-\frac{5}{7}$	26
27	4616	−6	$-\frac{1}{13}$	757	+1	$+\frac{1}{8}$	5220	−7	$-\frac{1}{8}$	5777	+16	$+\frac{5}{14}$	5137		5819	−26	$-\frac{5}{9}$	27
28	4545	−10	$-\frac{1}{7,5}$	750	+0	0	5164	−6	$-\frac{1}{9}$	5729	+19	$+\frac{3}{8}$	5095		5771	−23	$-\frac{1}{2}$	28
29	4472	−12	$-\frac{1}{6}$	742	+0	0	5107	−4	$-\frac{1}{14}$	5679	+19	$+\frac{1}{3}$	5051		5722	−24	$-\frac{4}{9}$	29
30	4403	−22	$-\frac{1}{3}$	734	+0	0	5049	−0	0	$5628\frac{1}{2}$	$+13\frac{1}{2}$	$+\frac{1}{4}$	5007	−3	$5671\frac{1}{2}$	$-29\frac{1}{2}$	$-\frac{4}{7}$	30
31	4325	−15	$-\frac{1}{5}$	726	+0	0	$4989\frac{1}{2}$	$-1\frac{1}{2}$	$-\frac{1}{37}$	5578	+7	$+\frac{1}{8}$	4961		5620	−34	$-\frac{3}{5}$	31
32	4250	−15	$-\frac{1}{5}$	718	+0	0	4929	−1	0	5524	+4	$+\frac{1}{14}$	4914		5567	−39	$-\frac{5}{7}$	32
33	4174	−14	$-\frac{1}{5}$	710	+0	0	4868	−0	0	$5470\frac{1}{2}$	$+1\frac{1}{2}$	$+\frac{1}{37}$	4866		$5512\frac{1}{2}$	$-42\frac{1}{2}$	$-\frac{3}{4}$	33
34	4098	−13	$-\frac{1}{5}$	702	+0	0	4805	+3	$+\frac{1}{20}$	5416	+1	0	4817		$5456\frac{1}{2}$	$-39\frac{1}{2}$	$-\frac{5}{7}$	34
35	4021	−11	$-\frac{1}{7}$	694	+0	0	4741	+7	$+\frac{1}{9}$	5360	+2	$+\frac{1}{27}$	4767	not compared.	5399	−37	$-\frac{1}{2}$	35
36	3944	−11	$-\frac{1}{7}$	686	+0	0	4676	+12	$+\frac{1}{5}$	5303	+4	$+\frac{1}{14}$	4715		5341	−34	$-\frac{3}{5}$	36
37	3866	−6	$-\frac{1}{12}$	678	+0	0	4611	+17	$+\frac{1}{4}$	$5245\frac{1}{2}$	$+5\frac{1}{2}$	$+\frac{1}{10}$	4662		5281	−30	$-\frac{4}{7}$	37
38	3788	−3	$-\frac{1}{27}$	669	+2	$+\frac{1}{4}$	4544	+24	$+\frac{2}{5}$	5187	+7	$+\frac{1}{8}$	4608		$5219\frac{1}{2}$	$-25\frac{1}{2}$	$-\frac{4}{9}$	38
39	3709	+1	$+\frac{1}{75}$	661	+3	$+\frac{1}{3}$	4476	+28	$+\frac{1}{2}$	5127	+9	$+\frac{1}{6}$	4553		5157	−21	$-\frac{1}{3}$	39
40	3630	+5	$+\frac{1}{15}$	653	+4	$+\frac{1}{2}$	4407	+41	$+\frac{2}{3}$	5065	+10	$+\frac{1}{6}$	4496	0	5093	−18	$-\frac{1}{4}$	40
41	3551	+8	$+\frac{1}{9}$	645	+5	$+\frac{1}{2}$	4337	+46	$+\frac{2}{3}$	5004	+5	$+\frac{1}{13}$	4438		5027	−18	$-\frac{1}{4}$	41
42	3473	+11	$+\frac{1}{7}$	636	+7	+1	4266	+45	$+\frac{5}{9}$	4941	−1	0	4379		5960	−20	$-\frac{2}{7}$	42
43	3392	+12	$+\frac{1}{6}$	628	+8	+1	4194	+37	$+\frac{4}{9}$	4877	−8	$-\frac{1}{9}$	4319		4892	−23	$-\frac{1}{3}$	43
44	3312	+14	$+\frac{1}{6}$	619	+10	$+1\frac{1}{4}$	4121	+30	$+\frac{3}{8}$	4812	−14	$-\frac{1}{5}$	4257		4882	−24	$-\frac{1}{3}$	44
45	3235	+13	$+\frac{1}{6}$	611	+11	$+1\frac{3}{8}$	4047	+24	$+\frac{3}{10}$	4746	−19	$-\frac{1}{4}$	4194	not compared.	4751	−24	$-\frac{1}{3}$	45
46	3152	+18	$+\frac{1}{4}$	603	+12	$+1\frac{1}{2}$	3973	+18	$+\frac{2}{9}$	4678	−21	$-\frac{3}{10}$	4130		$4678\frac{1}{2}$	$-21\frac{1}{2}$	$-\frac{1}{3}$	46
47	3072	+20	$+\frac{1}{4}$	594	+13	$+1\frac{1}{2}$	3897	+14	$+\frac{1}{6}$	4610	−22	$-\frac{3}{10}$	4065		$4604\frac{1}{2}$	$-16\frac{1}{2}$	$-\frac{1}{4}$	47
48	2991	+23	$+\frac{1}{3}$	586	+13	$+1\frac{1}{2}$	3821	+10	$+\frac{1}{8}$	4541	−20	$-\frac{3}{10}$	3998		4529	−8	$-\frac{1}{8}$	48
49	2911	+25	$+\frac{1}{3}$	577	+13	$+1\frac{1}{2}$	3744	+7	$+\frac{1}{12}$	4471	−13	$-\frac{1}{5}$	3931		$4452\frac{1}{2}$	$+5\frac{1}{2}$	$+\frac{1}{11}$	49
50	2831	+26	$+\frac{1}{3}$	569	+12	$+1\frac{1}{2}$	3660	0	0	$4400\frac{1}{2}$	$-3\frac{1}{2}$	$-\frac{1}{17}$	3862	+57	4375	+22	$+\frac{1}{3}$	50
51	2752	+24	$+\frac{1}{3}$	560	+11	$+1\frac{1}{2}$	3587	−16	$-\frac{1}{6}$	4329	+9	$+\frac{1}{7}$	3793		$4296\frac{1}{2}$	$+31\frac{1}{2}$	$+\frac{1}{2}$	51
52	2672	+22	$+\frac{1}{4}$	552	+8	+1	3508	−32	$-\frac{1}{3}$	4256	+20	$+\frac{1}{3}$	3721		4215	+61	+1	52
53	2593	+19	$+\frac{1}{4}$	543	+6	$+\frac{3}{4}$	3428	−47	$-\frac{1}{2}$	4182	+29	$+\frac{3}{7}$	3649		4133	+78	$1\frac{1}{7}$	53
54	2514	+16	$+\frac{1}{5}$	536	+2	$+\frac{1}{4}$	3348	−62	$-\frac{2}{3}$	4108	+35	$+\frac{1}{2}$	3575		4050	+93	$1\frac{1}{4}$	54
55	2436	+12	$+\frac{1}{7}$	526	+0	0				4033	+40	$+\frac{6}{11}$	3501	not compared.	3966	+107	$1\frac{1}{2}$	55
56	2358	+8	$+\frac{1}{10}$							3957	+43	$+\frac{4}{7}$	3426		3881	+219		56
57	2280	+4	$+\frac{1}{20}$							3880	+44	$+\frac{1}{2}$	3350		$3794\frac{1}{2}$	not compared.	not compared.	57
58	2206	−4	$-\frac{1}{20}$							3803	+39	$+\frac{3}{7}$	3273		3706			58
59	2123	−3	$-\frac{1}{30}$							3724	+25	$+\frac{1}{4}$	3195		3169			59
60	2052	−14	$-\frac{1}{5}$							3646	−3	0	3116	0	3529			60
	$\lambda(d) = \underline{3},9265$ $\lambda^2(g) = \bar{1},11556$ $\lambda(q) = ,011213$			$\lambda(d) = \underline{3},1557$ $\lambda^2(g) = \bar{1},25095$ $\lambda(q) = ,00704$			$\lambda(d) = \underline{3},8703$ $\lambda^2(g) = \bar{2},82861$ $\lambda(q) = ,0131457$			$\lambda(d) = \underline{3},89063$ $\lambda^2(g) = \bar{2},784336$ $\lambda(q) = ,0120948$			$\lambda(d) = \underline{3},813$ $\lambda^2(g) = \bar{2},6051$ $\lambda(q) = ,0149875$		$\lambda(d) = \underline{3},86743$ $\lambda^2(g) = \bar{2},6051$ $\lambda(q) = ,0149875$			

CHAPTER II.

ARTICLE 1. The near proximity to the geometrical progression of the series expressing the number of persons living at equal small successive intervals of time during short periods, out of a given number of persons living at the commencement of those intervals, affords a very convenient mode of calculating values connected with life contingencies, for short limited periods; by offering a manner of forming general tables, applicable (by means of small auxiliary tables of the particular mortalities) to calculations for any particular mortality; and by easy repetition, to calculate the values for any length of period for any table of mortality we please.

If, for instance, it were required to find the value of an annuity of an unit for p years, on three lives of the age b, c, d, the rate of interest being such that the present value of an unit to be received at the expiration of one year, be equal to r, then the value of the first payment would be $\frac{L_{b+1}}{L_b} \times \frac{L_{c+1}}{L_c} \times \frac{L_{d+1}}{L_d} \times r$; and of the p^{th} payment the present value would be $\frac{L_{b+p}}{L_b} \times \frac{L_{c+p}}{L_c} \times \frac{L_{d+p}}{L_d} \times r^p$; but if $L_{b+p} = L_b \times \left(\frac{L_{b+1}}{L_b}\right)^p$ whether p be 1, 2, 3, &c. which will be the case when L_b, L_{b+1}, L_{b+2}, &c. form a geometrical progression, and similarly, if $L_{c+p} = L_c \times \left(\frac{L_{c+1}}{L_c}\right)^p$, and also, $L_{d+p} = L_d \times \left(\frac{L_{d+1}}{L_d}\right)^p$, the present value of the p^{th} payment will be $\left(\frac{L_{1:b,c,d}}{L_{b,c,d}}r\right)^p$; hence, if $\frac{L_{1:b,c,d}}{L_{b,c,d}}r$ be put $= a$, the value of the annuity will be $a + a^2 + a^3 + a^4 \ldots a^p = \frac{a - a^{p+1}}{1 - a} = \frac{1 - a^p}{a^{-1} - 1}$.

Art. 2. Consequently, let a general table be formed of the logarithm of $\frac{1-a^p}{a^{-1}-1}$ for every value of the log. of a^p; and also let a particular table be formed for every value of the log. of $\frac{L_{x+p}}{L_x}$ according to the particular table of mortality to be adopted; from the last table take the log. of $\frac{L_{b+p}}{L_b}$, $\frac{L_{c+p}}{L_c}$, $\frac{L_{d+p}}{L_d}$; and also from a table constructed for the purpose, take the log. of r^p, add these four logs. together, and the sum will be the log. of $\overline{a}|^p$, which being sought for in the general table, will give the log. of $\left(\frac{1-a^p}{a^{-1}-1}\right)$ which will be the log. of the annuity sought for the term p, on supposition of the geometrical progression being sufficiently near. Here I remark, that were it not for more general questions than the above, it would be preferable to have general tables formed for the values of $\frac{1-a^p}{a^{-1}-1}$, instead of the log. of such values; but from the consideration that for most purposes a table of the logs. of $\frac{1-a^p}{a^{-1}-1}$ will be found most convenient, I have had them calculated in preference.

Art. 3. The shorter the periods are, the nearer does the series of the number of persons living at the equal intervals of successive ages approximate to the geometrical progression; and consequently this mode, by the assumption of sufficiently short periods, and frequent repetitions, will answer for any degree of accuracy the given table of mortality will admit of, but then the labour will be increased in proportion.

Art. 4. There are different modes of obviating, in a great measure, this inconvenience, by assuming an accommodated ratio for the given age, instead of the real ratio, from amongst which I shall only for the present select a few. The first is as follows: find for every value of a, the log. of $\overset{y}{\underset{p}{\overset{1}{1}}}\Big| \frac{L_{x+y}}{L_x}$, that is, the log. of $\frac{L_{x+1}}{L_x} + \frac{L_{x+2}}{L_x} + \frac{L_{x+3}}{L_x} \ldots\ldots \frac{L_{x+p}}{L_x}$; seek this value in the general table, which will give the corresponding value of the log. of a^p; and construct a table of such values for every value of x, and adopt these values for log. of a^p, instead of the abovenamed values of the log. of $\frac{L_{x+p}}{L_x}$, for the determination of the values of the limited periods: the preference of this to the first proposed method consists in this; that if the series $\frac{1}{L_b} \times (L_{b+1} + L_{b+2} + L_{b+3} \ldots L_{b+p}) = \beta + \beta^2 + \beta^3 + \&c. \ldots \beta^p$, the series $\frac{L_{b+1}}{L_b}, \frac{L_{b+2}}{L_b}$, &c. being nearly in geometrical progression, and $\frac{L_{b+1}}{L_b} - \beta = \varepsilon_1$, $\frac{L_{b+2}}{L_b} - \beta^2 = \varepsilon_2$, &c. $\varepsilon_1, \varepsilon_2$, &c. will be small, and $\varepsilon_1 + \varepsilon_2 + \varepsilon_3 \ldots \varepsilon_p = o$, and therefore, if the series $\frac{L_{c+1}}{L_c}, \frac{L_{c+2}}{L_c}, \frac{L_{c+3}}{L_c}$, &c. and $\frac{L_{d+1}}{L_d}, \frac{L_{d+2}}{L_d}$, &c. formed accurately geometrical progressions, and the value of $\frac{L_{c+1} \times L_{d+1}}{L_c \times L_d} . r = m$, the value of the annuity for the term, would be accurately equal to $m\beta + m^2\beta^2 + m^3\beta^3 \ldots\ldots + m^p\beta^p + m\varepsilon_1 + m^2\varepsilon_2 + m^3\varepsilon_3 \ldots\ldots + m^p\varepsilon_p$, but because in general $\frac{L_{c+1}}{L_c}$, $\frac{L_{d+1}}{L_d}$ and r differ very little from unity, m will not differ much from unity; and therefore if p be not great, m, m^2, m^3, &c. will not differ much from unity; and consequently, as ε_1, ε_2, ε_3, &c. are small, $m\varepsilon_1 + m^2\varepsilon_2 + m^3\varepsilon_3 \ldots\ldots m^p\varepsilon_p$ will not differ much from $\varepsilon_1 + \varepsilon_2 + \varepsilon_3 + \ldots\ldots + \varepsilon_p$; but this has been shown to be 0; consequently $m\varepsilon_1 + m^2\varepsilon_2 + m^3\varepsilon_3 \ldots\ldots + m^p\varepsilon_p$ differs very little from 0, or in other words is very small; and consequently, the value of the annuity differs very little from $m\mathfrak{E} + m^2\mathfrak{E}^2\, m^3\mathfrak{E}^3, \ldots\ldots + m^p\mathfrak{E}^p$; and the same method of demonstration would apply with any one of the other ages, the remaining ages being supposed to possess the property of the accurate geometrical progression; notwithstanding this, however, as none of them probably will contain that property, but in an approximate degree, a variation in the above approximations may be produced of a small quantity of the second order; that is, if the order of the product of two small quantities; but, as in this approximation, I was only aiming at retaining the quantities of the first order, I do not consider this as affecting the result as far as the approximation is intended to reach: thus far with regard to the first accommodated ratios.

Art. 5. Moreover, on the supposition that L_c, L_{c+1}, L_{c+2}, ... L_{c+p}, and also L_d, L_{d+1}, L_{d+2} ... L_{d+p} are series in geometrical progression, and that $r.\frac{L_{c+1}}{L_c} \times \frac{L_{d+1}}{L_d} = m = n.q.$ Since the annuity for p years on the three lives is equal to $\frac{L_{b+1}}{L_b}.m + \frac{L_{b+2}}{L_b}.m^2 + \ldots\ldots \frac{L_{b+p}}{L_b}.m^p$ it follows that if $\frac{L_{b+1}}{L_b}.n + \frac{L_{b+2}}{L_b}.n^2 + \frac{L_{b+3}}{L_b}.n^3 \ldots\ldots \frac{L_{b+p}}{L_b}.n^p = \varepsilon.n + \varepsilon^2.n^2 + \varepsilon^3.n^3 \ldots\ldots + \varepsilon^p.n^p$ that if n be very nearly equal to m, $\frac{L_{b+1}}{L_b}.n.q + \frac{L_{b+2}}{L_b}.n^2.q^2 + \&c. \ldots\ldots \frac{L_{b+p}}{L_b}.n^p q^p$ which will be the value of the annuity on the three lives, will be nearly $= \varepsilon.n.q + \varepsilon^2.n^2.q^2 + \&c. \ldots\ldots \varepsilon^p.n^p.q^p$. If q were equal to unity, or, which is the same thing, $m=n$, the equality would be accurate; but it may not be so when m differs from 1; but the nearer n is to m, at least when the difference does not exceed certain limited small quantities, the nearer will be the coincidence. It appears therefore, that if instead of taking the accommodated ratio for ε^p so that $\frac{1}{L_b} \times (L_{b+1} + L_{b+2} + L_{b+3} \ldots L_{b+p}) = \varepsilon + \varepsilon^2 + \varepsilon^3 \ldots\ldots \varepsilon^n$ it will be preferable generally to take it so that $\frac{1}{L_b} \times (n L_{b+1} + n^2 L_{b+2} + n. L_{b+3} \&c. \ldots\ldots n^p L_{b+p}) = \varepsilon + \varepsilon^2 + \varepsilon^3 \&c. \ldots \varepsilon^p$ in which n is between m and 1, the nearer m the better generally, though possibly not universally so throughout the whole limit. And the second method I use for increasing the accuracy, is to adopt an accommodated ratio, or ε^p, so that $\frac{1}{L_b} \times \left(1{,}05^{-1} L_{b+1} + 1{,}05^{-2} L_{b+2} + \&c. \ldots 1{,}05^p L_{b+p}\right) = \overline{1{,}05}|^{-1} \varepsilon + \overline{1{,}05}|^{-2} \varepsilon^2 + \overline{1{,}05}|^{-3} \varepsilon^3 \ldots \overline{1{,}05}|^{-p} \varepsilon^p$. Another method which might have its peculiar advantage, is to assume $\varepsilon^p = \overline{\frac{L_{b+\frac{1}{2}p}}{L_b}}|^{\frac{1}{2}p}$ under the idea of using a mean ratio.

The General Tables.*

Art. 6. I have had three general tables calculated for fixed periods, Numbers 1, 2, and 3. Number 1, for pe-

* The chief of the arithmetical operations in the constructions of most of the tables were performed under my direction, by Mr. DAVID JONES, of N°. 10, King-street, Soho; and, as far as my leisure would allow, I have endeavoured to assure myself of their accuracy by different inspections.

riods of ten years; that is, for $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$, corresponding to a given value of $\lambda(a^{10})$. N°. 2, for seven years, or for $\lambda\left(\frac{1-a^{7}}{a^{-1}-1}\right)$, corresponding to $\lambda(a^{7})$, and the 3d for five years, or for $\lambda\left(\frac{1-a^{5}}{a^{-1}-1}\right)$, corresponding to $\lambda(a^{5})$; calculated (whether $p=10$, 7 or 5) for every value of $\lambda(a^{p})$, answering to $\bar{3},00$; $\bar{3},01$; $\bar{3},02$, &c. . . . . *o*. The first column containing the aforesaid value of $\lambda.(a^{p})$, corresponding to which, in an horizontal line, is placed the log. of $\frac{1-a^{p}}{a^{-1}-p}$, and between each successive value is placed the difference, retaining a decimal figure more; at the head of the other columns for the proportional parts of the differences, are placed a column showing the number of cyphers to be prefixed to the differences entered in the column following, which are headed $\left\{\begin{matrix}1 & 2 & 3 & 4 & \\ 9 & 8 & 7 & 6 & 5\end{matrix}\right\}$ nearest under 1, 2, 3, 4 and 5, and opposite the number; suppose $\bar{2},16$ of table log. of a^{10}, stands $\left.\begin{matrix}0275, & 0550, & 0826, & 1101, & \\ 2477, & 2202, & 1926, & 1651, & 1376\end{matrix}\right\}$, the upper, with the addition of the two cyphers, give the proportional parts for ,001, 002, 003, ,004, 005: and the under, with the two cyphers, shows the proportional parts for ,009, 008, 007, 006; and the reason of choosing this arrangement, is the advantage which it offers of proof of correctness; thus the sum of the higher an lower numbers of each of the above row with the two cyphers = 002752, which is double ,001376, and equal to the whole difference between the successive terms.

Let it be required to find the logarithm of $\left(\frac{1-a^{10}}{a^{-1}-1}\right)$, corresponding to log. of $a^{10}=\bar{1}.7954$. In the General Table I,

Opposite to $\bar{1}.79$ we have . .	,88868
For ,005 we have proportional part .	256
For ,0004 . ditto . . .	20
The sum .	,89144 is the answer.

If log. of a^p is less than $\bar{3},00$, then it will be necessary to calculate $\lambda\left(\frac{1-a^p}{a^{-1}-1}\right)$ by common methods, as the tables do not go lower. And generally it will be then sufficient, omitting a^p, only to calculate the value of $-\lambda(a^{-1}-1)$; but from this, if more accuracy be required, subtract the number whose common logarithm is $(\bar{1},6378+\lambda(r)^p)$.

If $\lambda\left(\frac{1-a^p}{a^{-1}-1}\right)$ be given, and $\lambda(a)$ be required, proceed thus, $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$ being $=,89144$ for example. In Table I, the next value of

$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$ is ,88868 to which $\lambda(a^{10})$ corresponding is $\bar{1},79$			
Difference ,00256 belonging to $\bar{1}.79$ gives	. .		,005
Difference ,00020	. . .	ditto	,0004
$\therefore$ if $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)=,89144$		then we have $\lambda(a^{10})=\bar{1},7954$	

If $\lambda(a^p)$ is less than $\bar{3}$, proceed thus: put the given value of $\lambda\left(\frac{1-a^p}{a^{-1}-1}\right)=\lambda q$, and we have the common logarithm of $a=-p\times\lambda(1+q^{-1})+$ a small correction if great accuracy be required; which correction is nearly equal to $p\times$ the number whose common log. is $\left\{1.6378-\lambda q-\overline{p+1}.(1+q^{-1})\right\}$

These methods and tables only apply immediately to $\lambda\left(\frac{1-a^p}{a^{-1}-1}\right)$ when a is a proper fraction; but if a be greater than unity, put it equal to b^{-1}, then will b be a proper fraction; but $\frac{1-a^p}{a^{-1}-1}=\frac{a^p-1}{1-a^{-1}}=\frac{b^{-p}-1}{1-b}=b^{-p-1}\times\frac{1-b^p}{b^{-1}-1}=a^{p+1}\times\left(\frac{1-b^p}{b^{-1}-1}\right)$; consequently $\lambda\left(\frac{1-a^p}{a^{-1}-1}\right)=\overline{p+1}.\lambda(p)+\lambda\left(\frac{1-b^p}{b^{-1}-1}\right)$ I have likewise had Table IV. calculated, which is a general table, for the common log. of $\left(\frac{1}{a^{-1}-1}\right)$, corresponding to a given value of λa, commencing with $\lambda(a) = \bar{1}.7$; $\bar{1},701$; $\bar{1},702$, &c. with the differences between them. I have not, in this table, had the proportional parts inserted, though it would be attended with advantage, as the table is not meant to be of general use; but only given to be applied for rough purposes, or where accuracy is not particularly required for calculating at once the value of a life annuity for the whole term of life, or the whole remaining terms of life, after a given term, by considering the present value of each successive payment to form the successive terms of a geometrical progression whose first term and common ratio are each equal to *a*. And as $\lambda\left(\frac{1}{a^{-1}-1}\right)$ will represent the log. of the sum of the said geometrical progression, it will likewise express approximatively the logarithm of the value required. For many purposes, a table of $\frac{1}{a^{-1}-1}$, answering to given values of *a*, would be preferable, but not for general purposes.

Art. 7. I have already, in Art. 4 and 5, Chap. II, introduced the term accommodated ratios, or chances, and endeavoured to explain the methods to be adopted to reap the advantage of the ideas there expressed. Table V, for Carlisle, Deparcieux, and Northampton, are the logarithms of tenth terms of the accommodated ratios, or the logarithms of the accommodated chances for living ten years, calculated according to a mode laid down in Art. 5, Chap. II; that is, it expresses for every age, or value of *b*, the logarithm of ϵ^{10}, when $\frac{1}{L_b} \times (1,05^{\cdot -1} L_{b+1} + 1,05^{\cdot -2} L_{b+2} + \text{\&c.} \ldots 1,05^{\cdot -p} L_{b+p})$ is equal to $1,05^{\cdot -1}\epsilon + 1,05^{\cdot -2}\epsilon^2 + \text{\&c.} \ldots 1,05^{\cdot -10}\epsilon^{10}$. and to show, by example, how these are calculated, let it be required to find the logarithm of the accommodated chance for living ten years, for the age 20, calculated according to the Carlisle table upon the consideration of interest at 5 per cent. According to the Carlisle tables, I find $\lambda\, \overset{\overbrace{1,05^{-1}}}{\underset{10}{\overset{1}{1}}}\Big|_{20}$; that is, the logarithm of the annuity of one pound on a life of 20, for ten years, at 5 per cent $=$,87176, and putting $a = 105^{-1} \cdot \beta$, by hypothesis we shall have $\lambda\, \underset{10}{\overset{1}{1}}\Big| a^{x}$; that is the logarithm of $(a + a^2 + a^3 \ldots a^{10}) =$,87176; that is, $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right) =$,87176; hence proceeding, as shown above, to find from General Table I. $\lambda(a^{10})$

Having given . .	,87176	$= \lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		
We have next less $=$	,86842	corresponding to	. . .	$\bar{1}$.75
	,00334	difference		
	,00302	proportional part	. . .	,006
	30	. . ditto	. . . .	,0006
	2	. . ditto	. . . .	,00004
	.87176	corresponds to	. $\lambda(a^{10}) =$	$\bar{1}$.75664
			$\lambda(1,05^{10}) =$	,21189
				$\bar{1}$.96853 for the

log. of the accommodated chance to live 10 years at the Carlisle mortality.

In the same way may the accommodated chance be found for any other term, when general tables for the term are constructed, and from any other base of interest. I may observe, that by using different rates of interest, as a base for determining the accommodated chances, different degrees of accuracy may be obtained. See Art. 5. Chap. II.

Art. 8. Table VI. is the logarithm of the accommodated chances $\mathfrak{C}$ at every age, *b* for living one year, where $\mathfrak{C}$ is of such value that the sum of the geometrical progression $\frac{\mathfrak{C}}{1,05} + \frac{\mathfrak{C}^2}{1,05^2} +$ &c. ad infinitum, or, which is the same thing,

$\dfrac{1}{\frac{1,05}{\mathfrak{C}}-1}$ shall be equal to the value of the whole life annuity at five per cent. at such age, namely $\overset{1,05^{-1}}{\substack{1\\1}}\lfloor\underline{b}$; consequently $\dfrac{\mathfrak{C}}{1,05^{-1}}\times\left(1+\overset{1,05^{-1}}{\substack{1\\1}}\lfloor\underline{b}\right)=\overset{1,05^{-1}}{\substack{1\\1}}\lfloor\underline{b}$; $\therefore\ \lambda\,\mathfrak{C}=\lambda\left(\overset{1,05^{-1}}{\substack{1\\1}}\lfloor\underline{b}\right)+\lambda(1,05)-\lambda\left(\overset{1,05^{-1}}{\substack{1\\0}}\lfloor\underline{b}.\right)$ This table is constructed for Carlisle, Deparcieux, and Northampton, and is to be used in conjunction with Table IV., where only a rough value of the contingency is required; and though this table applies as the other tables of accommodated chances, to different rates of interest, still it would be of advantage more particularly *here* for the greater approximation to have similar tables constructed from the formula $\lambda(\mathfrak{C})=\lambda\left(\overset{r}{\substack{1\\1}}\lfloor\underline{b}\right)+\lambda(r^{-1})-\lambda\left(\overset{r}{\substack{1\\0}}\lfloor\underline{b}\right)$ for different values of r.

Art. 9. In calculating the value of life annuities for long periods, by means of adding together the values of portions of those periods, the portions of the distant periods contain factors of the real chance of living to these periods, and likewise of the discounted value of the money of which the payment is not immediate; thus if t be greater than 10,

$$\overset{r}{\substack{1\\1\\t}}\lfloor\underline{a,b,c}=\overset{r}{\substack{1\\1\\10}}\lfloor\underline{a,b,c}+\overset{r}{\substack{1\\11\\t}}\lfloor\underline{a,b,c}=\overset{r}{\substack{1\\1\\10}}\lfloor\underline{a,b,c}+\frac{\mathrm{L}_{10:a,b,c}}{\mathrm{L}_{a,b,c}}\cdot r^{10}\times\overset{r}{\substack{1\\1\\(t-10)}}\lfloor\underline{a+10,b+10,c+10}.$$

It will be therefore convenient to have a table of the logarithm of the real chance of living 10, 20, 30 years, &c. and also for other terms; and some of these are given by Tables VII., VIII., IX.

Time will not allow me, for the present, to offer more than a very few examples of the method to be employed in calculating by these tables, which are as follow:

Example 1. Required, according to the Carlisle table, the value of a life annuity, for ten years, on the joint lives 30 and 40, at 3 per cent interest.

In Table VIII. for Carlisle, log. of accommodated chance for 10 years, at the age 30 . .	$= \bar{1}.9552$	
Ditto 40	$= \bar{1}.9383$	
Ditto λ 1,03 . . .	$= \bar{1}.8716$	
Sum . .	$\bar{1}.7651$	$= \lambda\ (a^{10})$

In Table I, $\bar{1}.76$ corresponds to . . .	.8734
In proportional parts ,005 corresponds to	.253
Ditto . . 0001 corresponds to	. 5
Consequently $\bar{1}$,7651 corresponds to .	.87604

which is the log. of the required value: the number corresponding to this is 7,5169, for the value of the annuity, according to the Carlisle mortality, at 3 per cent. on the joint lives 30 and 40; and by calculation from Mr. MILNE's tables, I find the value should be 7,5168; the difference of the two is evidently insignificant. In this way I calculated the log. of the value of the life annuity, at the Carlisle mortality, at 3 per cent. for 10 years, for the joint lives 0 and 10, 10 and 20, 20 and 30, 30 and 40, 40 and 50, 50 and 60, to be ,76580; ,90247; ,89139; ,87604; ,86295; ,81067; and the annuity, or the numbers corresponding to the said logarithms,

5,8318; 7,9874; 7,7874; 7,5169; 7,2937; 6,4665;

and, according to calculation from Mr. MILNE's tables, I get

5,8595; 7,992; 7,7906; 7,5168; 7,2916; 6,4679.

The difference between the two sets is insignificant, except perhaps in the values of $\overset{\overbrace{1,05^{-1}}}{\overset{1}{\tfrac{1}{10}}}\big|\underline{0,10}$; that is, the value of the annuity on the joint life of a child just born, with one of the age of 10, at 3 per cent. Had we divided the period in portions, the value might have been obtained as near as we pleased; or we should likewise have obtained greater accuracy, had we assumed an accommodated chance deduced at a more appropriate interest than 5 per cent. See Art. 5, Chap. II.

Example 2. Let it be required to find the value of a life annuity at 3 per cent. for 10 years, at the Carlisle mortality, for the five lives of the age 20, 30, 40, 45 and 50.

In Table VIII. log. of accom. chance for 10 years at age	20	$= \bar{1}.9685$
Ditto	30	$= \bar{1}.9552$
Ditto	40	$= \bar{1}.9383$
Ditto	45	$= \bar{1}.9367$
Ditto	50	$= \bar{1}.9292$
	$\lambda\ 1,05^{-10}$	$= \bar{1}.8716$
	$\lambda\ (a^{10})$	$= \bar{1}.5995$

This sought in Table I.; thus, $\bar{1},59$ giving		,79035
	,009	427
	,0005	23
gives		,79485 the N° to which log. is 6,2352

for the value of $\overset{\overbrace{1,03^{-1}}}{\overset{1}{\tfrac{1}{10}}}\big|\underline{20, 30, 40, 45, 50}$.

Example 3. Let it be required to find the value of $\overset{\overbrace{1,03^{-1}}}{\overset{1}{1}}\big|\underline{b, b+10}$ Carlisle mortality, when $b = 10$, that is, for the whole joint lives of 10 and 20. By dividing the whole in portions of ten years, the operation will stand thus for $\overset{\overbrace{1,03^{-1}}}{\overset{1}{\tfrac{1}{10}}}\big|\underline{b, b+10}$.

	$b=10$	$b=20$	$b=30$	$b=40$	$b=50$	$b=60$	$b=70$	$b=80$	
Log. of accom. ratio for 10 years =	$\bar{1}.9768$	$\bar{1}.9685$	$\bar{1}.9552$	$\bar{1}.9383$	$\bar{1}.9292$	$\bar{1}.8318$	$\bar{1}.6689$	$\bar{1}.3134$	from Tab. VIII. Carlisle.
	$\bar{1}.9685$	$\bar{1}.9552$	$\bar{1}.9383$	$\bar{1}.9292$	$\bar{1}.8318$	$\bar{1}.6689$	$\bar{1}.3134$	$\bar{2}.6695$	
$\lambda(1{,}03^{-10})=$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	1.8716	
sum . . =	$\bar{1}.8169$	$\bar{1}.7953$	$\bar{1}.7651$	$\bar{1}.7391$	$\bar{1}.6326$	$\bar{1}.3723$	$\bar{2}.8539$	$\bar{3}.8545$	
Nos corresponding to sum in Table I.	.90247	.89139	.87604	.86295	.81067	.69156	.48781	.19146	
Log. of ratios for 10 years =		$\bar{1}.97438$	$\bar{1}.94120$	$\bar{1}.89520$	$\bar{1}.83292$	$\bar{1}.75123$	$\bar{1}.57016$	$\bar{1}.16886$	
		$\bar{1}.96681$	$\bar{1}.92082$	$\bar{1}.85854$	$\bar{1}.77684$	$\bar{1}.59577$	$\bar{1}.19448$	$\bar{2}.36767$	
$\lambda\, 1{,}03^{-10}$ . . =		$\bar{1}.87163$	$\bar{1}.74325$	$\bar{1}.61488$	$\bar{1}.48651$	$\bar{1}.35814$	$\bar{1}.22977$	$\bar{1}.10139$	
The log. of the present worth of each portion =		.70421	.48131	.23157	$\bar{1}.90694$	$\bar{1}.39670$	$\bar{2}.48222$	$\bar{4}.82938$	

And the present worth of each, or the numbers corresponding to the last logarithms are arranged below.

For first	10 years	7.9886
2nd	ditto	5.0607
3d	d°	3.0291
4th	d°	1.7044
5th	d°	.8071
6th	d°	.2492
7th	d°	.0303
8th	d°	.0007
	sum	18.8701

As the method by which the logarithms of the present worth of the different portions are found, may not be seen by every reader, I will explain the operation in the third portion; that is, when the logarithm of the portion first found is anticipated for 20 years.

Resume	.87604
Table VII. log. of real chance for age 10 living 20 years . . .	$\bar{1}.94120$
Ditto 20 years living . .	$\bar{1}.92082$
$\lambda(1{,}03^{-20})$	$\bar{1}.74325$
	.48131

which differs but insignificantly from Mr. MILNE's table, which gives 18.873. In a similar way, I find the value of the joint lives for ages 20 and 30, at 3 per cent. and Carlisle mortality to be 16.745; which, according to Mr. MILNE's table, should be 16.749; which appears to be an insignificant difference.

Example 4. To find, when particular accuracy is not required, according to the formula for the whole of life, the approximate value of $\overbrace{{}^{1}_{1}\rfloor\underline{a, a+10}}^{1,03^{-1}}$ at the Carlisle mortality, when $a=10$, 20, 30, &c. call the logarithm of accommodated ratios for an unlimited time at the age a, R_a standing for the accommodated ratio in Table VI. at the age a.

$a =$	10	20	30	40	50	60	70	80	90
R_a	$\bar{1}.99529$	$\bar{1}.99455$	$\bar{1}.99265$	$\bar{1}.98991$	$\bar{1}.98546$	$\bar{1}.97514$	$\bar{1}.95755$	$\bar{1}.92461$	$\bar{1}.86660$
R_{a+10}	$\bar{1}.99455$	$\bar{1}.99265$	$\bar{1}.98991$	$\bar{1}.98546$	$\bar{1}.97514$	$\bar{1}.95755$	$\bar{1}.92461$	$\bar{1}.86660$	$\bar{1}.81282$
$\lambda\, 1{,}03^{-1}$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$
	$\bar{1}.97700$	$\bar{1}.97436$	$\bar{1}.96972$	$\bar{1}.96253$	$\bar{1}.94776$	$\bar{1}.91985$	$\bar{1}.86932$	$\bar{1}.77837$	$\bar{1}.66658$
Log. which corresponds to	$\bar{1}.26451$	1.20975 .00631	1.13083 .01062	1.03886 .00641	.88674 .00667	.68817 .00502	.45337 .00123	.17571 .00093	
		1.21606	1.14145	1.04527	.89341	.69319	.45460	.17664	
Numbers . . Instead of .	18.387 18.873	16.446 16.749	13.850 14.449	11.099 11.954	7.824 8.729	4.9339 5.565	2.8485 3.229	1.5019 1.589	

To find the value corresponding to $\bar{1}.66658$, not in the table, find the number corresponding complement of the log. $\bar{1}.6658$, which number is 2,159; subtract 1, and find the complement of the log. which is $= \bar{1}.9359165$, whose number is ,8628. Mr. MILNE's table gives .979. But as it is not always the same rate of interest which gives the best accommodated ratios, in order to try when, for instance, the interest of money is 3 per cent. what rate of interest should be used in determining the ratios, use the following table:*

Interest.		
1.08	$\lambda\,(1.08^{-1} \times 1.03) = \bar{1}.979$	nearly;
1.07	$\lambda\,(1.07^{-1} \times 1.03) = \bar{1}.983$	
1.06	$\lambda\,(1.06^{-1} \times 1.03) = \bar{1}.987$	
1.05	$\lambda\,(1.05^{-1} \times 1.03) = \bar{1}.991$	
1.04	$\lambda\,(1.04^{-1} \times 1.03) = \bar{1}.996$	

* This is not given as a perfect and unerring rule, but as a method in many cases useful, and which would be perfect for the accommodated ratio of one of the lives, if the other lives followed an exact geometrical ratio throughout; and that the real geometrical ratios were in that case used for them, provided that instead of comparing the said sum with the small table, we take for the base of interest the number whose logarithm is $-\lambda\,(1{,}03)$, when the interest is 3 per cent.; and it is to be recollected that the methods is only given as a rough approximation.

Add the logarithm of accommodated ratios, as given in the Table VI. of all the lives but one in question, together, and see which of those rates of interest it nearest agrees with, and use that to calculate the life left, and proceed so for every life; thus for $\overset{1,03^{-1}}{\underset{1}{1}}\lfloor\underline{30, 40}$; to find the rate of interest for 30, I observe that $R_{40} = \bar{1}.9899$ agrees nearest with 6 per cent. in the little table, and $R_{30} = \bar{1}.99265$ agrees nearest with 5 per cent., I therefore take 6 per cent. for the age 30, and for the other I take 5 per cent.: proceed thus:

Example 5.

R_{30} if calculated at 6 per cent.	$\bar{1}.99316$
R_{40} per table	$\bar{1}.98991$
$\lambda\ 1,05^{-1}$ . . . . =	$\bar{1}.98716$
	$\bar{1}.97023$
	1.14558
Proportionate parts . .	$.00327$
To which logarithm . .	1.14885
The N° corresponding is .	14.088
Instead of	14.449

Example 6.

$\overset{1,03^{-1}}{\underset{1}{1}}\lfloor\underline{40, 50}$

R_{40} at 6 per cent. . .	$\bar{1}.99060$
R_{50} at 6 per cent. . .	$\bar{1}.98632$
	$\bar{1}.98716$
	$\bar{1}.96408$
	$\bar{1}.05336$
	$.00102$
	1.06438
	11.598
Instead of	11.954

Example 7.

$\overset{1,03^{-1}}{\underset{1}{1}}\lfloor\underline{50, 60}$

R_{50} at 8 per cent. . . . =	$\bar{1}.98759$
R_{60} at 6 per cent. . . . =	$\bar{1}.97599$
$\lambda\ 1,03^{-1}$ . . . . . =	$\bar{1}.98716$
	$\bar{1}.95074$
	$.91357$
	$.00687$
	$.92044$
which log. corresponds . .	$.8318$
instead of	$.8729$

I observe that I have not given any table of the logarithm of the accommodated ratios for an unlimited term, except that calculated with 5 per cent. as a radix; but by the assistance of a table of life annuities, for single life at different rates per cent., this will enable us, independent of certain exceptions, to derive the quantity for the same rates per cent. for any radix at the per cent. contained in the second table; thus to find R_{50} Carlisle mortality, radix 8 per cent. I look to the Carlisle table of single lives at 8 per cent., and I find the value of the annuity on the life of $50 = 8.987$, I search the age to which this will correspond at 5 per cent. and I find sufficiently nearly 59,82 for the age corresponding, to which from my table (with the radix at 5 per cent.) for the log. of ratios I find $\bar{1}.97536$; to this I add log. of $\frac{1.08}{1.05}$; that is, ,01223, and we get $\bar{1}.98759$, the same as given on the other side. This method is accurately consistent with the definition of accommodated ratios for unlimited periods; and if this description of accommodated ratios at a certain rate per cent. be given for one table, for which at the same rate per cent. we have the value of single lives, we may find the same description of accommodated ratios for any other table of mortality for which, at the same rate per cent. we have a table of the value of single lives: thus, suppose the logarithm of this description of accommodated ratios be given for the Carlisle table at five per cent., and the same be required for the Northampton for the age 60, at the same rate; $\overbrace{\begin{matrix}1\\1\end{matrix}}^{1,05^{-1}}\!\Big|\underline{60}$ Northampton $= 8,392$, this being sought in the Carlisle table for $\overbrace{{}^{1}_{1}\lfloor^{x}}^{1,05^{-1}}$ gives $x = 62,41$ for the corresponding age; seek the logarithm of accommodated ratios for an unlimited term, corresponding to this for Carlisle, for the age 6,241, and we have $\bar{1}.9723$, agreeing with the table given.

Previously to concluding this chapter, I shall add a small table, which will be found very useful in the application of the methods here proposed.

n	Log. of $1,03^{-n}$	Log. of $1,035^{-n}$	Log. of $1,04^{-n}$	Log. of $1,045^{-n}$	Log. of $1,05^{-n}$
1	$\bar{1}.9871628$	$\bar{1}.9850597$	$\bar{1}.9829667$	$\bar{1}.9808837$	$\bar{1}.9788107$
2	$\bar{1}.9743256$	$\bar{1}.9701193$	$\bar{1}.9659333$	$\bar{1}.9617674$	$\bar{1}.9576214$
3	$\bar{1}.9614883$	$\bar{1}.9551790$	$\bar{1}.9489000$	$\bar{1}.9426511$	$\bar{1}.9364321$
4	$\bar{1}.9486511$	$\bar{1}.9402386$	$\bar{1}.9318666$	$\bar{1}.9235348$	$\bar{1}.9152428$
5	$\bar{1}.9358139$	$\bar{1}.9252983$	$\bar{1}.9148333$	$\bar{1}.9044185$	$\bar{1}.8940535$
6	$\bar{1}.9229767$	$\bar{1}.9103579$	$\bar{1}.8978000$	$\bar{1}.8853023$	$\bar{1}.8728642$
7	$\bar{1}.9101394$	$\bar{1}.8954176$	$\bar{1}.8807666$	$\bar{1}.8661860$	$\bar{1}.8516749$
8	$\bar{1}.8973022$	$\bar{1}.8804772$	$\bar{1}.8637333$	$\bar{1}.8470697$	$\bar{1}.8304856$
9	$\bar{1}.8844650$	$\bar{1}.8655369$	$\bar{1}.8466999$	$\bar{1}.8279534$	$\bar{1}.8092963$
10	$\bar{1}.8716278$	$\bar{1}.8505965$	$\bar{1}.8296666$	$\bar{1}.8088371$	$\bar{1}.7881070$

General Table I. $\lambda(a^{10})$, $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{3}$.00	,00163	,00	0200	0399	0599	0798	0998
	,00199,6		1796	1597	1397	1198	
$\bar{3}$.01	,0036,2		0200	0401	0601	0801	1002
	,00200,3		1803	1602	1402	1202	
$\bar{3}$.02	,00563		0201	0401	0602	0802	1003
	,00200,6		1805	1605	1404	1204	
$\bar{3}$.03	,00763		0201	0402	0603	0804	1005
	,00201,0		1809	1608	1407	1206	
$\bar{3}$.04	,00964		0202	0403	0605	0806	1008
	,00201,5		1814	1612	1411	1209	
$\bar{3}$.05	,01166		0202	0404	0606	0808	1010
	,00202,0		1818	1616	1414	1212	
$\bar{3}$.06	,01368		0202	0405	0607	0810	1012
	,00202,4		1822	1619	1417	1214	
$\bar{3}$.07	,01570		0203	0406	0608	0811	1014
	,00202,8		1825	1622	1420	1217	
$\bar{3}$.08	,01773		0203	0407	0610	0814	1017
	,00203,4		1831	1627	1424	1220	
$\bar{3}$.09	,01976		0204	0408	0611	0815	1019
	,00203,8		1834	1630	1427	1223	
$\bar{3}$.10	,02180		0204	0409	0613	0817	1022
	,00204,3		1839	1634	1430	1226	
$\bar{3}$.11	,02384		0205	1409	0614	0819	1024
	,00204,7		1842	1638	1433	1228	
$\bar{3}$.12	,02589		0205	0410	0616	0821	1026
	,00205,2		1847	1642	1436	1231	
$\bar{3}$.13	,02794		0206	0411	0617	0823	1029
	,00205,7		1851	1646	1440	1234	
$\bar{3}$.14	,03000		0206	0412	0618	0824	1031
	,00206,1		1855	1649	1443	1237	
$\bar{3}$.15	,03206		0207	0413	0620	0826	1033
	,00206,5		1859	1654	1446	1239	
$\bar{3}$.16	,00207		0207	0415	0622	0829	1037
	,00207,3		1866	1658	1451	1244	
$\bar{3}$.17	,03620		0208	0415	0623	0830	1038
	,00207,6		1868	1661	1453	1246	
$\bar{3}$.18	,03827		0208	0416	0624	0832	1041
	,00208,1		1873	1665	1457	1249	
$\bar{3}$.19	,04036		0209	0417	0626	0834	1043
	,00208,6		1877	1669	1460	1252	
$\bar{3}$.20	,04244		0209	0418	0627	0836	1046
	,00209,1		1882	1673	1464	1255	
$\bar{3}$.21	,04453		0210	0419	0629	0838	1048
	,00209,6		1886	1677	1467	1258	
$\bar{3}$.22	,04663		0210	0420	0630	0840	1051
	,00210,1		1891	1681	1471	1261	
$\bar{3}$.23	,04873		0211	0421	0632	0842	1053
	,00210,6		1895	1685	1474	1264	
$\bar{3}$.24	,05084		0211	0422	0633	0844	1056
	,00211,1		1900	1689	1478	1267	

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{3}$.25	,05295	,00	0212	0423	0635	0847	1059
	,00211,7		1905	1694	1482	1270	
$\bar{3}$.26	,05506		0212	0424	0637	0849	1061
	,00212,2		1910	1698	1485	1273	
$\bar{3}$.27	,05719		0213	0425	0638	0851	1064
	,00212,7		1914	1702	1489	1276	
$\bar{3}$.28	,05931		0213	0426	0640	0853	1066
	,00213,2		1919	1706	1492	1279	
$\bar{3}$.29	,06144		0214	0427	0641	0855	1069
	,00213,7		1923	1710	1496	1282	
$\bar{3}$.30	,06358		0214	0429	0643	0857	1072
	,00214,3		1929	1714	1500	1286	
$\bar{3}$.31	,06572		0215	0430	0644	0859	1074
	,00214,8		1933	1718	1504	1289	
$\bar{3}$.32	,06787		0215	0431	0646	0861	1077
	,00215,3		1938	1722	1507	1292	
$\bar{3}$.33	,07002		0216	0432	0648	0864	1080
	,00216,0		1944	1728	1512	1296	
$\bar{3}$.34	,07218		0216	0433	0649	0866	1082
	,00216,4		1948	1731	1515	1298	
$\bar{3}$.35	,07435		0217	0434	0651	0868	1085
	,00217,0		1953	1736	1519	1302	
$\bar{3}$.36	,07652		0218	0435	0653	0870	1089
	,00217,5		1958	1740	1523	1305	
$\bar{3}$.37	,07869		0218	0436	0654	0872	1090
	,00218,0		1962	1744	1526	1308	
$\bar{3}$.38	,08087		0219	0437	0656	0875	1094
	,00218,7		1968	1750	1531	1312	
$\bar{3}$.39	,08306		0219	0438	0658	0877	1096
	,00219,2		1973	1754	1534	1315	
$\bar{3}$.40	,08525		0220	0439	0659	0879	1099
	,00219,7		1977	1758	1538	1318	
$\bar{3}$.41	,08745		0220	0441	0661	0882	1102
	,00220,4		1984	1763	1543	1322	
$\bar{3}$.42	,08965		0221	0442	0663	0884	1105
	,00221,0		1989	1768	1547	1326	
$\bar{3}$.43	,09186		0221	0443	0664	0886	1107
	,00221,4		1993	1771	1551	1328	
$\bar{3}$.44	,09408		0222	0444	0666	0888	1111
	,00222,1		1999	1777	1555	1333	
$\bar{3}$.45	,09630		0223	0445	0668	0890	1113
	,00222,6		2003	1781	1558	1336	
$\bar{3}$.46	,09852		0223	0446	0670	0893	1116
	,00223,2		2009	1786	1562	1339	
$\bar{3}$.47	,10076		0224	0448	0671	0895	1119
	,00223,8		2014	1790	1567	1343	
$\bar{3}$.48	,10300		0224	0449	0673	0898	1122
	,00224,4		2020	1795	1571	1346	
$\bar{3}$.49	,10524		0225	0450	0675	0900	1125
	,00225,0		2025	1800	1575	1350	

General Table I. $\lambda\,(a^{10}),\ \lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda\,(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.50$	,10749	,00	0226	0451	0677	0902	1128
	,00225,6		2030	1805	1579	1354	
$\bar{3}.51$	,10975		0226	0452	0679	0905	1131
	,00226,2		2036	1810	1583	1357	
$\bar{3}.52$	,11201		0227	0454	0680	0907	1134
	,00226,8		2041	1814	1588	1361	
$\bar{3}.53$	,11428		0228	0455	0683	0910	1138
	,00227,5		2048	1820	1593	1365	
$\bar{3}.54$	,11655		0228	0456	0684	0912	1141
	,00228,1		2053	1825	1597	1369	
$\bar{3}.55$	,11883		0229	0457	0686	0915	1144
	,00228,7		2058	1830	1601	1372	
$\bar{3}.56$	,12112		0229	0458	0688	0917	1146
	,00229,2		2063	1834	1604	1375	
$\bar{3}.57$	,12341		0230	0460	0690	0920	1151
	,00230,1		2071	1841	1611	1381	
$\bar{3}.58$	,12571		0231	0461	0692	0922	1153
	,00230,6		2075	1845	1614	1384	
$\bar{3}.59$	,12802		0231	0462	0694	0925	1156
	,00231,2		2081	1850	1618	1387	
$\bar{3}.60$	,13033		0232	0464	0696	0928	1160
	,00231,9		2087	1855	1623	1391	
$\bar{3}.61$	,13265		0233	0465	0698	0930	1163
	,00232,5		2093	1860	1628	1395	
$\bar{3}.62$	,13497		0233	0466	0699	0932	1165
	,00233,0		2097	1864	1631	1398	
$\bar{3}.63$	,13730		0234	0468	0701	0935	1169
	,00233,8		2104	1870	1637	1403	
$\bar{3}.64$	,13964		0235	0469	0704	0938	1174
	,00234,5		2111	1876	1642	1407	
$\bar{3}.65$	,14199		0235	0470	0705	0940	1176
	,00235,1		2116	1881	1646	1411	
$\bar{3}.66$	,14434		0236	0472	0707	0943	1179
	,00235,8		2122	1886	1651	1414	
$\bar{3}.67$	,14670		0237	0473	0710	0946	1183
	,00236,6		2129	1893	1656	1420	
$\bar{3}.68$	,14906		0237	0474	0711	0948	1186
	,00237,1		2134	1897	1660	1423	
$\bar{3}.69$	,15143		0238	0476	0714	0952	1190
	,00237,9		2141	1903	1665	1427	
$\bar{3}.70$	,15381		0239	0477	0716	0954	1193
	,00238,5		2147	1908	1670	1431	
$\bar{3}.71$	,15620		0239	0478	0718	0957	1196
	,00239,2		2153	1914	1674	1435	
$\bar{3}.72$	,15859		0240	0480	0720	0960	1200
	,00239,9		2159	1919	1679	1439	
$\bar{3}.73$	,16099		0241	0481	0722	0962	1203
	,00240,6		2165	1925	1684	1444	
$\bar{3}.74$	,16339		0241	0483	0724	0965	1207
	,00241,3		2172	1930	1689	1448	

$\lambda\,(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.75$	,16581	,00	0242	0484	0726	0968	1210
	,00242,0		2178	1936	1694	1452	
$\bar{3}.76$	,16823		0243	0485	0728	0971	1214
	,00242,7		2184	1942	1699	1456	
$\bar{3}.77$	,17065		0244	0487	0731	0974	1218
	,00243,5		2192	1948	1705	1461	
$\bar{3}.78$	,17309		0244	0488	0733	0977	1221
	,00244,2		2198	1954	1709	1465	
$\bar{3}.79$	,17553		0245	0490	0735	0980	1225
	,00244,9		2204	1959	1714	1469	
$\bar{3}.80$	,17798		0246	0491	0737	0982	1228
	,00245,6		2210	1965	1719	1474	
$\bar{3}.81$	,18044		0246	0493	0739	0986	1232
	,00246,4		2218	1971	1725	1478	
$\bar{3}.82$	,18290		0247	0494	0741	0988	1236
	,00247,1		2224	1977	1730	1482	
$\bar{3}.83$	,18537		0248	0496	0743	0991	1239
	,00247,8		2230	1982	1735	1487	
$\bar{3}.84$	,18785		0249	0497	0746	0994	1243
	,00248,6		2237	1989	1740	1492	
$\bar{3}.85$	,19034		0249	0499	0748	0997	1247
	,00249,3		2244	1994	1745	1496	
$\bar{3}.86$	,19284		0250	0500	0750	1000	1251
	,00250,1		2251	2001	1751	1501	
$\bar{3}.87$	,19533		0251	0502	0753	1004	1255
	,00250,9		2258	2007	1756	1505	
$\bar{3}.88$	,19784		0252	0503	0755	1006	1258
	,00251,6		2264	2013	1761	1510	
$\bar{3}.89$	,20035		0252	0505	0757	1010	1262
	,00252,4		2272	2019	1767	1514	
$\bar{3}.90$	,20288		0253	0506	0760	1013	1266
	,00253,2		2279	2026	1772	1519	
$\bar{3}.91$	,20541		0254	0508	0762	1016	1271
	,00254,1		2287	2033	1779	1525	
$\bar{3}.92$	,20795		0255	0509	0764	1019	1274
	,00254,7		2292	2038	1783	1528	
$\bar{3}.93$	,21050		0256	0511	0767	1023	1279
	,00255,7		2301	2046	1790	1534	
$\bar{3}.94$	,21306		0256	0513	0769	1025	1282
	,00256,3		2307	2050	1794	1538	
$\bar{3}.95$	,21562		0257	0514	0772	1029	1286
	,00257,2		2315	2058	1800	1543	
$\bar{3}.96$	,21819		0258	0516	0774	1032	1290
	,00258,0		2322	2064	1806	1548	
$\bar{3}.97$	,22077		0259	0518	0776	1035	1294
	,00258,8		2329	2070	1812	1553	
$\bar{3}.98$	,22336		0260	0519	0779	1038	1298
	,00259,6		2336	2077	1817	1558	
$\bar{3}.99$	,22559		0260	0521	0781	1042	1302
	,00260,4		2344	2083	1823	1562	

General Table I. $\lambda\,(a^{10}),\ \lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}$.00	,22856	,00	0261	0523	0784	1046	1307
	,00261,4		2353	2091	1830	1568	
$\bar{2}$.01	,23117		0262	0524	0786	1048	1310
	,00262,0		2358	2096	1834	1572	
$\bar{2}$.02	,23379		0263	0526	0789	1052	1315
	,00263,0		2367	2104	1841	1578	
$\bar{2}$.03	,23642		0264	0528	0791	1055	1319
	,00263,8		2374	2110	1847	1583	
$\bar{2}$.04	,23906		0265	0529	0794	1059	1324
	,00264,7		2382	2118	1853	1588	
$\bar{2}$.05	,24171		0266	0531	0797	1062	1328
	,00265,6		2390	2125	1859	1594	
$\bar{2}$.06	,24036		0266	0533	0799	1065	1332
	,00266,3		2397	2130	1864	1598	
2.07	,24703		0267	0534	0801	1068	1335
	,00267,0		2403	2136	1869	1602	
$\bar{2}$.08	,24970		0269	0537	0806	1074	1343
	,00268,5		2417	2148	1880	1611	
$\bar{2}$.09	,25238		0269	0538	0807	1076	1345
	,00269,0		2421	2152	1883	1614	
$\bar{2}$.10	,25507		0270	0540	0810	1080	1350
	,00269,9		2429	2159	1889	1619	
$\bar{2}$.11	,25777		0271	0542	0812	1083	1354
	,00270,8		2437	2166	1896	1625	
$\bar{2}$.12	,26048		0272	0543	0815	1087	1359
	,00271,7		2445	2174	1902	1630	
$\bar{2}$.13	,26320		0273	0545	0818	1090	1363
	,00272,6		2453	2181	1908	1636	
$\bar{2}$.14	,26592		0274	0547	0821	1094	1368
	,00273,5		2462	2188	1915	1641	
$\bar{2}$.15	,26866		0275	0549	0824	1098	1373
	,00274,6		2471	2197	1922	1648	
$\bar{2}$.16	,27140		0275	0550	0826	1101	1376
	,00275,2		2477	2202	1926	1651	
$\bar{2}$.17	,27415		0276	0553	0829	1105	1382
	,00276,3		2487	2210	1934	1658	
$\bar{2}$.18	,27692		0277	0554	0832	1109	1386
	,00277,2		2495	2218	1940	1663	
$\bar{2}$.19	,27969		0278	0556	0834	1112	1391
	,00278,1		2503	2225	1947	1669	
$\bar{2}$.20	,28247		0279	0558	0837	1116	1396
	,00279,1		2512	2233	1954	1675	
$\bar{2}$.21	,28526		0280	0560	0840	1120	1401
	,00280,1		2521	2241	1961	1681	
$\bar{2}$.22	,28806		0281	0562	0843	1124	1406
	,00281,1		2530	2249	1968	1687	
$\bar{2}$.23	,29087		0282	0564	0846	1128	1410
	,00281,9		2537	2255	1973	1691	
$\bar{2}$.24	,29369		0283	0566	0849	1132	1415
	,00282,9		2546	2263	1980	1697	

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}$.25	,29652	,00	0284	0568	0852	1136	1420
	,00283,9		2555	2271	1987	1703	
$\bar{2}$.26	,29936		0285	0570	0855	1140	1425
	,00284,9		2564	2279	1994	1709	
$\bar{2}$.27	,30221		0286	0572	0858	1144	1430
	,00285,9		2573	2287	2001	1715	
$\bar{2}$.28	,30507		0287	0574	0860	1147	1434
	,00286,8		2581	2294	2008	1721	
$\bar{2}$.29	,30794		0288	0576	0864	1152	1440
	,00287,9		2591	2303	2015	1727	
$\bar{2}$.30	,31081		0289	0578	0867	1156	1445
	,00288,9		2600	2311	2022	1733	
$\bar{2}$.31	,31370		0290	0580	0870	1160	1450
	,00289,9		2609	2319	2029	1739	
$\bar{2}$.32	,31660		0291	0582	0873	1164	1455
	,00290,9		2618	2327	2036	1745	
$\bar{2}$.33	,31951		0292	0584	0876	1168	1460
	,00291,9		2627	2335	2043	1751	
$\bar{2}$.34	,32243		0293	0586	0879	1172	1465
	,00293,0		2637	2344	2051	1758	
$\bar{2}$.35	,32536		0294	0588	0882	1176	1470
	,00294,0		2646	2352	2058	1764	
$\bar{2}$.36	,32830		0295	0590	0885	1180	1475
	,00295,0		2655	2360	2065	1770	
$\bar{2}$.37	,33125		0296	0592	0888	1184	1481
	,00296,1		2665	2369	2073	1777	
$\bar{2}$.38	,33421		0297	0594	0891	1188	1485
	,00297,1		2674	2377	2080	1783	
2.39	,33718		0298	0596	0895	1193	1491
	,00298,2		2684	2386	2087	1789	
$\bar{2}$.40	,34016		0299	0599	0898	1197	1497
	,00299,3		2694	2394	2095	1796	
$\bar{2}$.41	,34316		0300	0601	0901	1201	1502
	,00300,3		2703	2402	2102	1802	
$\bar{2}$.42	,34316		0301	0603	0904	1206	1507
	,00301,4		2713	2411	2110	1808	
$\bar{2}$.43	,34917		0303	0605	0908	1210	1513
	,00302,5		2723	2420	2118	1815	
$\bar{2}$.44	,35220		0304	0607	0911	1214	1518
	,00303,6		2732	2429	2125	1822	
$\bar{2}$.45	,35523		0305	0609	0914	1219	1524
	,00304,7		2742	2438	2133	1828	
$\bar{2}$.46	,35828		0306	0612	0917	1223	1529
	,00305,8		2752	2446	2141	1835	
$\bar{2}$.47	,36134		0307	0614	0921	1228	1535
	,00306,9		2762	2455	2148	1841	
$\bar{2}$.48	,36441		0308	0616	0924	1232	1541
	,00308,1		2773	2465	2157	1849	
$\bar{2}$.49	,36749		0309	0618	0928	1237	1546
	,00309,2		2783	2474	2164	1855	

General Table I. $\lambda(a^{10})$, $\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{2}.50$	,37058	,00	0310	0621	0931	1241	1552
	,00310,3		2794	2482	2172	1862	
$\bar{2}.51$	,37368		0312	0623	0935	1246	1558
	,00311,5		2804	2492	2181	1869	
$\bar{2}.52$	,37680		0313	0625	0938	1250	1563
	,00312,6		2813	2501	2188	1876	
$\bar{2}.53$	,37993		0314	0628	0941	1255	1569
	,00313,8		2824	2510	2197	1883	
$\bar{2}.54$	,38306		0315	0630	0945	1260	1575
	,00314,9		2834	2519	2204	1889	
$\bar{2}.55$	,38621		0316	0632	0948	1265	1581
	,00316,1		2845	2529	2213	1897	
$\bar{2}.56$	,38937		0317	0635	0952	1269	1587
	,00317,3		2856	2538	2221	1904	
$\bar{2}.57$	,39255		0319	0637	0956	1274	1593
	,00318,5		2867	2548	2230	1911	
$\bar{2}.58$	,39573		0320	0639	0959	1278	1598
	,00319,6		2876	2557	2237	1918	
$\bar{2}.59$	,39893		0321	0642	0962	1283	1604
	,00320,8		2887	2566	2246	1925	
$\bar{2}.60$	,40213		0322	0644	0966	1288	1610
	,00322,0		2898	2576	2254	1932	
$\bar{2}.61$	,40536		0323	0647	0970	1293	1617
	,00323,3		2910	2586	2263	1940	
$\bar{2}.62$	,40859		0325	0649	0974	1298	1623
	,00324,5		2921	2596	2272	1947	
$\bar{2}.63$	,41183		0326	0651	0977	1302	1628
	,00325,6		2930	2605	2279	1954	
$\bar{2}.64$	,41509		0327	0654	0980	1307	1634
	,00326,8		2941	2614	2288	1961	
$\bar{2}.65$	,41836		0328	0657	0985	1313	1642
	,00328,3		2955	2626	2298	1970	
$\bar{2}.66$	,42164		0329	0659	0988	1318	1647
	,00329,4		2965	2635	2306	1976	
$\bar{2}.67$	,42493		0331	0661	0992	1322	1653
	,00330,6		2975	2645	2314	1984	
$\bar{2}.68$	,42833		0332	0664	0996	1328	1660
	,00331,9		2987	2655	2323	1991	
$\bar{2}.69$	,43156		0333	0666	1000	1333	1666
	,00333,2		2999	2666	2332	1999	
$\bar{2}.70$	,43490		0334	0669	1003	1338	1672
	,00334,4		3010	2675	2341	2006	
$\bar{2}.71$	,43824		0336	0671	1007	1343	1679
	,00335,7		3021	2686	2350	2014	
$\bar{2}.72$	,44159		0337	0674	1011	1348	1686
	,00337,1		3034	2697	2360	2023	
$\bar{2}.73$	,44496		0338	0676	1015	1353	1691
	,00338,2		3044	2706	2367	2029	
$\bar{2}.74$	,44835		0340	0679	1019	1358	1698
	,00339,6		3056	2717	2377	2038	

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{2}.75$	,45174	,00	0341	0682	1022	1363	1704
	,00340,8		3067	2726	2386	2045	
$\bar{2}.76$	,45515		0342	0685	1027	1369	1712
	,00342,3		3081	2738	2396	2054	
$\bar{2}.77$	,45857		0343	0687	1031	1374	1718
	,00343,5		3092	2748	2405	2061	
2.78	,46201		0345	0690	1035	1380	1725
	,00345,0		3105	2760	2415	2070	
$\bar{2}.79$	,46546		0346	0692	1038	1384	1731
	,00346,1		3115	2769	2423	2077	
$\bar{2}.80$	,46892		0348	0695	1043	1390	1738
	,00347,5		3128	2780	2433	2085	
$\bar{2}.81$	,47239		0349	0698	1047	1396	1745
	,00348,9		3140	2791	2442	2093	
$\bar{2}.82$	,47588		0350	0700	1051	1410	1751
	,00350,2		3152	2802	2451	2101	
$\bar{2}.83$	,47938		0352	0703	1055	1406	1758
	,00351,6		3164	2813	2461	2110	
$\bar{2}.84$	,48290		0353	0706	1059	1412	1765
	,00353,0		3177	2824	2471	2118	
$\bar{2}.85$	,48643		0354	0709	1063	1417	1772
	,00354,3		3189	2834	2486	2126	
$\bar{2}.86$	,48997		0356	0712	1067	1423	1779
	,00355,8		3202	2846	2491	2135	
$\bar{2}.87$	,49353		0357	0714	1071	1428	1786
	,00357,1		3214	2857	2500	2143	
$\bar{2}.88$	,49710		0359	0717	1076	1434	1793
	,00358,5		3227	2868	2510	2151	
$\bar{2}.89$	,50069		0360	0720	1080	1440	1800
	,00360,0		3240	2880	2520	2160	
$\bar{2}.90$	,50429		0361	0723	1084	1446	1807
	,00361,4		3253	2891	2530	2168	
$\bar{2}.91$	,50790		0363	0725	1088	1451	1814
	,00362,7		3264	2902	2539	2176	
$\bar{2}.92$	,51153		0364	0728	1093	1457	1821
	,00364,2		3278	2914	2549	2185	
$\bar{2}.93$	,51517		0366	0731	1097	1462	1828
	,00365,6		3290	2925	2559	2194	
$\bar{2}.94$	,51883		0367	0734	1101	1468	1836
	,00367,1		3304	2937	2570	2203	
$\bar{2}.95$	,52250		0369	0737	1106	1474	1843
	,00368,5		3317	2948	2580	2211	
$\bar{2}.96$	,52618		0370	0740	1110	1480	1850
	,00369,9		3329	2959	2589	2219	
$\bar{2}.97$	,52988		0371	0743	1114	1486	1857
	,00371,4		3343	2971	2600	2228	
$\bar{2}.98$	,53360		0373	0746	1119	1492	1865
	,00372,9		3356	2983	2610	2237	
$\bar{2}.99$	,53732		0374	0749	1123	1498	1872
	,00374,4		3370	2995	2620	2246	

General Table I. $\lambda\,(a^{10}),\ \lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda\,(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5	$\lambda\,(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
1.00	,54107	,00	0376	0752	1127	1503	1879	$\bar{1}$.25	,63964	,00	0415	0831	1246	1661	2077
	,00375,8		3382	3006	2631	2255			,00415,3		3748	3322	2907	2492	
1.01	,54483		0377	0755	1132	1510	1887	$\bar{1}$.26	,64380		0417	0833	1250	1667	2084
	,00377,4		3397	3019	2642	2264			,00416,7		3750	3334	2917	2500	
1.02	,54860		0379	0757	1136	1515	1894	$\bar{1}$.27	,64796		0418	0837	1255	1674	2092
	,00378,7		3408	3030	2651	2273			,00418,4		3766	3347	2929	2510	
1.03	,55239		0380	0761	1141	1521	1902	$\bar{1}$.28	,65215		0420	0840	1260	1680	2100
	,00380,3		3423	3042	2662	2282			,00420,0		3780	3360	2940	2520	
1.04	,55619		0382	0764	1146	1528	1910	$\bar{1}$.29	,65635		0422	0843	1265	1687	2109
	,00381,9		3437	3055	2673	2291			,00421,7		3795	3374	2952	2530	
1.05	,56001		0383	0767	1150	1533	1917	$\bar{1}$.30	,66056		0423	0847	1270	1693	2117
	,00383,3		3450	3066	2683	2300			,00423,3		3810	3386	2963	2540	
1.06	,56384		0385	0770	1155	1540	1925	$\bar{1}$.31	,66480		0425	0850	1275	1700	2125
	,00384,9		3464	3079	2694	2309			,00425,0		3825	3400	2975	2550	
1.07	,56769		0386	0773	1159	1546	1932	$\bar{1}$.32	,66905		0427	0853	1280	1707	2134
	,00386,4		3478	3091	2705	2318			,00426,7		3840	3414	2987	2560	
1.08	,57156		0388	0776	1164	1552	1940	$\bar{1}$.33	,67331		0428	0857	1285	1714	2143
	,00388,0		3492	3104	2716	2328			,00428,4		3856	3427	2999	2570	
$\bar{1}$.09	,57544		0389	0779	1168	1558	1947	$\bar{1}$.34	,67760		0430	0860	1290	1720	2151
	,00389,4		3505	3115	2726	2336			,00430,1		3871	3441	3011	2581	
$\bar{1}$.10	,57933		0391	0782	1173	1564	1955	$\bar{1}$.35	,68190		0432	0863	1295	1727	2159
	,00391,0		3519	3128	2737	2346			,00431,7		3885	3454	3022	2590	
$\bar{1}$.11	,58324		0393	0785	1178	1570	1963	$\bar{1}$.36	,68622		0434	0868	1302	1736	2170
	,00392,5		3533	3140	2748	2355			,00434,0		3906	3472	3038	2604	
1.12	,58717		0394	0788	1183	1577	1971	$\bar{1}$.37	,69056		0435	0869	1304	1739	2174
	,00394,2		3548	3154	2759	2365			,00434,7		3912	3478	3043	2608	
1.13	,59111		0396	0792	1188	1584	1980	$\bar{1}$.38	,69490		0437	0874	1311	1748	2185
	,00395,9		3563	3167	2771	2375			,00437,0		3933	3496	3059	2622	
1.14	,59507		0397	0794	1191	1588	1986	$\bar{1}$.39	,69927		0439	0877	1316	1755	2194
	,00397,1		3574	3177	2780	2383			,00438,7		3948	3510	3071	2632	
$\bar{1}$.15	,59904		0399	0798	1196	1595	1994	$\bar{1}$.40	,70366		0440	0881	1321	1762	2202
	,00398,8		3589	3190	2792	2393			,00440,4		3964	3523	3083	2642	
$\bar{1}$.16	,60303		0401	0801	1202	1602	2003	$\bar{1}$.41	,70806		0442	0884	1326	1768	2211
	,00400,5		3605	3204	2804	2403			,00442,1		3979	3537	3095	2653	
$\bar{1}$.17	,60703		0402	0804	1206	1608	2011	$\bar{1}$.42	,71249		0444	0888	1331	1775	2219
	,00402,1		3619	3217	2815	2413			,00443,8		3994	3550	3107	2663	
$\bar{1}$.18	,61105		0404	0827	1211	1615	2019	$\bar{1}$.43	,71692		0445	0890	1335	1780	2225
	,00403,7		3633	3230	2826	2422			,00445,0		4005	3560	3115	2670	
$\bar{1}$.19	,61509		0405	0811	1216	1621	2027	$\bar{1}$.44	,72137		0448	0896	1344	1792	2240
	,00405,3		3648	3242	2837	2432			,00448,0		4032	3584	3136	2688	
$\bar{1}$.20	,61914		0407	0814	1221	1628	2035	$\bar{1}$.45	,72585		0449	0898	1347	1796	2246
	,00406,9		3662	3255	2848	2441			,00449,1		4042	3593	3144	2695	
$\bar{1}$.21	,62321		0409	0817	1226	1634	2043	$\bar{1}$.46	,73035		0451	0902	1352	1803	2254
	,00408,5		3677	3268	2860	2451			,00450,8		4057	3606	3156	2705	
$\bar{1}$.22	,62729		0410	0820	1230	1640	2051	$\bar{1}$.47	,73485		0453	0905	1358	1811	2264
	,00410,1		3691	3281	2871	2461			,00452,7		4074	3622	3169	2716	
$\bar{1}$.23	,63140		0412	0824	1235	1647	2059	$\bar{1}$.48	,73938		0454	0909	1363	1818	2272
	,00411,8		3706	3294	2883	2471			,00454,4		4090	3635	3181	2726	
$\bar{1}$.24	,63551		0413	0826	1239	1652	2066	$\bar{1}$.49	,74393		0456	0912	1368	1824	2281
	,00413,1		3718	3305	2892	2489			,00456,1		4105	3649	3193	2737	

General Table I. $\lambda\,(a^{10}),\ \lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$.

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.50$	,74849	,00	0458	0916	1374	1832	2290
	,00458,0		4122	3664	3206	2748	
$\bar{1}.51$	,75307		0460	0920	1379	1839	2299
	,00459,8		4138	3678	3219	2759	
$\bar{1}.52$	,75766		0462	0923	1385	1846	2308
	,00461,6		4154	3693	3231	2770	
$\bar{1}.53$	,76228		0463	0927	1390	1853	2317
	,00463,3		4170	3706	3243	2780	
$\bar{1}.54$	,76691		0465	0930	1396	1861	2326
	,00465,2		4187	3722	3256	2791	
$\bar{1}.55$	,77156		0467	0933	1400	1867	2334
	,00466,7		4200	3734	3267	2800	
$\bar{1}.56$	,77623		0469	0938	1407	1876	2345
	,00469,0		4221	3752	3283	2814	
$\bar{1}.57$	,78092		0470	0941	1411	1882	2352
	,00470,4		4234	3763	3293	2822	
$\bar{1}.58$	,78562		0472	0945	1417	1890	2362
	,00472,4		4252	3779	3307	2834	
$\bar{1}.59$	,79035		0474	0948	1422	1896	2371
	,00474,1		4267	3793	3319	2845	
$\bar{1}.60$	,79509		0476	0952	1428	1904	2380
	,00476,0		4284	3808	3332	2856	
$\bar{1}.61$	,79985		0478	0956	1433	1911	2389
	,00477,8		4300	3832	3345	2867	
$\bar{1}.62$	,80463		0480	0959	1439	1918	2398
	,00479,6		4316	3837	3357	2878	
$\bar{1}.63$	,80942		0482	0963	1445	1926	2408
	,00481,5		4334	3852	3371	2889	
$\bar{1}.64$	,81424		0483	0967	1450	1933	2417
	,00483,3		4350	3866	3383	2900	
$\bar{1}.65$	,81907		0486	0971	1457	1943	2429
	,00485,7		4371	3886	3400	2914	
$\bar{1}.66$	,82393		0486	0973	1459	1946	2432
	,00486,4		4378	3891	3405	2918	
$\bar{1}.67$	,82879		0489	0978	1466	1955	2444
	,00488,8		4399	3910	3422	2933	
$\bar{1}.68$	,83368		0492	0983	1475	1967	2459
	,00491,7		4425	3934	3442	2950	
$\bar{1}.69$	,83859		0493	0985	1478	1970	2463
	,00492,5		4433	3940	3448	2955	
$\bar{1}.70$	,84351		0494	0989	1483	1978	2472
	,00494,4		4450	3955	3461	2966	
$\bar{1}.71$	,84846		0496	0993	1489	1985	2482
	,00496,3		4467	3970	3474	2978	
$\bar{1}.72$	,85342		0498	0996	1494	1992	2491
	,00498,1		4483	3985	3487	2989	
$\bar{1}.73$	,85840		0500	1000	1500	2000	2500
	,00499,9		4499	3999	3499	2999	
$\bar{1}.74$	,86340		0502	1004	1506	2008	2510
	,00501,9		4517	4005	3513	3011	

$\lambda(a^{10})$	$\lambda\left(\frac{1-a^{10}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.75$	,86842	,00	0504	1007	1511	2015	2519
	,00503,7		4533	4030	3526	3022	
$\bar{1}.76$	,87346		0506	1011	1517	2022	2528
	,00505,6		4550	4045	3539	3034	
$\bar{1}.77$	,87851		0507	1015	1522	2030	2537
	,00507,4		4567	4059	3552	3044	
$\bar{1}.78$	,88359		0509	1019	1528	2038	2547
	,00509,4		4585	4075	3566	3056	
$\bar{1}.79$	,88868		0511	1022	1534	2045	2556
	,00511,2		4611	4090	3578	3067	
$\bar{1}.80$	,89379		0513	1026	1539	2052	2566
	,00513,1		4618	4105	3592	3079	
$\bar{1}.81$	,89892		0515	1030	1545	2060	2575
	,00515,0		4635	4120	3605	3090	
$\bar{1}.82$	,90407		0517	1034	1550	2067	2584
	,00516,8		4651	4134	3618	3101	
$\bar{1}.83$	,90924		0519	1038	1556	2075	2594
	,00518,8		4669	4150	3632	3113	
$\bar{1}.84$	,91443		0521	1041	1562	2082	2603
	,00520,6		4685	4165	3644	3124	
$\bar{1}.85$	,91964		0523	1045	1568	2090	2613
	,00522,6		4703	4181	3658	3136	
$\bar{1}.86$	,92486		0524	1049	1573	2098	2622
	,00524,4		4720	4195	3671	3146	
$\bar{1}.87$	,93011		0526	1052	1578	2104	2631
	,00526,1		4735	4209	3683	3157	
$\bar{1}.88$	,93537		0528	1057	1585	2113	2642
	,00528,3		4755	4226	3698	3170	
$\bar{1}.89$	,94065		0530	1060	1590	2120	2650
	,00530,0		4770	4240	3710	3180	
$\bar{1}.90$	,94595		0532	1064	1596	2128	2660
	,00532,0		4788	4256	3724	3192	
$\bar{1}.91$	,95127		0534	1068	1601	2135	2669
	,00533,8		4804	4270	3737	3203	
$\bar{1}.92$	,95661		0536	1072	1607	2143	2679
	,00535,8		4822	4286	3751	3215	
$\bar{1}.93$	,96197		0538	1075	1613	2150	2683
	,00537,6		4838	4301	3763	3226	
$\bar{1}.94$	,96734		0540	1079	1619	2158	2698
	,00539,6		4826	4317	3777	3238	
$\bar{1}.95$	,97274		0541	1083	1624	2166	2707
	,00541,4		4873	4331	3790	3248	
$\bar{1}.96$	,97815		0543	1087	1630	2173	2717
	,00543,3		4890	4346	3703	3260	
$\bar{1}.97$	,98359		0545	1090	1636	2181	2726
	,00545,2		4907	4362	3716	3271	
$\bar{1}.98$	,98904		0547	1094	1642	2189	2736
	,00547,2		4925	4378	3830	3283	
$\bar{1}.99$	,99451						

General Table II. $\lambda(a^7), \lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$.

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.00$	$\bar{1}$,77356	,00	0227	0454	0681	0908	1135
	,00227,0		2043	1816	1589	1362	
$\bar{3}.01$	$\bar{1}$,77583		0227	0455	0682	0910	1137
	,00227,4		2047	1819	1592	1364	
$\bar{3}.02$	$\bar{1}$,77810		0228	0456	1683	0911	1139
	,00227,8		2050	1822	1595	1367	
$\bar{3}.03$	$\bar{1}$,78038		0228	0457	0685	0913	1142
	,00228,3		2055	1826	1598	1370	
$\bar{3}.04$	$\bar{1}$,78266		0229	0457	0686	0914	1143
	,00228,6		2057	1829	1600	1372	
$\bar{3}.05$	$\bar{1}$,78495		0229	0458	0688	0917	1146
	,00229,2		2063	1834	1604	1375	
$\bar{3}.06$	$\bar{1}$,78724		0230	0460	0689	0918	1148
	,00229,6		2066	1837	1607	1378	
$\bar{3}.07$	$\bar{1}$,78954		0230	0460	0690	0920	1150
	,00230,0		2070	1840	1610	1380	
$\bar{3}.08$	$\bar{1}$,79184		0231	0461	0692	0922	1153
	,00230,5		2075	1844	1614	1383	
$\bar{3}.09$	$\bar{1}$.79414		0231	0462	0692	0923	1154
	,00230,8		2077	1846	1616	1385	
$\bar{3}.10$	$\bar{1}$,79645		0231	0463	0694	0926	1157
	,00231,4		2083	1851	1620	1388	
$\bar{3}.11$	$\bar{1}$,79877		0232	0464	0695	0927	1159
	,00231,8		2086	1854	1623	1391	
$\bar{1}.12$	$\bar{1}$,80108		0232	0464	0697	0929	1161
	,00232,2		2090	1858	1625	1393	
$\bar{3}.13$	$\bar{1}$,80341		0233	0465	0698	0931	1164
	,00232,7		2094	1862	1629	1396	
$\bar{3}.14$	$\bar{1}$,80573		0233	0466	0700	0933	1166
	,00233,2		2099	1866	1632	1399	
$\bar{3}.15$	$\bar{1}$,80806		0234	0467	0701	0934	1168
	,00233,6		2102	1869	1635	1402	
$\bar{3}.16$	$\bar{1}$,81040		0234	0468	0703	0937	1171
	,00234,2		2108	1874	1639	1405	
$\bar{3}.17$	$\bar{1}$,81274		0235	0469	0704	0938	1173
	,00234,5		2111	1876	1642	1407	
$\bar{3}.18$	$\bar{1}$,81509		0235	0470	0705	0940	1175
	,00235,0		2115	1880	1645	1410	
$\bar{3}.19$	$\bar{1}$,81744		0236	0471	0707	0942	1178
	00,235,5		2120	1884	1649	1413	
$\bar{3}.20$	$\bar{1}$,81979		0236	0472	0708	0944	1180
	,00236,0		2124	1888	1652	1416	
$\bar{3}.21$	$\bar{1}$,82215		0237	0473	0710	0946	1183
	,00236,5		2129	1892	1656	1419	
$\bar{3}.22$	$\bar{1}$,82452		0237	0474	0711	0948	1185
	,00237,0		2133	1896	1659	1422	
$\bar{3}.23$	$\bar{1}$,82689		0237	0475	0712	0950	1187
	,00237,4		2137	1899	1662	1424	
$\bar{3}.24$	$\bar{1}$,82926		0238	0476	0714	0952	1190
	,00238,0		2142	1904	1666	1428	

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.25$	$\bar{1}$,83164	,00	0239	0477	0716	0954	1193
	,00238,5		2147	1908	1670	1431	
$\bar{3}.26$	$\bar{1}$,83403		0239	0478	0717	0956	1195
	,00239,0		2151	1912	1673	1434	
$\bar{3}.27$	$\bar{1}$,83641		0240	0479	0719	0958	1198
	,00239,5		2156	1916	1677	1437	
$\bar{3}.28$	$\bar{1}$,83881		0240	0480	0720	0960	1200
	,00240,0		2160	1920	1680	1440	
$\bar{3}.29$	$\bar{1}$,84121		0241	0481	0722	0962	1203
	,00240,5		2165	1924	1684	1443	
$\bar{3}.30$	$\bar{1}$,84361		0241	0482	0723	0964	1205
	,00240,9		2168	1927	1686	1445	
$\bar{3}.31$	$\bar{1}$,84602		0242	0483	0725	0966	1208
	,00241,5		2174	1932	1691	1449	
$\bar{3}.32$	$\bar{1}$,84844		0242	0484	0726	0968	1210
	,00241,9		2177	1935	1693	1451	
$\bar{3}.33$	$\bar{1}$,85086		0243	0485	0728	0970	1213
	,00242,5		2183	1940	1698	1455	
$\bar{3}.34$	$\bar{1}$,85328		0243	0486	0730	0973	1216
	,00243,2		2189	1946	1702	1459	
$\bar{3}.35$	$\bar{1}$,85571		0244	0487	0731	0974	1218
	,00243,6		2192	1949	1705	1462	
$\bar{3}.36$	$\bar{1}$,85815		0244	0488	0732	0976	1221
	,00244,1		2197	1953	1709	1463	
$\bar{3}.37$	$\bar{1}$,86059		0245	0489	0734	0979	1224
	,00244,7		2202	1958	1713	1468	
$\bar{3}.38$	$\bar{1}$,86304		0245	0490	0736	0981	1226
	,00245,2		2207	1962	1716	1471	
$\bar{3}.39$	$\bar{1}$,86549		0246	0492	0737	0983	1229
	,00245,8		2212	1966	1721	1475	
$\bar{3}.40$	$\bar{1}$,86795		0246	0492	0739	0985	1231
	,00246,2		2216	1970	1723	1477	
$\bar{3}.41$	$\bar{1}$,87041		0247	0494	0741	0988	1235
	,00246,9		2222	1975	1728	1481	
$\bar{3}.42$	$\bar{1}$,87288		0247	0495	0742	0990	1237
	,00247,4		2227	1979	1732	1484	
$\bar{3}.43$	$\bar{1}$,87535		0248	0496	0744	0992	1240
	,00247,9		2231	1983	1735	1487	
$\bar{3}.44$	$\bar{1}$,87783		0249	0497	0746	0994	1243
	,00248,5		2237	1988	1740	1491	
$\bar{3}.45$	$\bar{1}$,88032		0249	0498	0747	0996	1246
	,00249,1		2242	1993	1744	1495	
$\bar{3}.46$	$\bar{1}$,88281		0250	0499	0749	0999	1248
	,00249,7		2247	1998	1748	1498	
$\bar{3}.47$	$\bar{1}$,88530		0250	0500	0751	1001	1251
	,00250,2		2252	2002	1751	1501	
$\bar{3}.48$	$\bar{1}$,88780		0251	0502	0752	1003	1254
	,00250,8		2257	2006	1756	1505	
$\bar{3}.49$	$\bar{1}$,89031		0251	0503	0754	1006	1257
	,00251,4		2263	2011	1760	1508	

General Table II. $\lambda\,(a^7),\ \lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$.

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.50$	$\bar{1},89283$	,00	0252	0504	0756	1008	1260
	,00252,0		2268	2016	1764	1512	
$\bar{3}.51$	$\bar{1},89535$		0253	0505	0758	1010	1263
	,00252,6		2273	2021	1768	1516	
$\bar{3}.52$	$\bar{1},89787$		0253	0506	0759	1012	1266
	,00253,1		2278	2025	1772	1519	
$\bar{3}.53$	$\bar{1},90040$		0254	0507	0761	1015	1269
	,00253,7		2283	2030	1776	1522	
$\bar{3}.54$	$\bar{1},90294$		0254	0509	0763	1017	1272
	,00254,3		2289	2034	1780	1526	
$\bar{3}.55$	$\bar{1},90548$		0255	0510	0765	1020	1275
	,00255,0		2295	2040	1785	1530	
$\bar{3}.56$	$\bar{1},90803$		0256	0511	0767	1022	1278
	,00255,5		2300	2044	1789	1533	
$\bar{3}.57$	$\bar{1},91059$		0256	0512	0769	1025	1281
	,00256,2		2306	2050	1793	1537	
$\bar{3}.58$	$\bar{1},91315$		0257	0514	0770	1027	1284
	,00256,8		2311	2054	1798	1541	
$\bar{3}.59$	$\bar{1},91572$		0257	0515	0772	1030	1287
	,00257,4		2317	2059	1802	1544	
$\bar{3}.60$	$\bar{1},91829$		0258	0516	0774	1032	1290
	,00258,0		2322	2064	1806	1548	
$\bar{3}.61$	$\bar{1},92087$		0259	0517	0776	1035	1294
	,00258,7		2328	2070	1811	1552	
$\bar{3}.62$	$\bar{1},92346$		0259	0518	0778	1037	1296
	,00259,2		2333	2074	1814	1555	
$\bar{3}.63$	$\bar{1},92605$		0260	0520	0780	1040	1300
	,00259,9		2339	2079	1819	1559	
$\bar{3}.64$	$\bar{1},92865$		0261	0521	0782	1042	1303
	,00260,6		2345	2085	1824	1564	
$\bar{3}.65$	$\bar{1},93125$		0261	0522	0784	1045	1306
	,00261,2		2351	2090	1828	1567	
$\bar{3}.66$	$\bar{1},93387$		0262	0524	0785	1047	1309
	,00261,8		2356	2094	1833	1571	
$\bar{3}.67$	$\bar{1},93648$		0263	0525	0788	1050	1313
	,00262,5		2363	2100	1838	1575	
$\bar{3}.68$	$\bar{1},93911$		0263	0526	0790	1053	1316
	,00263,2		2369	2106	1842	1579	
$\bar{3}.69$	$\bar{1},94174$		0264	0528	0791	1055	1319
	,00263,8		2374	2110	1847	1583	
$\bar{3}.70$	$\bar{1},94438$		0264	0529	0793	1058	1322
	,00264,4		2380	2115	1851	1586	
$\bar{3}.71$	$\bar{1},94702$		0265	0530	0795	1060	1326
	,00265,1		2386	2121	1856	1591	
$\bar{3}.72$	$\bar{1},94967$		0266	0532	0797	1063	1329
	,00265,8		2392	2126	1861	1595	
$\bar{3}.73$	$\bar{1},95233$		0267	0533	0800	1066	1333
	,00266,5		2399	2132	1866	1599	
$\bar{3}.74$	$\bar{1},95500$		0267	0534	0802	1069	1336
	,00267,2		2405	2138	1870	1603	

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{3}.75$	$\bar{1},95767$	,00	0268	0536	0804	1072	1340
	,00268,0		2412	2144	1876	1608	
$\bar{3}.76$	$\bar{1},96035$		0269	0537	0806	1074	1343
	,00268,5		2417	2148	1880	1611	
$\bar{3}.77$	$\bar{1},96303$		0269	0539	0808	1077	1347
	,00269,3		2424	2154	1885	1616	
$\bar{3}.78$	$\bar{1},96573$		0270	0540	0810	1080	1350
	,00270,0		2430	2160	1890	1620	
$\bar{3}.79$	$\bar{1},96843$		0271	0541	0812	1083	1354
	,00270,7		2436	2166	1895	1624	
$\bar{3}.80$	$\bar{1},97113$		0271	0543	0814	1085	1357
	,00271,3		2442	2170	1899	1628	
$\bar{3}.81$	$\bar{1},97385$		0272	0544	0816	1088	1361
	,00272,1		2449	2177	1905	1633	
$\bar{3}.82$	$\bar{1},97657$		0273	0546	0819	1092	1365
	,00272,9		2456	2183	1910	1637	
$\bar{3}.83$	$\bar{1},97930$		0273	0547	0820	1094	1367
	,00273,4		2461	2187	1914	1640	
$\bar{3}.84$	$\bar{1},98203$		0274	0549	0823	1097	1372
	,00274,3		2469	2194	1920	1646	
$\bar{3}.85$	$\bar{1},98477$		0275	0550	0825	1100	1375
	,00275,0		2475	2200	1925	1650	
$\bar{3}.86$	$\bar{1},98752$		0276	0552	0827	1103	1379
	,00275,8		2482	2206	1931	1655	
$\bar{3}.87$	$\bar{1},99028$		0277	0553	0830	1106	1383
	,00276,5		2489	2212	1936	1659	
$\bar{3}.88$	$\bar{1},99305$		0277	0555	0832	1109	1387
	,00277,3		2496	2218	1941	1664	
$\bar{3}.89$	$\bar{1},99582$		0278	0556	0834	1112	1390
	,00278,0		2502	2224	1946	1668	
$\bar{3}.90$	$\bar{1},99860$		0279	0558	0836	1115	1394
	,00278,8		2509	2230	1952	1673	
$\bar{3}.91$	,00139		0280	0559	0839	1118	1398
	,00279,5		2516	2236	1957	1677	
$\bar{3}.92$	,00418		0280	0561	0841	1121	1402
	,00280,3		2523	2242	1962	1682	
$\bar{3}.93$	,00699		0281	0562	0843	1124	1406
	,00281,1		2530	2249	1968	1687	
$\bar{3}.94$	,00980		0282	0564	0846	1128	1410
	,00281,9		2537	2255	1973	1691	
$\bar{3}.95$	,01262		0283	0565	0848	1131	1414
	,00282,7		2544	2262	1979	1696	
$\bar{3}.96$	,01544		0283	0567	0850	1134	1417
	,00283,4		2551	2267	1984	1700	
$\bar{3}.97$	,01828		0284	0568	0853	1137	1421
	,00284,2		2558	2274	1989	1705	
$\bar{3}.98$	,02112		0285	0570	0855	1140	1425
	,00285,0		2565	2280	1995	1710	
$\bar{3}.99$	,02397		0286	0572	0858	1144	1430
	,00285,9		2573	2287	2001	1715	

General Table II. $\lambda(a^7)$, $\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$.

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{2}.00$	,02683	,00	0287	0573	0860	1147	1434
	,00286,7		2580	2294	2007	1720	
$\bar{2}.01$	,02969		0288	0575	0863	1150	1438
	,00287,5		2588	2300	2013	1725	
$\bar{2}.02$	,03257		0288	0577	0865	1153	1442
	,00288,3		2595	2306	2018	1730	
$\bar{2}.03$	,03545		0289	0578	0867	1156	1446
	,00289,1		2602	2313	2024	1735	
$\bar{2}.04$	,03834		0290	0580	0870	1160	1450
	,00290,0		2610	2320	2030	1740	
$\bar{2}.05$	,04124		0291	0582	0872	1163	1454
	,00290,8		2617	2326	2036	1745	
$\bar{2}.06$	,04415		0292	0583	0875	1167	1459
	,00291,7		2625	2334	2043	1750	
$\bar{2}.07$	,04707		0293	0585	0878	1170	1463
	,00292,5		2633	2340	2048	1755	
$\bar{2}.08$	,04999		0293	0587	0880	1174	1467
	,00293,4		2641	2347	2054	1760	
$\bar{2}.09$	,05293		0294	0588	0883	1177	1471
	,00294,2		2648	2354	2059	1765	
$\bar{2}.10$	,05587		0295	0590	0885	1180	1476
	,00295,1		2656	2361	2066	1771	
$\bar{2}.11$	,05882		0296	0592	0888	1184	1480
	,00296,0		2664	2368	2072	1776	
$\bar{2}.12$	,06178		0297	0594	0890	1187	1484
	,00296,8		2671	2374	2078	1781	
$\bar{2}.13$	,06475		0298	0596	0893	1191	1489
	,00297,8		2680	2382	2085	1787	
$\bar{2}.14$	,06772		0299	0597	0896	1194	1493
	,00298,6		2687	2389	2090	1792	
$\bar{2}.15$	,07071		0300	0599	0899	1198	1498
	,00299,5		2696	2396	2097	1797	
$\bar{2}.16$	,07370		0300	0601	0901	1202	1502
	,00300,4		2704	2403	2103	1802	
$\bar{2}.17$	,07671		0301	0603	0904	1205	1507
	,00301,3		2712	2410	2109	1808	
$\bar{2}.18$	,07972		0302	0604	0907	1209	1511
	,00302,2		2720	2418	2115	1813	
$\bar{2}.19$	,08274		0303	0606	0902	1212	1516
	,00303,1		2728	2425	2122	1819	
$\bar{2}.20$	,08577		0304	0608	0912	1216	1521
	,00304,1		2737	2433	2129	1825	
$\bar{2}.21$	,08882		0305	0610	0915	1220	1525
	,00305,0		2745	2440	2135	1830	
$\bar{2}.22$	,09187		0306	0612	0918	1224	1530
	,00305,9		2753	2447	2141	1835	
$\bar{2}.23$	,09493		0307	0614	0921	1228	1535
	,00306,9		2762	2455	2148	1841	
$\bar{2}.24$	,09799		0308	0616	0923	1231	1539
	,00307,8		2770	2462	2155	1847	

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{2}.25$	,10107	,00	0309	0618	0926	1235	1544
	,00308,8		2779	2470	2162	1853	
$\bar{2}.26$	,10416		0310	0620	0929	1239	1549
	,00309,8		2788	2478	2169	1859	
$\bar{2}.27$	,10726		0311	0621	0932	1243	1554
	,00310,7		2796	2486	2175	1864	
$\bar{2}.28$	,11037		0312	0623	0935	1247	1559
	,00311,7		2805	2494	2182	1870	
$\bar{2}.29$	,11348		0313	0625	0938	1251	1564
	,00312,7		2814	2502	2189	1876	
$\bar{2}.30$	,11661		0314	0627	0941	1255	1569
	,00313,7		2823	2510	2196	1882	
$\bar{2}.31$	,11975		0315	0629	0944	1258	1573
	,00314,6		2831	2517	2202	1888	
$\bar{2}.32$	,12289		0316	0631	0947	1262	1578
	,00315,6		2840	2525	2209	1894	
$\bar{2}.33$	,12605		0317	0633	0950	1267	1583
	,00316,7		2850	2534	2216	1900	
$\bar{2}.34$	,12921		0318	0635	0953	1271	1589
	,00317,7		2859	2542	2224	1906	
$\bar{2}.35$	,13239		0319	0637	0956	1275	1594
	,00318,7		2868	2550	2231	1912	
$\bar{2}.36$	,13558		0320	0639	0959	1279	1599
	,00319,7		2877	2558	2238	1918	
$\bar{2}.37$	,13898		0321	0641	0962	1283	1604
	,00320,7		2886	2566	2245	1924	
$\bar{2}.38$	,14198		0322	0644	0965	1287	1609
	,00321,8		2896	2574	2253	1931	
$\bar{2}.39$	,14520		0323	0646	0968	1291	1614
	,00322,8		2905	2582	2260	1937	
$\bar{2}.40$	,14843		0324	0648	0972	1296	1620
	,00323,9		2915	2591	2267	1943	
$\bar{2}.41$	,15167		0325	0650	0975	1300	1625
	,00324,9		2924	2599	2274	1949	
$\bar{2}.42$	,15492		0326	0652	0978	1304	1630
	,00325,9		2933	2607	2281	1955	
$\bar{2}.43$	,15818		0327	0654	0981	1308	1636
	,00327,1		2944	2617	2290	1963	
$\bar{2}.44$	,16145		0328	0656	0984	1312	1641
	,00328,1		2953	2625	2297	1969	
$\bar{2}.45$	,16473		0329	0658	0988	1317	1646
	,00329,2		2963	2634	2304	1975	
$\bar{2}.46$	,16802		0330	0661	0991	1321	1652
	,00330,3		2973	2642	2312	1982	
$\bar{2}.47$	,17132		0331	0663	0994	1326	1657
	,00331,4		2983	2651	2320	1988	
$\bar{2}.48$	,17464		0333	0665	0998	1330	1663
	,00332,5		2993	2660	2328	1995	
$\bar{2}.49$	,17796		0334	0667	1001	1334	1668
	,00333,6		3002	2669	2335	2002	

General Table II. $\lambda\left(a^{7}\right),\ \lambda\left(\frac{1-a^{7}}{a^{-1}-1}\right)$.

$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5	$\lambda(a^7)$	$\lambda\left(\frac{1-a^7}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{2}.50$	,18130	,00	0335	0669	1004	1339	1674	$\bar{2}.75$	,26850	,00	0365	0729	1094	1459	1824
	,00334,7		3012	2678	2343	2008			,00364,7		3282	2918	2553	2188	
$\bar{2}.51$	,18464		0336	0672	1007	1343	1679	$\bar{2}.76$	,27214		0366	0732	1099	1465	1831
	,00335,8		3022	2686	2351	2015			,00366,2		3296	2930	2563	2197	
$\bar{2}.52$	,18880		0337	0674	1011	1348	1685	$\bar{2}.77$	,27581		0367	0735	1102	1470	1837
	,00336,9		3032	2695	2358	2021			,00367,4		3307	2939	2572	2204	
$\bar{2}.53$	,19137		0338	0676	1014	1352	1691	$\bar{2}.78$	,27948		0369	0737	1106	1475	1844
	,00338,1		3043	2705	2367	2029			,00368,7		3318	2950	2581	2212	
$\bar{2}.54$	,19475		0339	0678	1018	1357	1696	$\bar{2}.79$	,28317		0370	0740	1110	1480	1851
	,00339,2		3053	2714	2374	2035			,00370,1		3331	2961	2591	2221	
$\bar{2}.55$	,19815		0340	0681	1021	1362	1702	$\bar{2}.80$	,28687		0370	0743	1114	1485	1857
	,00340,4		3064	2723	2383	2042			,00371,3		3343	2970	2599	2228	
$\bar{2}.56$	,20155		0342	0683	1025	1366	1708	$\bar{2}.81$	,29058		0373	0746	1118	1491	1864
	,00341,5		3074	2732	2391	2049			,00372,8		3355	2982	2610	2237	
$\bar{2}.57$	,20496		0343	0685	1028	1371	1714	$\bar{2}.82$	,29431		0374	0748	1122	1496	1870
	,00342,7		3084	2742	2399	2056			,00373,9		3365	2991	2617	2243	
$\bar{2}.58$	,20839		0344	0688	1032	1376	1720	$\bar{2}.83$	,29805		0375	0751	1126	1502	1877
	,00343,9		3095	2751	2407	2063			,00375,4		3379	3003	2628	2252	
$\bar{2}.59$	,21183		0345	0690	1035	1380	1725	$\bar{2}.84$	,30180		0377	0753	1130	1507	1884
	,00345,0		3105	2760	2415	2070			,00376,7		3390	3014	2637	2260	
$\bar{2}.60$	,21528		0346	0692	1039	1385	1731	$\bar{2}.85$	,30557		0378	0756	1134	1512	1891
	,00346,2		3116	2770	2423	2077			,00378,1		3403	3025	2647	2269	
$\bar{2}.61$	,21874		0347	0695	1042	1390	1737	$\bar{2}.86$	,30935		0379	0759	1138	1518	1897
	,00347,4		3127	2779	2432	2084			,00379,4		3415	3035	2656	2276	
$\bar{2}.62$	,22222		0349	0697	1046	1395	1744	$\bar{2}.87$	,31314		0381	0762	1142	1523	1904
	,00348,7		3138	2790	2441	2092			,00380,8		3427	3046	2666	2285	
$\bar{2}.63$	,22570		0350	0699	1049	1399	1749	$\bar{2}.88$	,31695		0382	0764	1146	1529	1911
	,00349,7		3147	2798	2448	2098			,00382,2		3440	3058	2675	2293	
$\bar{2}.64$	,22920		0351	0702	1053	1404	1756	$\bar{2}.89$	,32077		0384	0767	1151	1534	1918
	,00351,1		3160	2809	2458	2107			,00383,6		3452	3069	2685	2302	
$\bar{2}.65$	,23271		0352	0705	1057	1409	1762	$\bar{2}.90$	,32461		0385	0770	1155	1540	1925
	,00352,3		3171	2818	2466	2113			,00385,0		3465	3080	2695	2310	
$\bar{2}.66$	,23623		0354	0707	1061	1414	1768	$\bar{2}.91$	,32846		0386	0773	1159	1545	1932
	,00353,5		3182	2828	2475	2121			,00386,3		3477	3090	2704	2318	
$\bar{2}.67$	,23977		0355	0709	1064	1419	1774	$\bar{2}.92$	,33232		0388	0776	1163	1551	1939
	,00354,7		3192	2838	2483	2128			,00387,8		3490	3102	2715	2327	
$\bar{2}.68$	,24332		0356	0712	1068	1424	1780	$\bar{2}.93$	,33620		0389	0778	1168	1557	1946
	,00356,0		3204	2848	2492	2136			,00389,2		3503	3114	2724	2335	
$\bar{2}.69$	,24688		0357	0714	1072	1429	1786	$\bar{2}.94$	,34009		0391	0781	1172	1562	1953
	,00357,2		3215	2858	2500	2143			,00390,6		3515	3125	2734	2344	
$\bar{2}.70$	,25045		0358	0717	1075	1434	1792	$\bar{2}.95$	,34400		0392	0784	1176	1568	1960
	,00358,4		3226	2867	2509	2150			,00392,0		3528	3136	2744	2352	
2.71	,25403		0360	0719	1079	1439	1799	$\bar{2}.96$	,34792		0394	0787	1181	1574	1968
	,00359,7		3237	2878	2518	2158			,00393,5		3542	3148	2755	2361	
$\bar{2}.72$	,25763		0361	0722	1083	1444	1805	$\bar{2}.97$	,35185		0395	0790	1185	1580	1975
	,00361,0		3249	2888	2527	2166			,00394,9		3554	3159	2764	2369	
$\bar{2}.73$	,26124		0362	0724	1087	1449	1811	$\bar{2}.98$	,35580		0396	0793	1189	1585	1982
	,00362,2		3260	2898	2535	2173			,00396,3		3567	3170	2774	2378	
$\bar{2}.74$	,26486		0364	0727	1091	1454	1817	$\bar{2}.99$	,35976		0398	0796	1193	1591	1989
	,00363,5		3272	2908	2545	2181			,00397,8		3580	3182	2785	2387	

General Table II. $\lambda\left(a^{7}\right), \lambda\left(\frac{1-a^{7}}{a^{-1}-1}\right)$.

$\lambda(a^{7})$	$\lambda\left(\frac{1-a^{7}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.00$	,36374	,00	0399	0799	1198	1597	1997
	,00399,3		3594	3194	2795	2396	
$\bar{1}.01$	,36773		0401	0801	1202	1603	2004
	,00400,7		3606	3206	2805	2404	
$\bar{1}.02$	,37174		0402	0804	1207	1609	2011
	,00402,2		3620	3218	2815	2413	
$\bar{1}.03$	,37576		0404	0807	1211	1615	2019
	,00403,7		3633	3230	2826	2422	
$\bar{1}.04$	,37980		0405	0811	1216	1622	2027
	,00405,4		3649	3243	2838	2432	
$\bar{1}.05$	,38385		0406	0813	1219	1626	2032
	,00406,4		3658	3251	2845	2438	
$\bar{1}.06$	,38792		0408	0816	1225	1633	2041
	,00408,2		3674	3266	2857	2449	
$\bar{1}.07$	,39200		0410	0819	1229	1639	2050
	,00409,7		3687	3278	2868	2458	
$\bar{1}.08$	,39610		0411	0822	1234	1645	2056
	,00411,2		3701	3290	2878	2467	
$\bar{1}.09$	,40021		0413	0826	1238	1651	2064
	,00412,8		3715	3302	2890	2477	
$\bar{1}.10$	,40434		0414	0828	1243	1657	2071
	,00414,2		3728	3314	2899	2485	
$\bar{1}.11$	,40848		0416	0832	1247	1663	2079
	,00415,8		3742	3326	2911	2495	
$\bar{1}.12$	,41264		0417	0835	1252	1669	2087
	,00417,3		3756	3338	2921	2504	
$\bar{1}.13$	,41681		0419	0838	1257	1676	2096
	,00419,1		3772	3353	2934	2515	
$\bar{1}.14$	,42100		0420	0840	1261	1681	2101
	,00420,2		3782	3362	2941	2521	
$\bar{1}.15$	,42520		0422	0844	1266	1688	2110
	,00421,9		3797	3375	2953	2531	
$\bar{1}.16$	,42942		0424	0847	1271	1694	2118
	,00423,6		3812	3389	2965	2542	
$\bar{1}.17$	,43366		0425	0850	1275	1700	2126
	,00425,1		3826	3401	2976	2551	
$\bar{1}.18$	,43791		0427	0854	1280	1707	2134
	,00426,8		3841	3414	2988	2561	
$\bar{1}.19$	,44218		0428	0856	1284	1712	2141
	,00428,1		3853	3425	2997	2569	
$\bar{1}.20$	,44646		0430	0860	1290	1720	2150
	,00429,9		3869	3439	3009	2579	
$\bar{1}.21$	,45076		0432	0863	1295	1726	2158
	,00431,5		3884	3452	3021	2589	
$\bar{1}.22$	,45507		0433	0866	1299	1732	2166
	,00433,1		3898	3465	3032	2599	
$\bar{1}.23$	,45940		0435	0869	1304	1739	2174
	,00434,7		3912	3478	3043	2608	
$\bar{1}.24$	,46375		0436	0873	1309	1745	2182
	,00436,3		3927	3490	3054	2618	

$\lambda(a^{7})$	$\lambda\left(\frac{1-a^{7}}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.25$	,48811	,00	0438	0876	1314	1752	2190
	,00438,0		3942	3504	3066	2628	
$\bar{1}.26$	,47249		0439	0879	1318	1758	2197
	,00439,4		3955	3515	3076	2636	
$\bar{1}.27$	,47689		0441	0882	1324	1765	2206
	,00441,2		3971	3530	3088	2647	
$\bar{1}.28$	,48130		0443	0886	1329	1772	2215
	,00442,9		3986	3543	3100	2657	
$\bar{1}.29$	,48573		0445	0889	1334	1778	2223
	,00444,5		4001	3556	3112	2667	
$\bar{1}.30$	,49017		0446	0892	1339	1785	2231
	,00446,2		4016	3570	3123	2677	
$\bar{1}.31$	,49463		0448	0896	1343	1791	2239
	,00447,8		4030	3582	3135	2687	
$\bar{1}.32$	,49911		0450	0899	1349	1798	2248
	,00449,5		4046	3596	3147	2697	
$\bar{1}.33$	,50361		0451	0902	1353	1804	2256
	,00451,1		4060	3609	3158	2707	
$\bar{1}.34$	,50812		0453	0909	1359	1812	2265
	,00452,9		4076	3623	3170	2717	
$\bar{1}.35$	,51265		0455	0909	1364	1818	2273
	,00454,5		4090	3636	3182	2727	
$\bar{1}.36$	,51719		0456	0912	1369	1825	2281
	,00456,2		4106	3650	3193	2737	
$\bar{1}.37$	,52175		0458	0916	1373	1831	2289
	,00457,8		4120	3662	3205	2747	
$\bar{1}.38$	,52633		0460	0919	1379	1839	2299
	,00459,7		4137	3678	3218	2758	
$\bar{1}.39$	,53093		0461	0923	1384	1846	2307
	,00461,4		4153	3691	3230	2768	
$\bar{1}.40$	,53554		0463	0926	1389	1852	2315
	,00462,9		4166	3703	3240	2777	
$\bar{1}.41$	,54017		0465	0930	1394	1859	2324
	,00464,8		4183	3718	3254	2789	
$\bar{1}.42$	,54482		0467	0933	1400	1866	2333
	,00466,5		4199	3732	3266	2799	
$\bar{1}.43$	,54948		0468	0936	1404	1872	2341
	,00468,1		4213	3745	3277	2809	
$\bar{1}.44$	,55417		0470	0940	1410	1880	2350
	,00469,9		4229	3759	3289	2819	
$\bar{1}.45$	,55886		0472	0943	1415	1887	2359
	,00471,7		4245	3774	3302	2830	
$\bar{1}.46$	,56358		0474	0947	1421	1894	2368
	,00473,6		4262	3789	3315	2842	
$\bar{1}.47$	,56832		0475	0950	1425	1900	2376
	,00475,1		4276	3801	3326	2851	
$\bar{1}.48$	,57307		0477	0954	1431	1901	2385
	,00476,9		4292	3815	3338	2861	
$\bar{1}.49$	,57784		0479	0957	1436	1915	2394
	,00478,7		4308	3830	3351	2872	

General Table II. $\lambda(a^x)$, $\lambda\left(\frac{1-a^x}{a^{-1}-1}\right)$.

$\lambda(a^x)$	$\lambda\left(\frac{1-a^x}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5	$\lambda(a^x)$	$\lambda\left(\frac{1-a^x}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{1}.50$	,58262	,00	0480	0960	1441	1921	2401	$\bar{1}.75$	,70810	,00	0526	1052	1578	2104	2630
	,00480,2		4322	3842	3361	2881			,00526,0		4734	4208	3682	3156	
$\bar{1}.51$	,58742		0482	0964	1447	1929	2411	$\bar{1}.76$	,71336		0527	1055	1582	2109	2637
	,00482,2		4340	3858	3375	2893			,00527,3		4746	4218	3691	3164	
$\bar{1}.52$	,59225		0484	0968	1452	1936	2420	$\bar{1}.77$	,71863		0530	1059	1589	2118	2648
	,00483,9		4355	3871	3387	2903			,00529,6		4766	4237	3707	3178	
$\bar{1}.53$	,59709		0486	0971	1457	1943	2429	$\bar{1}.78$	,72392		0531	1062	1593	2124	2655
	,00485,7		4371	3886	3400	2914			,00531,0		4779	4248	3717	3186	
$\bar{1}.54$	,60194		0487	0975	1462	1950	2437	$\bar{1}.79$	,72924		0533	1067	1600	2133	2667
	,00487,4		4387	3899	3412	2924			,00533,3		4800	4266	3733	3200	
$\bar{1}.55$	,60682		0489	0979	1468	1957	2447	$\bar{1}.80$	,73457		0535	1069	1604	2139	2674
	,00489,3		4404	3914	3425	2936			,00534,7		4812	4278	3743	3208	
$\bar{1}.56$	,61171		0491	0982	1473	1964	2456	$\bar{1}.81$	,73992		0536	1072	1608	2144	2681
	,00491,1		4420	3929	3438	2947			,00536,1		4825	4289	3753	3217	
$\bar{1}.57$	,61662		0493	0985	1478	1971	2464	$\bar{1}.82$	,74528		0539	1077	1616	2154	2693
	,00492,7		4434	3942	3449	2956			,00538,5		4847	4308	3770	3231	
$\bar{1}.58$	,62155		0495	0989	1484	1978	2473	$\bar{1}.83$	,75067		0541	1081	1622	2163	2704
	,00494,6		4451	3957	3462	2968			,00540,7		4866	4326	3785	3244	
$\bar{1}.59$	,62649		0496	0993	1489	1986	2482	$\bar{1}.84$	,75608		0542	1085	1627	2169	2712
	,00496,4		4468	3971	3475	2978			,00542,3		4881	4338	3796	3254	
$\bar{1}.60$	,63146		0498	0997	1495	1993	2492	$\bar{1}.85$	,76150		0544	1088	1632	2176	2721
	,00498,3		4485	3986	3488	2990			,00544,1		4897	4353	3809	3265	
$\bar{1}.61$	,63644		0500	1000	1500	2000	2500	$\bar{1}.86$	,76694		0546	1092	1638	2184	2731
	,00500,0		4500	4000	3500	3000			,00546,1		4915	4369	3823	3277	
$\bar{1}.62$	,64144		0502	1004	1505	2007	2509	$\bar{1}.87$	,77240		0548	1096	1644	2192	2741
	,00501,8		4516	4014	3513	3011			,00548,1		4933	4385	3837	3289	
$\bar{1}.63$	,64646		0504	1007	1511	2015	2519	$\bar{1}.88$	,77788		0550	1100	1650	2200	2750
	,00503,7		4533	4030	3526	3022			,00550,0		4950	4400	3850	3300	
$\bar{1}.64$	,65150		0505	1011	1516	2021	2527	$\bar{1}.89$	,78338		0551	1103	1654	2206	2757
	,00505,3		4548	4042	3537	3032			,00551,4		4963	4411	3860	3308	
$\bar{1}.65$	,65655		0507	1015	1522	2030	2537	$\bar{1}.90$	,78889		0554	1108	1661	2215	2769
	,00507,4		4567	4059	3552	3044			,00553,8		4984	4430	3877	3323	
$\bar{1}.66$	,66162		0509	1018	1527	2036	2546	$\bar{1}.91$	,79443		0556	1111	1667	2222	2778
	,00509,1		4582	4073	3564	3055			,00555,5		5000	4444	3889	3333	
$\bar{1}.67$	,66671		0511	1022	1533	2044	2555	$\bar{1}.92$	,79999		0557	1115	1672	2229	2787
	,00511,0		4599	4088	3577	3066			,00557,3		5016	4458	3901	3344	
$\bar{1}.68$	,67182		0513	1025	1538	2051	2564	$\bar{1}.93$	,80556		0560	1119	1679	2238	2798
	,00512,7		4614	4102	3589	3076			,00559,5		5036	4476	3917	3357	
$\bar{1}.69$	,67695		0515	1029	1544	2058	2573	$\bar{1}.94$	,81116		0561	1122	1683	2244	2805
	,00514,6		4631	4117	3602	3088			,00561,0		5049	4488	3927	3366	
$\bar{1}.70$	,68209		0517	1033	1550	2066	2583	$\bar{1}.95$	,81677		0563	1126	1690	2253	2816
	,00516,5		4649	4132	3616	3099			,00563,2		5069	4506	3942	3379	
$\bar{1}.71$	,68726		0518	1036	1554	2072	2591	$\bar{1}.96$	,82240		0565	1129	1694	2258	2823
	,00518,1		4663	4145	3627	3089			,00564,6		5081	4517	3952	3388	
$\bar{1}.72$	,69244		0520	1040	1561	2081	2601	$\bar{1}.97$	,82804		0568	1137	1705	2274	2842
	,00520,2		4682	4162	3641	3121			,00568,4		5116	4547	3979	3419	
$\bar{1}.73$	,69764		0522	1044	1566	2088	2610	$\bar{1}.98$	,83373		0568	1137	1705	2273	2842
	,00522,0		4698	4176	3654	3132			,00568,3		5115	4546	3978	3410	
$\bar{1}.74$	,70286		0524	1047	1571	2095	2619	$\bar{1}.99$	,83941						
	,00523,7		4713	4190	3666	3142									

General Table III. $\lambda(a^5)$, $\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$.

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{3}$.00	$\bar{1}$,52519	,00	0266	0533	0799	1065	1332
	,00266,3		2397	2130	1864	1598	
$\bar{3}$.01	$\bar{1}$,52786		0267	0533	0800	1066	1333
	,00266,5		2399	2132	1866	1599	
$\bar{3}$.02	$\bar{1}$,53052		0267	0534	0802	1069	1336
	,00267,2		2405	2138	1870	1603	
$\bar{3}$.03	$\bar{1}$,53319		0268	0535	0803	1070	1338
	,00267,5		2408	2140	1873	1605	
$\bar{3}$.04	$\bar{1}$,53587		0268	0536	0804	1072	1340
	,00267,9		2411	2143	1875	1607	
$\bar{3}$.05	$\bar{1}$,53855		0268	0537	0805	1073	1342
	,00268,3		2415	2146	1878	1610	
$\bar{3}$.06	$\bar{1}$,54123		0269	0537	0806	1075	1344
	,00268,7		2418	2150	1881	1612	
$\bar{3}$.07	$\bar{1}$,54392		0269	0538	0807	1076	1346
	,00269,1		2422	2153	1884	1615	
$\bar{3}$.08	$\bar{1}$,54661		0270	0539	0809	1078	1348
	,00269,5		2426	2156	1887	1617	
$\bar{3}$.09	$\bar{1}$,54930		0270	0540	0810	1080	1350
	,00269,9		2429	2159	1889	1619	
$\bar{3}$.10	$\bar{1}$,55200		0270	0541	0811	1081	1352
	,00270,3		2433	2162	1892	1622	
$\bar{3}$.11	$\bar{1}$,55470		0271	0541	0812	1083	1354
	,00270,7		2436	2166	1895	1624	
$\bar{3}$.12	$\bar{1}$,55741		0271	0542	0814	1085	1356
	,00271,2		2441	2170	1898	1627	
$\bar{3}$.13	$\bar{1}$,56012		0272	0543	0815	1086	1358
	,00271,6		2444	2173	1901	1630	
$\bar{3}$.14	$\bar{1}$,56284		0272	0544	0816	1088	1360
	,00272,0		2448	2176	1904	1632	
$\bar{3}$.15	$\bar{1}$,56556		0273	0545	0818	1090	1363
	,00272,5		2453	2180	1908	1635	
$\bar{3}$.16	$\bar{1}$,56828		0273	0546	0819	1092	1365
	,00272,9		2456	2183	1910	1637	
$\bar{3}$.17	$\bar{1}$,57101		0273	0547	0820	1093	1367
	,00273,3		2460	2186	1913	1640	
$\bar{3}$.18	$\bar{1}$,57375		0274	0548	0821	1095	1369
	,00273,8		2464	2190	1916	1643	
$\bar{3}$.19	$\bar{1}$,57648		0274	0548	0823	1097	1371
	,00274,2		2468	2194	1919	1645	
3.20	$\bar{1}$,57923		0275	0549	0824	1099	1374
	,00274,7		2472	2198	1923	1648	
$\bar{3}$.21	$\bar{1}$,58197		0275	0550	0825	1100	1376
	,00275,1		2476	2201	1926	1651	
$\bar{3}$.22	$\bar{1}$,58472		0276	0551	0827	1102	1378
	,00275,6		2480	2205	1929	1654	
$\bar{3}$.23	$\bar{1}$,58748		0276	0552	0828	1104	1380
	,00276,0		2484	2208	1932	1656	
$\bar{3}$.24	$\bar{1}$,59024		0277	0553	0830	1106	1383
	,00276,5		2489	2212	1936	1659	

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{3}$.25	$\bar{1}$,59300	,00	0277	0554	0831	1108	1385
	,00276,9		2492	2215	1938	1661	
$\bar{3}$.26	$\bar{1}$,59577		0277	0555	0832	1110	1387
	,00277,4		2497	2219	1942	1664	
$\bar{3}$.27	$\bar{1}$,59855		0278	0556	0834	1112	1390
	,00277,9		2491	2223	1945	1667	
$\bar{3}$.28	$\bar{1}$,60133		0278	0557	0835	1114	1392
	,00278,4		2507	2227	1949	1670	
$\bar{3}$.29	$\bar{1}$,60411		0279	0558	0836	1115	1394
	,00278,8		2509	2230	1952	1673	
$\bar{3}$.30	$\bar{1}$,60690		0279	0559	0838	1117	1397
	,00279,3		2514	2234	1955	1676	
$\bar{3}$.31	$\bar{1}$,60969		0280	0560	0839	1119	1399
	,00279,8		2518	2238	1959	1679	
$\bar{3}$.32	$\bar{1}$,61249		0280	0560	0841	1121	1401
	,00280,2		2522	2242	1961	1681	
$\bar{3}$.33	$\bar{1}$,61529		0281	0562	0842	1123	1404
	,00280,8		2527	2244	1966	1685	
$\bar{3}$.34	$\bar{1}$,61810		0281	0563	0844	1125	1407
	,00281,3		2532	2250	1969	1688	
$\bar{3}$.35	$\bar{1}$,62091		0282	0564	0845	1127	1409
	,00281,8		2536	2254	1973	1691	
$\bar{3}$.36	$\bar{1}$,62373		0282	0564	0847	1129	1411
	,00282,2		2540	2258	1975	1693	
$\bar{3}$.37	$\bar{1}$,62655		0283	0566	0848	1131	1414
	,00282,8		2545	2262	1979	1697	
$\bar{3}$.38	$\bar{1}$,62938		0283	0567	0850	1133	1417
	,00283,3		2550	2266	1983	1700	
$\bar{3}$.39	$\bar{1}$,63221		0284	0568	0851	1135	1419
	,00283,8		2554	2270	1987	1703	
$\bar{3}$.40	$\bar{1}$,63505		0284	0569	0853	1137	1422
	,00284,3		2559	2274	1990	1706	
$\bar{3}$.41	$\bar{1}$,63789		0285	0570	0854	1139	1424
	,00284,8		2561	2278	1994	1709	
$\bar{3}$.42	$\bar{1}$,64074		0285	0571	0856	1141	1427
	,00285,3		2568	2282	1997	1712	
$\bar{3}$.43	$\bar{1}$,64359		0286	0572	0857	1143	1429
	,00285,8		2572	2286	2001	1715	
$\bar{3}$.44	$\bar{1}$,64645		0286	0573	0859	1145	1432
	,00286,3		2577	2290	2004	1718	
$\bar{3}$.45	$\bar{1}$,64931		0287	0574	0861	1148	1435
	,00286,9		2582	2295	2008	1721	
$\bar{3}$.46	$\bar{1}$,65218		0287	0575	0862	1150	1437
	,00287,4		2587	2299	2012	1724	
$\bar{3}$.47	$\bar{1}$,65506		0288	0576	0864	1152	1440
	,00288,0		2592	2304	2016	1728	
$\bar{3}$.48	$\bar{1}$,65794		0289	0577	0866	1154	1443
	,00288,5		2597	2308	2020	1731	
$\bar{3}$.49	$\bar{1}$,66082		0289	0578	0867	1156	1445
	,00289,0		2601	2312	2023	1734	

General Table III. $\lambda\left(a^s\right), \lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$.

$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5	$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{3}.50$	$\bar{1},66371$	,00	0290	0579	0869	1158	1448	$\bar{3}.75$	$\bar{1},73787$	,00	0305	0609	0914	1219	1524
	,00289,6		2606	2317	2027	1738			,00304,7		2742	2438	2133	1828	
$\bar{3}.51$	$\bar{1},66661$		0290	0580	0870	1160	1451	$\bar{3}.76$	$\bar{1},74091$		0305	0611	0916	1221	1527
	,00290,1		2611	2321	2031	1741			,00305,3		2748	2442	2137	1832	
$\bar{3}.52$	$\bar{1},66951$		0291	0581	0872	1163	1454	$\bar{3}.77$	$\bar{1},74393$		0306	0612	0918	1224	1530
	,00290,7		2616	2326	2035	1744			,00306,0		2754	2448	2142	1836	
$\bar{3}.53$	$\bar{1},67242$		0291	0583	0874	1166	1457	$\bar{3}.78$	$\bar{1},74702$		0307	0613	0920	1226	1533
	,00291,4		2623	2331	2040	1748			,00306,6		2759	2453	2146	1840	
$\bar{3}.54$	$\bar{1},67533$		0292	0584	0875	1167	1459	$\bar{3}.79$	$\bar{1},75009$		0307	0615	0922	1230	1537
	,00291,8		2626	2334	2043	1751			,00307,4		2767	2459	2152	1844	
$\bar{3}.55$	$\bar{1},67825$		0292	0585	0877	1170	1462	$\bar{3}.80$	$\bar{1},75316$		0308	0616	0924	1232	1540
	,00292,4		2632	2339	2047	1754			,00308,0		2772	2464	2156	1848	
$\bar{3}.56$	$\bar{1},68117$		0293	0586	0879	1172	1465	$\bar{3}.81$	$\bar{1},75624$		0309	0618	0926	1235	1544
	,00292,9		2636	2343	2050	1757			,00308,8		2779	2470	2162	1853	
$\bar{3}.57$	$\bar{1},68410$		0294	0587	0881	1175	1469	$\bar{3}.82$	$\bar{1},75933$		0309	0609	0928	1237	1547
	,00293,7		2643	2350	2056	1762			,00309,3		2784	2474	2165	1856	
$\bar{3}.58$	$\bar{1},68704$		0294	0588	0882	1176	1471	$\bar{3}.83$	$\bar{1},76243$		0310	0620	0930	1240	1551
	,00294,1		2647	2333	2059	1765			,00310,1		2771	2481	2171	1861	
$\bar{3}.59$	$\bar{1},68998$		0295	0589	0884	1179	1474	$\bar{3}.84$	$\bar{1},76553$		0311	0622	0932	1243	1554
	,00294,7		2652	2358	2063	1768			,00310,8		2797	2486	2176	1865	
$\bar{3}.60$	$\bar{1},69293$		0295	0591	0886	1181	1477	$\bar{3}.85$	$\bar{1},76863$		0311	0623	0934	1246	1557
	,00295,3		2658	2362	2067	1772			,00311,4		2803	2491	2180	1868	
$\bar{3}.61$	$\bar{1},69588$		0296	0592	0888	1184	1480	$\bar{3}.86$	$\bar{1},77175$		0312	0624	0937	1249	1561
	,00295,9		2663	2367	2071	1775			,00312,2		2810	2498	2185	1873	
$\bar{3}.62$	$\bar{1},69884$		0297	0593	0890	1186	1483	$\bar{3}.87$	$\bar{1},77487$		0313	0626	0939	1252	1565
	,00296,5		2669	2372	2076	1779			,00313,0		2817	2504	2191	1878	
$\bar{3}.63$	$\bar{1},70180$		0297	0594	0891	1188	1486	$\bar{3}.88$	$\bar{1},77800$		0314	0627	0941	1254	1568
	,00297,1		2674	2377	2080	1783			,00313,6		2822	2509	2195	1882	
$\bar{3}.64$	$\bar{1},70477$		0298	0595	0893	1191	1489	$\bar{3}.89$	$\bar{1},78113$		0314	0629	0943	1257	1572
	,00297,7		2679	2382	2084	1786			,00314,3		2829	2514	2200	1886	
$\bar{3}.65$	$\bar{1},70775$		0298	0597	0895	1194	1492	$\bar{3}.90$	$\bar{1},78428$		0315	0630	0945	1260	1575
	,00298,4		2686	2387	2089	1790			,00315,0		2835	2520	2205	1890	
$\bar{3}.66$	$\bar{1},71074$		0299	0598	0896	1195	1494	$\bar{3}.91$	$\bar{1},78743$		0316	0632	0947	1263	1579
	,0029,88		2689	2390	2092	1793			,00315,8		2842	2526	2211	1895	
$\bar{3}.67$	$\bar{1},71372$		0300	0599	0899	1198	1498	$\bar{3}.92$	$\bar{1},79059$		0316	0633	0949	1266	1582
	,00299,6		2696	2397	2097	1798			,00316,4		2848	2531	2215	1898	
$\bar{3}.68$	$\bar{1},71672$		0300	0600	0901	1201	1501	$\bar{3}.93$	$\bar{1},79375$		0317	0635	0952	1269	1587
	,00300,2		2702	2402	2101	1801			,00317,3		2856	2538	2221	1904	
$\bar{3}.69$	$\bar{1},71972$		0301	0602	0902	1203	1504	$\bar{3}.94$	$\bar{1},79692$		0318	0636	0954	1272	1590
	,00300,8		2707	2406	2106	1805			,00318,0		2862	2544	2226	1908	
$\bar{3}.70$	$\bar{1},72273$		0301	0603	0904	1206	1507	$\bar{3}.95$	$\bar{1},80010$		0319	0637	0956	1275	1594
	,00301,4		2713	2411	2110	1808			,00318,7		2868	2550	2231	1912	
$\bar{3}.71$	$\bar{1},72574$		0302	0604	0906	1208	1510	$\bar{3}.96$	$\bar{1},80329$		0320	0639	0959	1278	1598
	,00302,0		2718	2416	2114	1812			,00319,5		2876	2556	2237	1917	
$\bar{3}.72$	$\bar{1},72876$		0303	0605	0908	1211	1514	$\bar{3}.97$	$\bar{1},80648$		0320	0641	0961	1281	1602
	,00302,7		2724	2422	2119	1816			,00320,3		2883	2562	2242	1922	
$\bar{3}.73$	$\bar{1},73179$		0303	0607	0910	1214	1517	$\bar{3}.98$	$\bar{1},80969$		0321	0642	0963	1284	1605
	,00303,4		2731	2427	2124	1820			,00321,0		2889	2568	2247	1926	
$\bar{3}.74$	$\bar{1},73483$		0304	0608	0912	1216	1520	$\bar{3}.99$	$\bar{1},81290$		0322	0644	0965	1287	1609
	,00304,0		2736	2432	2128	1824			,00321,8		2896	2574	2253	1931	

General Table III. $\lambda\ (a^s),\ \lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$.

$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}.00$	$\bar{1},81612$	,00	0323	0645	0968	1290	1613
	,00322,5		2903	2580	2258	1935	
$\bar{2}.01$	$\bar{1},81934$		0323	0647	0970	1294	1617
	,00323,4		2911	2587	2264	1940	
$\bar{2}.02$	$\bar{1},82257$		0324	0648	0973	1297	1621
	,00324,2		2918	2594	2269	1945	
$\bar{2}.03$	$\bar{1},82582$		0325	0650	0975	1300	1625
	,00324,9		2924	2599	2274	1949	
$\bar{2}.04$	$\bar{1},82907$		0326	0652	0977	1303	1629
	,00325,8		2932	2606	2281	1955	
$\bar{2}.05$	$\bar{1},83232$		0327	0653	0980	1306	1633
	,00326,5		2939	2612	2286	1959	
$\bar{2}.06$	$\bar{1},83559$		0327	0655	0982	1309	1637
	,00327,3		2946	2618	2291	1964	
2.07	$\bar{1},83886$		0328	0656	0985	1313	1641
	,00328,2		2954	2626	2297	1969	
$\bar{2}.08$	$\bar{1},84214$		0329	0658	0987	1316	1645
	,00329,0		2961	2632	2303	1974	
$\bar{2}.09$	$\bar{1},84543$		0330	0660	0989	1319	1649
	,00329,8		2968	2638	2309	1979	
$\bar{2}.10$	$\bar{1},84873$		0331	0661	0992	1322	1653
	,00330,6		2975	2645	2314	1984	
$\bar{2}.11$	$\bar{1},85204$		0332	0663	0995	1326	1658
	,00331,5		2983	2652	2320	1989	
$\bar{2}.12$	$\bar{1},85553$		0332	0665	0997	1330	1662
	,00332,4		2992	2659	2327	1994	
$\bar{2}.13$	$\bar{1},85868$		0333	0666	1000	1333	1666
	,00333,2		2999	2666	2332	1999	
$\bar{2}.14$	$\bar{1},86201$		0334	0668	1002	1336	1670
	,00334,0		3006	2672	2338	2004	
$\bar{2}.15$	$\bar{1},86535$		0335	0670	1005	1340	1675
	,00334,9		3014	2679	2344	2009	
$\bar{2}.16$	$\bar{1},86870$		0336	0671	1007	1343	1679
	,00335,7		3021	2686	2350	2014	
$\bar{2}.17$	$\bar{1},87205$		0337	0673	1010	1346	1683
	,00336,6		3049	2693	2356	2020	
$\bar{2}.18$	$\bar{1},87542$		0338	0675	1013	1350	1688
	,00337,5		3038	2700	2363	2025	
$\bar{2}.19$	$\bar{1},87880$		0338	0677	1015	1354	1692
	,00338,4		3046	2707	2369	2030	
$\bar{2}.20$	$\bar{1},88218$		0339	0679	1018	1357	1697
	,00339,3		3054	2714	2375	2036	
$\bar{2}.21$	$\bar{1},88557$		0340	0680	1021	1361	1701
	,00340,2		3062	2722	2381	2041	
$\bar{2}.22$	$\bar{1},88897$		0341	0682	1023	1364	1705
	,00341,0		3069	2728	2387	2046	
$\bar{2}.23$	$\bar{1},89238$		0342	0684	1026	1368	1711
	,00342,1		3079	2737	2395	2053	
$\bar{2}.24$	$\bar{1},89581$		0343	0686	1028	1371	1714
	,00342,8		3085	2742	2400	2057	

$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}.25$	$\bar{1},89923$	,00	0344	0688	1031	1375	1719
	,00343,8		3094	2750	2407	2063	
$\bar{2}.26$	$\bar{1},90267$		0345	0689	1034	1379	1724
	,00344,7		3102	2758	2413	2068	
$\bar{2}.27$	$\bar{1},90612$		0346	0691	1037	1383	1729
	,00345,7		3111	2766	2420	2074	
$\bar{2}.28$	$\bar{1},90958$		0347	0693	1040	1386	1733
	,00346,6		3119	2773	2426	2080	
$\bar{2}.29$	$\bar{1},91304$		0348	0695	1043	1390	1738
	,00347,6		3128	2781	2433	2086	
$\bar{2}.30$	$\bar{1},91652$		0349	0697	1046	1394	1743
	,00348,5		3137	2788	2440	2091	
$\bar{2}.31$	$\bar{1},92000$		0349	0699	1048	1397	1747
	,00349,3		3144	2794	2445	2096	
$\bar{2}.32$	$\bar{1},92349$		0351	0701	1052	1403	1754
	,00350,7		3156	2806	2455	2104	
$\bar{2}.33$	$\bar{1},92700$		0351	0703	1054	1406	1757
	,00351,4		3163	2811	2460	2108	
$\bar{2}.34$	$\bar{1},93052$		0352	0705	1057	1410	1762
	,00352,4		3172	2819	2467	2114	
$\bar{2}.35$	$\bar{1},93404$		0353	0707	1060	1413	1767
	,00353,3		3180	2826	2473	2120	
$\bar{2}.36$	$\bar{1},93757$		0354	0709	1063	1417	1771
	,00354,3		3189	2834	2480	2126	
$\bar{2}.37$	$\bar{1},94112$		0355	0711	1066	1422	1777
	,00355,4		3199	2843	2488	2132	
$\bar{2}.38$	$\bar{1},94467$		0356	0713	1069	1426	1782
	,00356,4		3208	2851	2495	2138	
2.39	$\bar{1},94823$		0357	0715	1072	1429	1787
	,00357,3		3216	2858	2501	2144	
$\bar{2}.40$	$\bar{1},95181$		0358	0717	1075	1434	1792
	,00358,4		3226	2867	2509	2150	
$\bar{2}.41$	$\bar{1},95539$		0359	0719	1078	1438	1797
	,00359,4		3235	2875	2516	2156	
$\bar{2}.42$	$\bar{1},95898$		0360	0721	1081	1442	1802
	,00360,4		3244	2883	2523	2162	
$\bar{2}.43$	$\bar{1},96259$		0361	0723	1084	1446	1807
	,00361,4		3253	2891	2530	2168	
$\bar{2}.44$	$\bar{1},96620$		0362	0725	1087	1450	1812
	,00362,4		3262	2899	2537	2174	
$\bar{2}.45$	$\bar{1},96983$		0363	0727	1090	1454	1817
	,00363,4		3271	2907	2544	2180	
$\bar{2}.46$	$\bar{1},97346$		0365	0729	1094	1458	1823
	,00364,6		3281	2917	2552	2188	
$\bar{2}.47$	$\bar{1},97711$		0366	0731	1097	1462	1828
	,00365,6		3290	2925	2559	2194	
$\bar{2}.48$	$\bar{1},98076$		0367	0733	1100	1467	1834
	,00366,7		3300	2934	2567	2200	
$\bar{2}.49$	$\bar{1},98443$		0368	0735	1103	1471	1839
	,00367,8		3310	2942	2575	2207	

General Table III. $\lambda(a^s)$, $\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$.

$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}.50$	$\bar{1}$,98811	,00	0369	0738	1106	1475	1844
	,00368,8		3319	2950	2582	2213	
$\bar{2}.51$	$\bar{1}$,99179		0370	0740	1109	1480	1850
	,00369,9		3329	2959	2589	2219	
$\bar{2}.52$	$\bar{1}$,99549		0371	0742	1113	1484	1855
	,00371,0		3339	2968	2597	2226	
$\bar{2}.53$	$\bar{1}$,99920		0372	0744	1116	1488	1861
	,00372,1		3349	2977	2605	2233	
$\bar{2}.54$	,00293		0373	0747	1120	1493	1867
	,00373,3		3360	2986	2613	2240	
$\bar{2}.55$	,00666		0374	0749	1123	1497	1872
	,00374,3		3369	2994	2620	2246	
$\bar{2}.56$	,01040		0376	0751	1127	1502	1878
	,00375,5		3380	3004	2629	2253	
$\bar{2}.57$	,01416		0376	0753	1129	1506	1882
	,00376,4		3388	3011	2635	2258	
$\bar{2}.58$	,00792		0378	0756	1134	1512	1890
	,00377,9		3401	3023	2645	2267	
$\bar{2}.59$	,02170		0379	0758	1136	1515	1894
	,00378,3		3409	3030	2652	2273	
$\bar{2}.60$	,02549		0380	0760	1140	1520	1900
	,00380,0		3420	3040	2660	2280	
$\bar{2}.61$	,02929		0381	0762	1144	1525	1906
	,00381,2		3431	3050	2668	2287	
$\bar{2}.62$	,03310		0382	0765	1147	1530	1912
	,00382,4		3442	3059	2677	2294	
$\bar{2}.63$	,03692		0383	0767	1150	1534	1917
	,00383,4		3451	3067	2684	2300	
2.64	,04076		0385	0769	1154	1539	1924
	,00384,7		3462	3078	2693	2308	
$\bar{2}.65$	,04460		0386	0772	1157	1543	1929
	,00385,8		3472	3086	2701	2315	
$\bar{2}.66$	,04846		0387	0774	1161	1548	1936
	,00387,1		3484	3097	2710	2323	
2.67	,05233		0388	0776	1165	1553	1941
	,00388,2		3494	3106	2717	2329	
$\bar{2}.68$	,05621		0389	0779	1168	1558	1947
	,00389,4		3505	3115	2726	2336	
$\bar{2}.69$	,06010		0391	0781	1172	1562	1953
	,00390,6		3515	3125	2734	2344	
$\bar{2}.70$	,06401		0392	0784	1176	1568	1960
	,00391,9		3527	3135	2743	2351	
$\bar{2}.71$	,06793		0393	0786	1179	1572	1965
	,00393,0		3537	3144	2751	2358	
$\bar{2}.72$	,07186		0394	0789	1183	1577	1972
	,00394,3		3549	3154	2760	2366	
$\bar{2}.73$	,07581		0396	0791	1187	1582	1978
	00395,5		3560	3164	2769	2373	
$\bar{2}.74$	,07976		0397	0794	1190	1587	1984
	,00396,8		3571	3174	2778	2381	

$\lambda(a^s)$	$\lambda\left(\frac{1-a^s}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{2}.75$	,08373	,00	0398	0796	1194	1592	1990
	,00397,9		3581	3183	2785	2387	
$\bar{2}.76$	,08771		0399	0799	1198	1598	1997
	,00399,4		3595	3195	2796	2396	
$\bar{2}.77$	,09170		0401	0801	1202	1602	2003
	,00400,6		3605	3205	2804	2404	
$\bar{2}.78$	,09571		0402	0803	1205	1607	2009
	,00401,7		3615	3214	2812	2410	
$\bar{2}.79$	,09972		0403	0806	1209	1612	2016
	,00403,1		3628	3225	2822	2419	
$\bar{2}.80$	,10376		0404	0809	1213	1618	2022
	,00404,4		3640	3235	2831	2426	
$\bar{2}.81$	,10780		0406	0811	1217	1623	2029
	,00405,7		3651	3246	2840	2434	
$\bar{2}.82$	,11186		0407	0814	1221	1628	2035
	,00407,0		3663	3256	2849	2442	
$\bar{2}.83$	,11593		0408	0817	1225	1633	2042
	,00408,3		3675	3266	2858	2450	
$\bar{2}.84$	,12001		0410	0819	1229	1638	2048
	,00409,5		3686	3276	2867	2457	
$\bar{2}.85$	,12410		0411	0822	1233	1644	2055
	,00410,9		3698	3287	2876	2465	
$\bar{2}.86$	,12821		0412	0824	1237	1649	2061
	,00412,2		3710	3298	2885	2473	
$\bar{2}.87$	,13234		0414	0827	1241	1654	2068
	,00413,6		3722	3309	2895	2482	
$\bar{2}.88$	,13647		0415	0830	1245	1660	2075
	,00414,9		3734	3319	2904	2489	
$\bar{2}.89$	,14062		0416	0833	1249	1665	2082
	,00416,3		3747	3330	2914	2498	
$\bar{2}.90$	,14478		0418	0835	1253	1670	2088
	,00417,6		3758	3341	2923	2506	
$\bar{2}.91$	,14896		0419	0838	1257	1676	2095
	,00419,0		3771	3352	2933	2514	
$\bar{2}.92$	,15315		0420	0841	1261	1682	2102
	,00420,4		3784	3363	2943	2522	
$\bar{2}.93$	,15735		0422	0843	1265	1687	2109
	,00421,7		3795	3344	2952	2530	
$\bar{2}.94$	,16157		0423	0846	1269	1692	2116
	,00423,1		3808	3385	2962	2539	
$\bar{2}.95$	,16580		0425	0849	1274	1698	2123
	,00424,6		3821	3397	2972	2548	
$\bar{2}.96$	,17005		0426	0852	1277	1703	2129
	,00425,8		3832	3406	2981	2555	
$\bar{2}.97$	,17430		0427	0855	1282	1719	2137
	,00427,3		3846	3418	2991	2564	
$\bar{2}.98$	,17858		0429	0857	1286	1715	2144
	,00428,7		3858	3430	3001	2572	
$\bar{2}.99$	,18286		0430	0860	1290	1720	2151
	,00430,1		3871	3441	3011	2581	

General Table III. $\lambda(a^5)$, $\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$.

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.00$	,18717	,00	0432	0863	1295	1726	2158
	,00431,6		3884	3453	3021	2590	
$\bar{1}.01$	,19148		0433	0866	1299	1732	2165
	,00433,0		3897	3464	3031	2598	
$\bar{1}.02$	,19581		0434	0869	1304	1738	2175
	,00434,5		3911	3476	3042	2607	
$\bar{1}.03$	,20016		0435	0871	1306	1742	2177
	,00435,4		3919	3483	3048	2612	
$\bar{1}.04$	,20451		0438	0875	1313	1750	2188
	,00437,6		3938	3401	3063	2626	
$\bar{1}.05$	,20889		0439	0877	1316	1755	2194
	,00438,7		3948	3510	3071	2632	
$\bar{1}.06$	,21328		0440	0880	1321	1761	2201
	,00440,2		3962	3522	3081	2641	
$\bar{1}.07$	,21768		0442	0883	1325	1767	2209
	,00441,7		3975	3534	3092	2650	
$\bar{1}.08$	,22209		0443	0886	1330	1773	2216
	,00443,2		3989	3546	3102	2659	
$\bar{1}.09$	,22653		0445	0889	1334	1779	2224
	,00444,7		4002	3558	3113	2668	
$\bar{1}.10$	,23097		0446	0892	1338	1784	2231
	,00446,1		4015	3569	3123	2677	
$\bar{1}.11$	,23543		0448	0895	1343	1791	2240
	,00447,7		4029	3582	3134	2686	
$\bar{1}.12$	,23991		0449	0898	1348	1797	2246
	,00449,2		4043	3594	3144	2695	
$\bar{1}.13$	,24440		0451	0992	1353	1804	2255
	,00450,9		4058	3607	3156	2705	
$\bar{1}.14$	,24891		0452	0904	1356	1808	2260
	,00452,0		4068	3616	3164	2712	
$\bar{1}.15$	,25343		0454	0907	1361	1815	2269
	,00453,7		4083	3630	3176	2722	
$\bar{1}.16$	,25797		0455	09 1	1366	1821	2277
	,00455,3		4098	3642	3187	2732	
$\bar{1}.17$	,26252		0457	0914	1370	1827	2284
	,00456,8		4111	3654	3198	2741	
$\bar{1}.18$	,26709		0458	0917	1375	1833	2292
	,00458,3		4125	3666	3208	2750	
$\bar{1}.19$	,27167		0460	0920	1380	1840	2300
	,00459,9		4139	3679	3219	2759	
$\bar{1}.20$	,27627		0461	0923	1384	1846	2307
	,00461,4		4153	3691	3230	2768	
$\bar{1}.21$	,28089		0463	0926	1389	1852	2315
	,00463,0		4167	3704	3241	2778	
$\bar{1}.22$	,28551		0465	0929	1394	1858	2323
	,00464,6		4181	3717	3252	2788	
$\bar{1}.23$	,29016		0466	0932	1398	1864	2331
	,00466,1		4194	3729	3263	2797	
$\bar{1}.24$	,29482		0468	0935	1403	1871	2339
	,00467,7		4209	3742	3274	2806	

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$		1 9	2 8	3 7	4 6	5
$\bar{1}.25$	,29950	,00	0469	0939	1408	1877	2347
	,00469,3		4224	3754	3285	2816	
$\bar{1}.26$	,30419		0471	0942	1413	1884	2355
	,00470,9		4238	3767	3206	2825	
$\bar{1}.27$	,30890		0473	0945	1418	1890	2363
	,00472,5		4253	3780	3308	2835	
$\bar{1}.28$	,31363		0474	0948	1422	1896	2371
	,00474,1		4267	3793	3319	2845	
$\bar{1}.29$	,31837		0476	0951	1427	1903	2379
	,00475,7		4281	3806	3330	2854	
$\bar{1}.30$	,32312		0477	0955	1432	1909	2387
	,00477,3		4296	3818	3341	2864	
$\bar{1}.31$	,32790		0479	0958	1437	1916	2395
	,00479,0		4310	3831	3352	2873	
$\bar{1}.32$	,33269		0481	0961	1442	1922	2403
	,00480,6		4325	3845	3364	2884	
$\bar{1}.33$	,33749		0482	0964	1447	1929	2411
	,00482,2		4340	3858	3375	2893	
$\bar{1}.34$	,34232		0484	0968	1452	1936	2420
	,00483,9		4355	3871	3387	2903	
$\bar{1}.35$	,34715		0486	0971	1457	1942	2428
	,00485,5		4370	3884	3399	2913	
$\bar{1}.36$	,35201		0487	0974	1462	1949	2436
	,00487,2		4385	3898	3410	2923	
$\bar{1}.37$	,35688		0489	0978	1466	1955	2444
	,00488,8		4399	3910	3422	2933	
$\bar{1}.38$	,36177		0490	0981	1471	1962	2452
	,00490,4		4414	3923	3433	2942	
$\bar{1}.39$	,36676		0492	0984	1476	1968	2461
	,00492,1		4429	3937	3445	2953	
$\bar{1}.40$	,37159		0494	0988	1481	1975	2469
	,00493,8		4444	3950	3457	2963	
$\bar{1}.41$	,37653		0496	0991	1487	1982	2477
	,00495,5		4460	3964	3469	2973	
$\bar{1}.42$	,38149		0497	0994	1492	1989	2486
	,00497,2		4475	3988	3480	2983	
$\bar{1}.43$	,38646		0499	0998	1497	1996	2495
	,00498,9		4490	3991	3492	2993	
$\bar{1}.44$	,39145		0501	1001	1502	2002	2503
	,00500,6		4505	4005	3504	3004	
$\bar{1}.45$	,39645		0502	1004	1507	2009	2511
	,00502,2		4520	4018	3515	3013	
$\bar{1}.46$	,40148		0504	1008	1512	2016	2520
	,00594,0		4536	4032	3528	3024	
$\bar{1}.47$	,40652		0506	1011	1517	2023	2529
	,00505,7		4551	4046	3540	3034	
$\bar{1}.48$	,41157		0507	1015	1522	2030	2537
	,00507,4		4567	4059	3552	3044	
$\bar{1}.49$	,41665		0509	1018	1527	2036	2546
	,00509,0		4582	4073	3564	3055	

General Table III. $\lambda(a^5)$, $\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$.

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$		1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{1}.50$	,42174	,00	0511	1022	1532	2043	2554
	,00510,8		4597	4086	3576	3065	
$\bar{1}.51$	,42684		0513	1025	1538	2050	2563
	,00512,5		4613	4100	3588	3075	
$\bar{1}.52$	,43197		0514	1028	1543	2057	2571
	,00514,2		4628	4114	3599	3085	
$\bar{1}.53$	,43711		0516	1032	1548	2064	2581
	,00516,1		4645	4129	3613	3097	
$\bar{1}.54$	,44227		0518	1036	1553	2071	2589
	,00517,8		4660	4142	3625	3107	
$\bar{1}.55$	,44745		0520	1039	1559	2078	2598
	,00519,5		4676	4156	3637	3117	
$\bar{1}.56$	,45264		0521	1042	1564	2085	2606
	,00521,2		4691	4170	3648	3127	
$\bar{1}.57$	,45786		0523	1046	1569	2092	2615
	,00523,0		4707	4184	3661	3138	
$\bar{1}.58$	,46309		0525	1049	1574	2099	2624
	,00524,7		4722	4198	3673	3148	
$\bar{1}.59$	,46833		0527	1053	1580	2106	2633
	,00526,5		4739	4212	3686	3159	
$\bar{1}.60$	,47360		0528	1057	1585	2113	2642
	,00528,3		4755	4226	3698	3170	
$\bar{1}.61$	,47888		0530	1060	1590	2120	2650
	,00530,0		4770	4240	3710	3180	
$\bar{1}.62$	,48418		0532	1064	1595	2127	2659
	,00531,8		4786	4254	3723	3191	
$\bar{1}.63$	,48950		05[illegible]4	1067	1601	2134	2668
	,00533,6		4802	4269	3735	3202	
$\bar{1}.64$	,49484		0535	1071	1606	2141	2677
	,00535,3		4818	4282	3747	3212	
$\bar{1}.65$	,50019		0537	1074	1611	2148	2688
	,00537,1		4834	4297	3760	3223	
$\bar{1}.66$	,50556		0539	1078	1617	2156	2695
	,00538,9		4850	4311	3772	3233	
$\bar{1}.67$	,51095		0541	1081	1622	2163	2704
	,00540,7		4866	4326	3785	3244	
$\bar{1}.68$	,51636		0543	1085	1628	2170	2713
	,00542,5		4883	4340	3798	3255	
$\bar{1}.69$	,52178		0544	1089	1633	2177	2722
	,00544,3		4899	4354	3810	3266	
$\bar{1}.70$	,52722		0546	1092	1638	2184	2731
	,00546,1		4915	4369	3823	3277	
$\bar{1}.71$	,53269		0548	1096	1643	2191	2739
	,00547,8		4920	4382	3835	3287	
$\bar{1}.72$	,53816		0550	1099	1649	2199	2749
	,00549,7		4947	4398	3848	3298	
$\bar{1}.73$	,54366		0552	1103	1655	2206	2758
	,00551,5		4964	4412	3861	3309	
$\bar{1}.74$	,54918		0553	1107	1660	2213	2767
	,00553,3		4980	4426	3873	3320	

$\lambda(a^5)$	$\lambda\left(\frac{1-a^5}{a^{-1}-1}\right)$	$\lambda(a^5)$	1 / 9	2 / 8	3 / 7	4 / 6	5
$\bar{1}.75$	,55471	,00	0555	1110	1666	2221	2776
	,00555,2		4997	4442	3886	3331	
$\bar{1}.76$	,56026		0557	1114	1671	2228	2785
	,00556,9		5012	4455	3898	3341	
$\bar{1}.77$	,56583		0559	1117	1676	2234	2793
	,00558,6		5027	4469	3910	3352	
$\bar{1}.78$	,57142		0561	1121	1682	2243	2804
	,00560,7		5046	4486	3925	3364	
$\bar{1}.79$	,57702		0562	1125	1687	2250	2812
	,00562,4		5062	4499	3937	3374	
$\bar{1}.80$	,58265		0564	1128	1693	2257	2821
	,00564,2		5078	4514	3949	3385	
$\bar{1}.81$	,58829		0566	1132	1698	2264	2830
	,00565,9		5093	4527	3961	3395	
$\bar{1}.82$	,59395		0568	1136	1703	2271	2839
	,00567,8		5110	4542	3975	3407	
$\bar{1}.83$	,59963		0570	1139	1709	2279	2849
	,00569,7		5127	4558	3988	3418	
$\bar{1}.84$	,60532		0572	1143	1715	2286	2858
	,00571,5		5144	4572	4001	3429	
$\bar{1}.85$	,61104		0573	1147	1720	2293	2867
	,00573,3		5160	4586	4013	3440	
$\bar{1}.86$	,61677		0575	1150	1725	2300	2876
	,00575,1		4176	4601	4026	3451	
$\bar{1}.87$	,62252		0577	1154	1731	2308	2885
	,00577,0		5193	4616	4039	3462	
$\bar{1}.88$	,62829		0579	1158	1736	2315	2894
	,00578,8		5210	4630	4052	3473	
$\bar{1}.89$	,63408		0581	1162	1742	2323	2904
	,00580,8		5227	4646	4066	3485	
$\bar{1}.90$	,63989		0583	1165	1748	2330	2913
	,00582,5		5243	4660	4078	3495	
$\bar{1}.91$	,64572		0584	1169	1753	2338	2922
	,00584,4		5260	4675	4091	3506	
$\bar{1}.92$	,65156		0586	1172	1759	2345	2931
	,00586,2		5276	4690	4103	3517	
$\bar{1}.93$	,65742		0588	1176	1764	2352	2940
	,00587,9		5291	4713	4115	3527	
$\bar{1}.94$	,66330		0590	1180	1770	2360	2950
	,00590,0		5310	4720	4130	3540	
$\bar{1}.95$	,66920		0592	1183	1775	2367	2959
	,00591,7		5325	4734	4142	3550	
$\bar{1}.96$	,67512		0594	1187	1781	2374	2968
	,00593,5		5342	4748	4155	3561	
$\bar{1}.97$	,68105		0595	1191	1786	2382	2977
	,00595,4		5359	4763	4168	3572	
$\bar{1}.98$	,68701		0597	1195	1791	2389	2987
	,00597,3		5376	4778	4181	3584	
$\bar{1}.99$	,69298						

General Table IV. For the whole of life. $-\lambda(a^{-1}-1)$.

$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$
$\bar{1}.700$	,00206	$\bar{1}.725$	,05372	$\bar{1}.750$	,10886	$\bar{1}.775$	,16826	$\bar{1}.800$	,23292	$\bar{1}.825$	,30431
	,00201		,00213		,00229		,00247		,00271		,00302
$\bar{1}.701$	,00407	$\bar{1}.726$	,05585	$\bar{1}.751$	,11115	$\bar{1}.776$	,17073	$\bar{1}.801$	,23564	$\bar{1}.826$	,30733
	,00201		,00214		,00230		,00248		,00272		,00304
$\bar{1}.702$	,00608	$\bar{1}.727$	,05799	$\bar{1}.752$	,11345	$\bar{1}.777$	,17322	$\bar{1}.802$	,23836	$\bar{1}.827$	,31037
	,00202		,00215		,00230		,00249		,00274		,00305
$\bar{1}.703$	,00810	$\bar{1}.728$	,06014	$\bar{1}.753$	,11575	$\bar{1}.778$	,17571	$\bar{1}.803$	,24110	$\bar{1}.828$	,31342
	,00202		,00215		,00231		,00250		,00275		,00307
$\bar{1}.704$	,01012	$\bar{1}.729$	,06229	$\bar{1}.754$	,11806	$\bar{1}.779$	,17822	$\bar{1}.804$	,24385	$\bar{1}.829$	,31649
	,00203		,00216		,00232		,00251		,00276		,00308
$\bar{1}.705$	,01214	$\bar{1}.730$	,06445	$\bar{1}.755$	,12037	$\bar{1}.780$	,18073	$\bar{1}.805$	,24661	$\bar{1}.830$	,31957
	,00203		,00216		,00233		,00252		,00277		,00309
$\bar{1}.706$	,01418	$\bar{1}.731$	,06661	$\bar{1}.756$	,12270	$\bar{1}.781$	,18325	$\bar{1}.806$	,24938	$\bar{1}.831$	,32266
	,00203		,00217		,00233		,00253		,00278		,00311
$\bar{1}.707$	,01621	$\bar{1}.732$	,06878	$\bar{1}.757$	,12503	$\bar{1}.782$	,18578	$\bar{1}.807$	,25216	$\bar{1}.832$	,32577
	,00204		,00217		,00234		,00254		,00279		,00313
$\bar{1}.708$	,01825	$\bar{1}.733$	,07095	$\bar{1}.758$	,12736	$\bar{1}.783$	,18832	$\bar{1}.808$	,25495	$\bar{1}.833$	,32890
	,00205		,00219		,00235		,00254		,00281		,00314
$\bar{1}.709$	,02030	$\bar{1}.734$	,07314	$\bar{1}.759$	,12971	$\bar{1}.784$	,19086	$\bar{1}.809$	,25776	$\bar{1}.834$	,33204
	,00205		,00218		,00235		,00256		,00281		,00315
$\bar{1}.710$	,02235	$\bar{1}.735$	,07532	$\bar{1}.760$	,13206	$\bar{1}.785$	,19342	$\bar{1}.810$	,26057	$\bar{1}.835$	,33519
	,00205		,00219		,00236		,00257		,00283		,00317
$\bar{1}.711$	,02440	$\bar{1}.736$	,07751	$\bar{1}.761$	,13442	$\bar{1}.786$	,19599	$\bar{1}.811$	,26340	$\bar{1}.836$	,33836
	,00206		,00220		,00237		,00258		,00284		,00319
$\bar{1}.712$	,02646	$\bar{1}.737$	,07971	$\bar{1}.762$	,13679	$\bar{1}.787$	,19856	$\bar{1}.812$	,26624	$\bar{1}.837$	,34155
	,00207		,00221		,00237		,02259		,00285		,00320
$\bar{1}.713$	,02853	$\bar{1}.738$	,08192	$\bar{1}.763$	,13916	$\bar{1}.788$	,20115	$\bar{1}.813$	,26909	$\bar{1}.838$	,34475
	,00207		,00221		,00238		,00259		,00287		,00322
$\bar{1}.714$	,03060	$\bar{1}.739$	,08413	$\bar{1}.764$	,14154	$\bar{1}.789$	,20374	$\bar{1}.814$	,27196	$\bar{1}.839$	,34797
	,00207		,00221		,00239		,00260		,00287		,00324
$\bar{1}.715$	,03267	$\bar{1}.740$	,08634	$\bar{1}.765$	,14393	$\bar{1}.790$	,20634	$\bar{1}.815$	,27483	$\bar{1}.840$	,35121
	,00208		,00223		,00240		,00261		,00289		,00325
$\bar{1}.716$	,03476	$\bar{1}.741$	,08857	$\bar{1}.766$	,14633	$\bar{1}.791$	,20896	$\bar{1}.816$	,27772	$\bar{1}.841$	,35446
	,00208		,00223		,00240		,00262		,00291		,00327
$\bar{1}.717$	,03684	$\bar{1}.742$	,09080	$\bar{1}.767$	,14873	$\bar{1}.792$	,21158	$\bar{1}.817$	,28063	$\bar{1}.842$	,35773
	,00209		,00223		,00241		,00263		,00291		,00329
$\bar{1}.718$	,03893	$\bar{1}.743$	,09303	$\bar{1}.768$	,15114	$\bar{1}.793$	,21421	$\bar{1}.818$	,28354	$\bar{1}.843$	,36102
	,00210		,00224		,00242		,00264		,00293		,00331
$\bar{1}.719$	,04103	$\bar{1}.744$	,09527	$\bar{1}.769$	,15356	$\bar{1}.794$	,21685	$\bar{1}.819$	,28647	$\bar{1}.844$	,36433
	,00210		,00225		,00243		,00265		,00294		,00332
$\bar{1}.720$	,04313	$\bar{1}.745$	,09752	$\bar{1}.770$	,15599	$\bar{1}.795$	,21951	$\bar{1}.820$	,28941	$\bar{1}.845$	,36765
	,00211		,00226		,00244		,00266		,00295		,00334
$\bar{1}.721$	,04524	$\bar{1}.746$	,09978	$\bar{1}.771$	,15843	$\bar{1}.796$	,22217	$\bar{1}.821$	,29236	$\bar{1}.846$	,37099
	,00211		,00226		,00244		,00267		,00297		,00336
$\bar{1}.722$	,04735	$\bar{1}.747$	,10204	$\bar{1}.772$	,16087	$\bar{1}.797$	,22484	$\bar{1}.822$	,29533	$\bar{1}.847$	,37435
	,00212		,00227		,00245		,00268		,00298		,00338
$\bar{1}.723$	,04947	$\bar{1}.748$	,10431	$\bar{1}.773$	,16333	$\bar{1}.798$	,22753	$\bar{1}.823$	,29831	$\bar{1}.848$	,37773
	,00212		,00227		,00246		,00269		,00299		,00339
$\bar{1}.724$	,05159	$\bar{1}.749$	,10658	$\bar{1}.774$	,16579	$\bar{1}.799$	,23022	$\bar{1}.824$	,30130	$\bar{1}.849$	,38112
	,00213		,00228		,00247		,00270		,00301		,00342

General Table IV. For the whole of life. $-\lambda(a^{-1}-1)$.

$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$	$\lambda(a)$	$-\lambda(a^{-1}-1)$
$\bar{1}.850$	,38454	$\bar{1}.875$	,47688	$\bar{1}.900$	,58683	$\bar{1}.925$	,72468	$\bar{1}.950$	,91357	$\bar{1}.975$	1,22728
	,00343		,00401		,00488		,00635		,00929		,01824
$\bar{1}.851$	,38797	$\bar{1}.876$	,48088	$\bar{1}.901$	,59171	$\bar{1}.926$	,73103	$\bar{1}.951$	,92286	$\bar{1}.976$	1,24552
	,00345		,00405		,00493		,00642		,00946		,01899
$\bar{1}.852$	,39142	$\bar{1}.877$	,48493	$\bar{1}.902$	,59664	$\bar{1}.927$	,73745	$\bar{1}.952$	,93232	$\bar{1}.977$	1,26451
	,00348		,00407		,00497		,00650		,00966		,01980
$\bar{1}.853$	,39490	$\bar{1}.878$	,48900	$\bar{1}.903$	,60161	$\bar{1}.928$	,74395	$\bar{1}.953$	,94198	$\bar{1}.978$	1,28431
	,00349		,00410		,00502		,00659		,00984		,02071
$\bar{1}.854$	,39839	$\bar{1}.879$	,49310	$\bar{1}.904$	,60663	$\bar{1}.929$	,75054	$\bar{1}.954$	,95182	$\bar{1}.979$	1,30502
	,00351		,00412		,00507		,00668		,01006		,02170
$\bar{1}.855$	,40190	$\bar{1}.880$	,49722	$\bar{1}.905$	,61170	$\bar{1}.930$	,75722	$\bar{1}.955$	,96188	$\bar{1}.980$	1,32672
	,00353		,00416		,00511		,00676		,01027		,02278
$\bar{1}.856$	,40543	$\bar{1}.881$	,50138	$\bar{1}.906$	,61681	$\bar{1}.931$	,76398	$\bar{1}.956$	,97215	$\bar{1}.981$	1,34950
	,00355		,00419		,00516		,00685		,01049		,02398
$\bar{1}.857$	,40899	$\bar{1}.882$	,50557	$\bar{1}.907$	,62197	$\bar{1}.932$	,77083	$\bar{1}.957$	,98264	$\bar{1}.982$	1,37348
	,00357		,00422		,00521		,00695		,01073		,02583
$\bar{1}.858$	,41256	$\bar{1}.883$	,50979	$\bar{1}.908$	,62718	$\bar{1}.933$	,77778	$\bar{1}.958$	,99337	$\bar{1}.983$	1,39881
	,00360		,00425		,00527		,00704		,01097		,02683
$\bar{1}.859$	,41616	$\bar{1}.884$	,51404	$\bar{1}.909$	,63245	$\bar{1}.934$	,78482	$\bar{1}.959$	1,00434	$\bar{1}.984$	1,42564
	,00362		,00428		,00531		,00715		,01123		,02853
$\bar{1}.860$	,41978	$\bar{1}.885$	,51832	$\bar{1}.910$	,63776	$\bar{1}.935$	,79197	$\bar{1}.960$	1,01557	$\bar{1}.985$	1,45417
	,00364		,00431		,00537		,00724		,01150		,03047
$\bar{1}.861$	,42342	$\bar{1}.886$	,52263	$\bar{1}.911$	,64313	$\bar{1}.936$	,79921	$\bar{1}.961$	1,02707	$\bar{1}.986$	1,48464
	,00366		,00435		,00543		,00735		,01179		,03269
$\bar{1}.862$	,42708	$\bar{1}.887$	,52698	$\bar{1}.912$	,64856	$\bar{1}.937$	,80656	$\bar{1}.962$	1,03886	$\bar{1}.987$	1,51733
	,00368		,00438		,00548		,00746		,01209		,03526
$\bar{1}.863$	,44076	$\bar{1}.888$	,53136	$\bar{1}.913$	,65404	$\bar{1}.938$	,81402	$\bar{1}.963$	1,05095	$\bar{1}.988$	1,55259
	,00371		,00442		,00554		,00758		0,01241		,03829
$\bar{1}.864$	,43447	$\bar{1}.889$	,53578	$\bar{1}.914$	,65958	$\bar{1}.939$	,82160	$\bar{1}.964$	1,06336	$\bar{1}.989$	1,59088
	,00373		,00445		,00559		,00769		,01274		,04189
$\bar{1}.865$	,43820	$\bar{1}.890$	,54023	$\bar{1}.915$	,66517	$\bar{1}.940$	,82929	$\bar{1}.965$	1,07610	$\bar{1}.990$	1,63277
	,00376		,00449		,00566		,00781		,01309		,04626
$\bar{1}.866$	44196	$\bar{1}.891$	,54472	$\bar{1}.916$	,67083	$\bar{1}.941$	,83710	$\bar{1}.966$	1,08919	$\bar{1}.991$	1,67903
	,00378		,00452		,00572		,00793		,01348		,05163
$\bar{1}.867$	,44574	$\bar{1}.892$	,54924	$\bar{1}.917$	,67655	$\bar{1}.942$	,84503	$\bar{1}.967$	1,10267	$\bar{1}.992$	1,73069
	,00380		,00456		,00578		,00807		,01387		,05849
$\bar{1}.868$	,44954	$\bar{1}.893$	,55380	$\bar{1}.918$	,68233	$\bar{1}.943$	,85310	$\bar{1}.968$	1,11654	$\bar{1}.993$	1,78918
	,00383		,00460		,00584		,00820		,01429		,06745
$\bar{1}.869$	,45337	$\bar{1}.894$	,55840	$\bar{1}.919$	,68817	$\bar{1}.944$	,86130	$\bar{1}.969$	1,13083	$\bar{1}.994$	1,85663
	,00385		,00464		,00591		,00833		,01475		,07968
$\bar{1}.870$	,45722	$\bar{1}.895$	,56304	$\bar{1}.920$	,69408	$\bar{1}.945$	,86963	$\bar{1}.970$	1,14558	$\bar{1}.995$	1,93631
	,00388		,00467		,00598		,00848		,01523		,09741
$\bar{1}.871$	,46110	$\bar{1}.896$	,56771	$\bar{1}.921$	,70006	$\bar{1}.946$	,87811	$\bar{1}.971$	1,16081	$\bar{1}.996$	2,03372
	,00390		,00472		,00695		,00863		,01574		,12544
$\bar{1}.872$	,46500	$\bar{1}.897$	,57243	$\bar{1}.922$	,70611	$\bar{1}.947$	,88674	$\bar{1}.972$	1,17655	$\bar{1}.997$	2,15916
	,00393		,00476		,00611		,00878		,01530		,17459
$\bar{1}.873$	,46893	$\bar{1}.898$	,57719	$\bar{1}.923$	,71222	$\bar{1}.948$	,89552	$\bar{1}.973$	1,19285	$\bar{1}.998$	2,33575
	,00396		,00479		,00620		,00894		,01690		,30153
$\bar{1}.874$	,47289	$\bar{1}.899$	,58198	$\bar{1}.924$	,71842	$\bar{1}.949$	,90446	$\bar{1}.974$	1,20975	$\bar{1}.999$	2,63728
	,00399		,00485		,00626		,00911		,01753		

TABLE V.—Logarithms of the accommodated chances of living 10 years, deduced from the value of an annuity for 10 years, at 5 per cent. from the actual tables of mortality, and considered equal to a geometrical series of ten terms, of which the common ratio is the same as the first term, and the tenth term the accommodated chance; and to find the accommodated chance for 5, 7 years, &c. without a table calculated for the purpose, it may be considered sufficient to multiply by ,5 ; ,7, &c. the accommodated ratio in this table when extreme accuracy be not required.

Age.	Carlisle.	Deparcieux.	Northampton.	Age.	Carlisle.	Deparcieux.	Northampton.
0	$\bar{1}$,6892	—	—	52	$\bar{1}$,9172	$\bar{1}$,9006	$\bar{1}$,8523
1	$\bar{1}$,6763	—	$\bar{1}$,7044	53	$\bar{1}$,9098	$\bar{1}$,8957	$\bar{1}$,8471
2	$\bar{1}$,8699	—	$\bar{1}$,8356	54	$\bar{1}$,9013	$\bar{1}$,8901	$\bar{1}$,8417
3	$\bar{1}$,9159	$\bar{1}$,9166	$\bar{1}$,8790	55	$\bar{1}$,8915	$\bar{1}$,8853	$\bar{1}$,8357
4	$\bar{1}$,9401	$\bar{1}$,9315	$\bar{1}$,9081	56	$\bar{1}$,8803	$\bar{1}$,8799	$\bar{1}$,8294
5	$\bar{1}$,9586	$\bar{1}$,9411	$\bar{1}$,9220	57	$\bar{1}$,8680	$\bar{1}$,8732	$\bar{1}$,8228
6	$\bar{1}$,9686	$\bar{1}$,9486	$\bar{1}$,9369	58	$\bar{1}$,8513	$\bar{1}$,8673	$\bar{1}$,8156
7	$\bar{1}$,9737	$\bar{1}$,9544	$\bar{1}$,9476	59	$\bar{1}$,8435	$\bar{1}$,8601	$\bar{1}$,8081
8	$\bar{1}$,9764	$\bar{1}$,9592	$\bar{1}$,9550	60	$\bar{1}$,8318	$\bar{1}$,8511	$\bar{1}$,7998
9	$\bar{1}$,9773	$\bar{1}$,9637	$\bar{1}$,9586	61	$\bar{1}$,8243	$\bar{1}$,8398	$\bar{1}$,7908
10	$\bar{1}$,9768	$\bar{1}$,9669	$\bar{1}$,9592	62	$\bar{1}$,8171	$\bar{1}$,8264	$\bar{1}$,7811
11	$\bar{1}$,9754	$\bar{1}$,9679	$\bar{1}$,9582	63	$\bar{1}$,8090	$\bar{1}$,8120	$\bar{1}$,7699
12	$\bar{1}$,9742	$\bar{1}$,9669	$\bar{1}$,9566	64	$\bar{1}$,7974	$\bar{1}$,7946	$\bar{1}$,7576
13	$\bar{1}$,9729	$\bar{1}$,9658	$\bar{1}$,9546	65	$\bar{1}$,7860	$\bar{1}$,7735	$\bar{1}$,7431
14	$\bar{1}$,9716	$\bar{1}$,9704	$\bar{1}$,9521	66	$\bar{1}$,7703	$\bar{1}$,7510	$\bar{1}$,7267
15	$\bar{1}$,9704	$\bar{1}$,9628	$\bar{1}$,9490	67	$\bar{1}$,7506	$\bar{1}$,7270	$\bar{1}$,7083
16	$\bar{1}$,9698	$\bar{1}$,9609	$\bar{1}$,9455	68	$\bar{1}$,7107	$\bar{1}$,7017	$\bar{1}$,6879
17	$\bar{1}$,9694	$\bar{1}$,9600	$\bar{1}$,9419	69	$\bar{1}$,7005	$\bar{1}$,6754	$\bar{1}$,6651
18	$\bar{1}$,9693	$\bar{1}$,9586	$\bar{1}$,9388	70	$\bar{1}$,6689	$\bar{1}$,6480	$\bar{1}$,6402
19	$\bar{1}$,9690	$\bar{1}$,9574	$\bar{1}$,9358	71	$\bar{1}$,6319	$\bar{1}$,6167	$\bar{1}$,6126
20	$\bar{1}$,9685	$\bar{1}$,9559	$\bar{1}$,9337	72	$\bar{1}$,5936	$\bar{1}$,5841	$\bar{1}$,5823
21	$\bar{1}$,9679	$\bar{1}$,9554	$\bar{1}$,9321	73	$\bar{1}$,5563	$\bar{1}$,5500	$\bar{1}$,5487
22	$\bar{1}$,9670	$\bar{1}$,9549	$\bar{1}$,9311	74	$\bar{1}$,5269	$\bar{1}$,5119	$\bar{1}$,5117
23	$\bar{1}$,9659	$\bar{1}$,9544	$\bar{1}$,9298	75	$\bar{1}$,4940	$\bar{1}$,4711	$\bar{1}$,4723
24	$\bar{1}$,9644	$\bar{1}$,9540	$\bar{1}$,9289	76	$\bar{1}$,4642	$\bar{1}$,4218	$\bar{1}$,4308
25	$\bar{1}$,9628	$\bar{1}$,9534	$\bar{1}$,9277	77	$\bar{1}$,4344	$\bar{1}$,3684	$\bar{1}$,3846
26	$\bar{1}$,9573	$\bar{1}$,9531	$\bar{1}$,9264	78	$\bar{1}$,4007	$\bar{1}$,3134	$\bar{1}$,3307
27	$\bar{1}$,9591	$\bar{1}$,9524	$\bar{1}$,9257	79	$\bar{1}$,3538	$\bar{1}$,2497	$\bar{1}$,2644
28	$\bar{1}$,9570	$\bar{1}$,9521	$\bar{1}$,9238	80	$\bar{1}$,3134	$\bar{1}$,1876	$\bar{1}$,1900
29	$\bar{1}$,9556	$\bar{1}$,9518	$\bar{1}$,9226	81	$\bar{1}$,2582	$\bar{1}$,1214	$\bar{1}$,1101
30	$\bar{1}$,9552	$\bar{1}$,9514	$\bar{1}$,9211	82	$\bar{1}$,2043	$\bar{1}$,0609	$\bar{1}$,0234
31	$\bar{1}$,9548	$\bar{1}$,9514	$\bar{1}$,9196	83	$\bar{1}$,1765	$\bar{2}$,9688	$\bar{2}$,9341
32	$\bar{1}$,9540	$\bar{1}$,9514	$\bar{1}$,9180	84	$\bar{1}$,0727	$\bar{2}$,8536	$\bar{2}$,8592
33	$\bar{1}$,9528	$\bar{1}$,9515	$\bar{1}$,9164	85	$\bar{2}$,9939	$\bar{2}$,7199	$\bar{2}$,7813
34	$\bar{1}$,9513	$\bar{1}$,9517	$\bar{1}$,9146	86	$\bar{2}$,9166	$\bar{2}$,5736	$\bar{2}$,7003
35	$\bar{1}$,9485	$\bar{1}$,9522	$\bar{1}$,9126	87	$\bar{2}$,8490	$\bar{2}$,4254	$\bar{2}$,6149
36	$\bar{1}$,9477	$\bar{1}$,9528	$\bar{1}$,9104	88	$\bar{2}$,8055	$\bar{2}$,1943	$\bar{2}$,5369
37	$\bar{1}$,9452	$\bar{1}$,9534	$\bar{1}$,9083	89	$\bar{2}$,7537	$\bar{3}$,9129	$\bar{2}$,4179
38	$\bar{1}$,9437	$\bar{1}$,9527	$\bar{1}$,8057	90	$\bar{2}$,6695	$\bar{3}$,5265	$\bar{2}$,2414
39	$\bar{1}$,9406	$\bar{1}$,9517	$\bar{1}$,9031	91	$\bar{2}$,6658	$\bar{3}$,0266	$\bar{3}$,9356
40	$\bar{1}$,9383	$\bar{1}$,9506	$\bar{1}$,9001	92	$\bar{2}$,7323	$\bar{4}$,3694	$\bar{3}$,5037
41	$\bar{1}$,9372	$\bar{1}$,9488	$\bar{1}$,8973	93	$\bar{2}$,8031	$\bar{5}$,2971	$\bar{4}$,7375
42	$\bar{1}$,9365	$\bar{1}$,9466	$\bar{1}$,8943	94	$\bar{2}$,8355	—	$\bar{5}$,5769
43	$\bar{1}$,9365	$\bar{1}$,9438	$\bar{1}$,8915	95	$\bar{2}$,8107	—	$\bar{7}$,0496
44	$\bar{1}$,9366	$\bar{1}$,9403	$\bar{1}$,8882	96	$\bar{2}$,8279	—	—
45	$\bar{1}$,9367	$\bar{1}$,9361	$\bar{1}$,8848	97	$\bar{2}$,7589	—	—
46	$\bar{1}$,9366	$\bar{1}$,9308	$\bar{1}$,8810	98	$\bar{2}$,6695	—	—
47	$\bar{1}$,9358	$\bar{1}$,9263	$\bar{1}$,8767	99	$\bar{2}$,5111	—	—
48	$\bar{1}$,9351	$\bar{1}$,9200	$\bar{1}$,8740	100	$\bar{2}$,1629	—	—
49	$\bar{1}$,9328	$\bar{1}$,9158	$\bar{1}$,8631	101	$\bar{3}$,5689	—	—
50	$\bar{1}$,9292	$\bar{1}$,9098	$\bar{1}$,8621	102	$\bar{4}$,3245	—	—
51	$\bar{1}$,9233	$\bar{1}$,9027	$\bar{1}$,8571	103	$\bar{6}$,0595	—	—

TABLE VI.—Accommodated annual ratio for an unlimited period for every age a

$$\lambda r = \lambda \overbrace{{}^{1}_{1}\lfloor a}^{1,05^{-1}} - \lambda \overbrace{{}^{1}_{0}\lfloor a}^{1,05^{-1}} + \lambda\, 1,05.$$

a	λr Carlisle.	λr Deparcieux.	λr Northampton.	a	λr Carlisle.	λr Deparcieux.	λr Northampton.
0	1̄,98665	—	—	52	1̄,98390	1̄,98216	1̄,97950
1	1̄,99121	—	1̄,98517	53	1̄,98305	1̄,98240	1̄,97878
2	1̄,99313	—	1̄,98997	54	1̄,98212	1̄,98156	1̄,97802
3	1̄,99458	1̄,99399	1̄,99151	55	1̄,98112	1̄,98073	1̄,97721
4	1̄,99528	1̄,99446	1̄,99244	56	1̄,98005	1̄,97982	1̄,97635
5	1̄,99577	1̄,99473	1̄,99284	57	1̄,97887	1̄,97882	1̄,97542
6	1̄,99599	1̄,99493	1̄,99324	58	1̄,97763	1̄,97780	1̄,97445
7	1̄,99606	1̄,99505	1̄,99346	59	1̄,97637	1̄,97668	1̄,97341
8	1̄,99606	1̄,99513	1̄,99357	60	1̄,97514	1̄,97545	1̄,97230
9	1̄,99600	1̄,99519	1̄,99354	61	1̄,97400	1̄,97408	1̄,97111
10	1̄,99529	1̄,99519	1̄,99341	62	1̄,97281	1̄,97254	1̄,96983
11	1̄,99576	1̄,99514	1̄,99323	63	1̄,97154	1̄,97093	1̄,96843
12	1̄,99563	1̄,99503	1̄,99304	64	1̄,97014	1̄,96912	1̄,96693
13	1̄,99549	1̄,99491	1̄,99284	65	1̄,96858	1̄,96707	1̄,96526
14	1̄,99535	1̄,99478	1̄,99262	66	1̄,96685	1̄,96489	1̄,96346
15	1̄,99522	1̄,99464	1̄,99240	67	1̄,96491	1̄,96250	1̄,96150
16	1̄,99509	1̄,99450	1̄,99213	68	1̄,96273	1̄,96009	1̄,95936
17	1̄,99487	1̄,99438	1̄,99190	69	1̄,96029	1̄,95750	1̄,95703
18	1̄,99484	1̄,99425	1̄,99167	70	1̄,95755	1̄,95480	1̄,95448
19	1̄,99471	1̄,99413	1̄,99145	71	1̄,95440	1̄,95181	1̄,95171
20	1̄,99455	1̄,99398	1̄,99124	72	1̄,95111	1̄,94870	1̄,94869
21	1̄,99442	1̄,99388	1̄.99106	73	1̄,94784	1̄,94542	1̄,94541
22	1̄,99425	1̄,99375	1̄,99088	74	1̄,94467	1̄,94180	1̄,94186
23	1̄,99408	1̄,99364	1̄,99070	75	1̄,94185	1̄,93790	1̄,93812
24	1̄,99390	1̄,99350	1̄,99051	76	1̄,93888	1̄,93330	1̄,93423
25	1̄,99370	1̄,99338	1̄,99030	77	1̄,93591	1̄,92833	1̄,92994
26	1̄,99349	1̄,99323	1̄,99009	78	1̄,93265	1̄,92314	1̄,92503
27	1̄,99328	1̄,99308	1̄,98988	79	1̄,92863	1̄,91715	1̄,91916
28	1̄,99306	1̄,99293	1̄,98965	80	1̄,92461	1̄,91124	1̄,91246
29	1̄,99290	1̄,99277	1̄,98943	81	1̄,91891	1̄,90493	1̄,90509
30	1̄,99265	1̄,99259	1̄,98917	82	1̄,91491	1̄,89856	1̄,89697
31	1̄,99245	1̄,99241	1̄,98892	83	1̄,90939	1̄,89069	1̄,88844
32	1̄,99224	1̄,99223	1̄,98865	84	1̄,90344	1̄,88005	1̄,88110
33	1̄,99201	1̄,99202	1̄,98837	85	1̄,89657	1̄,86782	1̄,87361
34	1̄,99176	1̄,99181	1̄,98808	86	1̄,88978	1̄,85416	1̄,86599
35	1̄,99149	1̄,99158	1̄,98777	87	1̄,88369	1̄,84011	1̄,85803
36	1̄,99110	1̄,99134	1̄,98745	88	1̄,87972	1̄,81788	1̄,85069
37	1̄,99090	1̄,99109	1̄,98811	89	1̄,87481	1̄,78941	1̄,85454
38	1̄,99058	1̄,99077	1̄,98675	90	1̄,86660	1̄,75223	1̄,82243
39	1̄,99025	1̄,99043	1̄,98637	91	1̄,86560	1̄,70265	1̄,79303
40	1̄,98991	1̄,99006	1̄,98597	92	1̄,87056	1̄,63694	1̄,74992
41	1̄,98958	1̄,98967	1̄,98556	93	1̄,87595	1̄,52971	1̄,67376
42	1̄,98924	1̄,98924	1̄,98513	94	1̄,87840	—	1̄,55753
43	1̄,98890	1̄,98878	1̄,98469	95	1̄,87967	—	1̄,30505
44	1̄,98853	1̄,98828	1̄,98423	96	1̄,77774	—	—
45	1̄,98814	1̄,98771	1̄,98375	97	1̄,77140	—	—
46	1̄,98771	1̄,98714	1̄,98323	98	1̄,76333	—	—
47	1̄,98725	1̄,98655	1̄,98270	99	1̄,84829	—	—
48	1̄,98673	1̄,98590	1̄,98209	100	1̄,81282	—	—
49	1̄,98612	1̄,98526	1̄,98148	101	1̄,75663	—	—
50	1̄,98546	1̄,98456	1̄,98083	102	1̄,65421	—	—
51	1̄,98471	1̄,98386	1̄,98017	103	1̄,40266	—	—

TABLE VII.—Logarithm of Carlisle chance of living 5 years at every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,83232	20	$\bar{1}$,98469	40	$\bar{1}$,96915	60	$\bar{1}$,91826	80	$\bar{1}$,66927
1	$\bar{1}$,89709	21	$\bar{1}$,98457	41	$\bar{1}$,96836	61	$\bar{1}$,91483	81	$\bar{1}$,64194
2	$\bar{1}$,92823	22	$\bar{1}$,98439	42	$\bar{1}$,96790	62	$\bar{1}$,91180	82	$\bar{1}$,61095
3	$\bar{1}$,95354	23	$\bar{1}$,98405	43	$\bar{1}$,96780	63	$\bar{1}$,90864	83	$\bar{1}$,57100
4	$\bar{1}$,96747	24	$\bar{1}$,98333	44	$\bar{1}$,96808	64	$\bar{1}$,90492	84	$\bar{1}$,53422
5	$\bar{1}$,97792	25	$\bar{1}$,98213	45	$\bar{1}$,96857	65	$\bar{1}$,90067	85	$\bar{1}$,50393
6	$\bar{1}$,98376	26	$\bar{1}$,98091	46	$\bar{1}$,96918	66	$\bar{1}$,89586	86	$\bar{1}$,45652
7	$\bar{1}$,98703	27	$\bar{1}$,97967	47	$\bar{1}$,96941	67	$\bar{1}$,88838	87	$\bar{1}$,40377
8	$\bar{1}$,98869	28	$\bar{1}$,97863	48	$\bar{1}$,96915	68	$\bar{1}$,87746	88	$\bar{1}$,36691
9	$\bar{1}$,98930	29	$\bar{1}$,97804	49	$\bar{1}$,96818	69	$\bar{1}$,86279	89	$\bar{1}$,34438
10	$\bar{1}$,98911	30	$\bar{1}$,97789	50	$\bar{1}$,96676	70	$\bar{1}$,84362	90	$\bar{1}$,32483
11	$\bar{1}$,98836	31	$\bar{1}$,97783	51	$\bar{1}$,96477	71	$\bar{1}$,82305	91	$\bar{1}$,34054
12	$\bar{1}$,98754	32	$\bar{1}$,97767	52	$\bar{1}$,96269	72	$\bar{1}$,80220	92	$\bar{1}$,38021
13	$\bar{1}$,98670	33	$\bar{1}$,97736	53	$\bar{1}$,96017	73	$\bar{1}$,78348	93	$\bar{1}$,41373
14	$\bar{1}$,98593	34	$\bar{1}$,97687	54	$\bar{1}$,95660	74	$\bar{1}$,76877	94	$\bar{1}$,43933
15	$\bar{1}$,98528	35	$\bar{1}$,97611	55	$\bar{1}$,95155	75	$\bar{1}$,75508	95	$\bar{1}$,47712
16	$\bar{1}$,98490	36	$\bar{1}$,97490	56	$\bar{1}$,94461	76	$\bar{1}$,74231	96	$\bar{1}$,48337
17	$\bar{1}$,98479	37	$\bar{1}$,97349	57	$\bar{1}$,93711	77	$\bar{1}$,72712	97	$\bar{1}$,44370
18	$\bar{1}$,98476	38	$\bar{1}$,97194	58	$\bar{1}$,92973	78	$\bar{1}$,71062	98	$\bar{1}$,33099
19	$\bar{1}$,98472	39	$\bar{1}$,97044	59	$\bar{1}$,92343	79	$\bar{1}$,68963		

Logarithm of the Carlisle chance of living 10 years at every age *a*.

0	$\bar{1}$,81023	19	$\bar{1}$,96805	38	$\bar{1}$,93973	57	$\bar{1}$,84891	76	$\bar{1}$,38425
1	$\bar{1}$,88086	20	$\bar{1}$,96682	39	$\bar{1}$,93851	58	$\bar{1}$,83836	77	$\bar{1}$,33807
2	$\bar{1}$,91526	21	$\bar{1}$,96548	40	$\bar{1}$,93772	59	$\bar{1}$,82835	78	$\bar{1}$,28163
3	$\bar{1}$,94223	22	$\bar{1}$,96406	41	$\bar{1}$,93754	60	$\bar{1}$,81893	79	$\bar{1}$,22385
4	$\bar{1}$,95677	23	$\bar{1}$,96268	42	$\bar{1}$,93731	61	$\bar{1}$,81070	80	$\bar{1}$,17320
5	$\bar{1}$,96702	24	$\bar{1}$,96136	43	$\bar{1}$,93694	62	$\bar{1}$,80018	81	$\bar{1}$,09846
6	$\bar{1}$.97213	25	$\bar{1}$,96002	44	$\bar{1}$,93626	63	$\bar{1}$,78610	82	$\bar{1}$,01472
7	$\bar{1}$,97457	26	$\bar{1}$,95873	45	$\bar{1}$,93533	64	$\bar{1}$,76771	83	$\bar{2}$,93791
8	$\bar{1}$,97540	27	$\bar{1}$,95734	46	$\bar{1}$,93395	65	$\bar{1}$,74430	84	$\bar{2}$,87860
	$\bar{1}$,97523	28	$\bar{1}$,95598	47	$\bar{1}$,93211	66	$\bar{1}$,71891	85	$\bar{2}$,82876
10	$\bar{1}$,97438	29	$\bar{1}$,95490	48	$\bar{1}$,92932	67	$\bar{1}$,69058	86	$\bar{2}$,79706
11	$\bar{1}$,97326	30	$\bar{1}$,95400	49	$\bar{1}$,92478	68	$\bar{1}$,66094	87	$\bar{2}$,78398
12	$\bar{1}$,97233	31	$\bar{1}$,95273	50	$\bar{1}$,91830	69	$\bar{1}$,63157	88	$\bar{2}$,78064
13	$\bar{1}$,97146	32	$\bar{1}$,95116	51	$\bar{1}$,90938	70	$\bar{1}$,59870	89	$\bar{2}$,78371
14	$\bar{1}$,07065	33	$\bar{1}$,94929	52	$\bar{1}$,89980	71	$\bar{1}$,56536	90	$\bar{2}$,80195
15	$\bar{1}$,96996	34	$\bar{1}$,94730	53	$\bar{1}$,88990	72	$\bar{1}$,52932	91	$\bar{2}$,82391
16	$\bar{1}$,96947	35	$\bar{1}$,94526	54	$\bar{1}$,88003	73	$\bar{1}$,49411	92	$\bar{2}$,82391
17	$\bar{1}$,96918	36	$\bar{1}$,94326	55	$\bar{1}$,86981	74	$\bar{1}$,45840	93	$\bar{2}$,74473
18	$\bar{1}$,96881	37	$\bar{1}$,94138	56	$\bar{1}$,85944	75	$\bar{1}$,42434		

TABLE VII.—*continued.*

Logarithm of the Carlisle chance of living 15 years for every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,79934	18	$\bar{1}$,94744	36	$\bar{1}$,91244	54	$\bar{1}$,78495	72	$\bar{1}$,14027
1	$\bar{1}$,86922	19	$\bar{1}$,94609	37	$\bar{1}$,91080	55	$\bar{1}$,77048	73	$\bar{1}$,06511
2	$\bar{1}$,90280	20	$\bar{1}$,94471	38	$\bar{1}$,90888	56	$\bar{1}$,75530	74	$\bar{2}$,99263
3	$\bar{1}$,92893	21	$\bar{1}$,94331	39	$\bar{1}$,90669	57	$\bar{1}$,73729	75	$\bar{2}$,92827
4	$\bar{1}$,94270	22	$\bar{1}$,94173	40	$\bar{1}$,90448	58	$\bar{1}$,71582	76	$\bar{2}$,84078
5	$\bar{1}$,95230	23	$\bar{1}$,94004	41	$\bar{1}$,90231	59	$\bar{1}$,69114	77	$\bar{2}$,74184
6	$\bar{1}$,95702	24	$\bar{1}$,93823	42	$\bar{1}$,90000	60	$\bar{1}$,66256	78	$\bar{2}$,64853
7	$\bar{1}$,95936	25	$\bar{1}$,93613	43	$\bar{1}$,89712	61	$\bar{1}$,63375	79	$\bar{2}$,56823
8	$\bar{1}$,96015	26	$\bar{1}$,93364	44	$\bar{1}$,89284	62	$\bar{1}$,60238	80	$\bar{2}$,49803
9	$\bar{1}$,95995	27	$\bar{1}$ 93082	45	$\bar{1}$,88687	63	$\bar{1}$,56958	81	$\bar{2}$,43900
10	$\bar{1}$,95907	28	$\bar{1}$,92792	46	$\bar{1}$,87856	64	$\bar{1}$,53648	82	$\bar{2}$,39494
11	$\bar{1}$,95784	29	$\bar{1}$,92534	47	$\bar{1}$,86922	65	$\bar{1}$,49937	83	$\bar{2}$,35164
12	$\bar{1}$,95672	30	$\bar{1}$,92316	48	$\bar{1}$,85905	66	$\bar{1}$,46123	84	$\bar{2}$,31794
13	$\bar{1}$,95551	31	$\bar{1}$,92108	49	$\bar{1}$,84820	67	$\bar{1}$,41770	85	$\bar{2}$,30588
14	$\bar{1}$,95397	32	$\bar{1}$,91905	50	$\bar{1}$,83656	68	$\bar{1}$,37157	86	$\bar{2}$,28043
15	$\bar{1}$,95209	33	$\bar{1}$,91709	51	$\bar{1}$,82421	69	$\bar{1}$,32120	87	$\bar{2}$,22768
16	$\bar{1}$,95038	34	$\bar{1}$,91538	52	$\bar{1}$,81160	70	$\bar{1}$,26797	88	$\bar{2}$,11163
17	$\bar{1}$,94885	35	$\bar{1}$,91383	53	$\bar{1}$,79853	71	$\bar{1}$,20730		

Logarithm of the Carlisle chance of living 20 years for every age *a*.

0	$\bar{1}$,78462	17	$\bar{1}$,92652	34	$\bar{1}$,88356	51	$\bar{1}$,72007	68	$\bar{2}$,94257
1	$\bar{1}$,85412	18	$\bar{1}$,92479	35	$\bar{1}$,88059	52	$\bar{1}$,69998	69	$\bar{2}$,85542
2	$\bar{1}$,88759	19	$\bar{1}$,92295	36	$\bar{1}$,87721	53	$\bar{1}$,67599	70	$\bar{2}$,77190
3	$\bar{1}$,91369	20	$\bar{1}$,92082	37	$\bar{1}$,87349	54	$\bar{1}$,64744	71	$\bar{2}$,66383
4	$\bar{1}$,92742	21	$\bar{1}$,91821	38	$\bar{1}$,86906	55	$\bar{1}$,61410	72	$\bar{2}$,54404
5	$\bar{1}$,93699	22	$\bar{1}$,91521	39	$\bar{1}$,86329	56	$\bar{1}$,57835	73	$\bar{2}$,43202
6	$\bar{1}$,94160	23	$\bar{1}$,91197	40	$\bar{1}$,85602	57	$\bar{1}$,53949	74	$\bar{2}$,33701
7	$\bar{1}$,94376	24	$\bar{1}$,90866	41	$\bar{1}$,84692	58	$\bar{1}$,49930	75	$\bar{2}$,25311
8	$\bar{1}$,94421	25	$\bar{1}$,90528	42	$\bar{1}$,83711	59	$\bar{1}$,45991	76	$\bar{2}$,18132
9	$\bar{1}$,94328	26	$\bar{1}$,90199	43	$\bar{1}$,82684	60	$\bar{1}$,41763	77	$\bar{2}$,12205
10	$\bar{1}$,94120	27	$\bar{1}$,89872	45	$\bar{1}$,81628	61	$\bar{1}$,37606	78	$\bar{2}$,06227
11	$\bar{1}$,93874	28	$\bar{1}$,89572	45	$\bar{1}$,80513	62	$\bar{1}$,32950	79	$\bar{2}$,00757
12	$\bar{1}$,93639	29	$\bar{1}$,89342	46	$\bar{1}$,79339	63	$\bar{1}$,28021	80	$\bar{3}$,97515
13	$\bar{1}$,93414	30	$\bar{1}$,89172	45	$\bar{1}$,78101	64	$\bar{1}$,22611	81	$\bar{3}$,92237
14	$\bar{1}$,93201	31	$\bar{1}$,89027	48	$\bar{1}$,76768	65	$\bar{1}$,16864	82	$\bar{3}$,83863
15	$\bar{1}$,92999	32	$\bar{1}$,88847	49	$\bar{1}$,75312	66	$\bar{1}$,10317	83	$\bar{3}$,68263
16	$\bar{1}$,92821	33	$\bar{1}$,88624	50	$\bar{1}$,73723	67	$\bar{1}$,02866		

TABLE VII.—*continued.*

Logarithm of the Carlisle chance of living 25 years at every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,76930	16	$\bar{1}$,90311	32	$\bar{1}$,85116	48	$\bar{1}$,64514	64	$\bar{2}$,76034
1	$\bar{1}$,83969	17	$\bar{1}$,90001	33	$\bar{1}$,84641	49	$\bar{1}$,61591	65	$\bar{2}$,67257
2	$\bar{1}$,87198	18	$\bar{1}$,89673	34	$\bar{1}$,84016	50	$\bar{1}$,58086	66	$\bar{2}$,55969
3	$\bar{1}$,89774	19	$\bar{1}$,89339	35	$\bar{1}$,83213	51	$\bar{1}$,5431	67	$\bar{2}$,43242
4	$\bar{1}$,91075	20	$\bar{1}$,88997	36	$\bar{1}$,82182	52	$\bar{1}$,50218	68	$\bar{2}$,30948
5	$\bar{1}$,91912	21	$\bar{1}$,88657	37	$\bar{1}$,81060	53	$\bar{1}$,45948	69	$\bar{2}$,19980
6	$\bar{1}$,92251	22	$\bar{1}$,88311	38	$\bar{1}$,79878	54	$\bar{1}$,41651	70	$\bar{2}$,09673
7	$\bar{1}$,92342	23	$\bar{1}$,87977	39	$\bar{1}$,78672	55	$\bar{1}$,36918	71	$\bar{2}$,00437
8	$\bar{1}$,92283	24	$\bar{1}$,87674	40	$\bar{1}$,77428	56	$\bar{1}$,32067	72	$\bar{3}$,92425
9	$\bar{1}$,92131	25	$\bar{1}$,87385	41	$\bar{1}$,76175	57	$\bar{1}$,26661	73	$\bar{3}$,84575
10	$\bar{1}$,91909	26	$\bar{1}$,87117	42	$\bar{1}$,74891	58	$\bar{1}$,20993	74	$\bar{3}$,77634
11	$\bar{1}$,91657	27	$\bar{1}$,86813	43	$\bar{1}$,73548	59	$\bar{1}$,14954	75	$\bar{3}$,73023
12	$\bar{1}$,91406	28	$\bar{1}$,86487	44	$\bar{1}$,72120	60	$\bar{1}$,08690	76	$\bar{3}$,66469
13	$\bar{1}$,91150	29	$\bar{1}$,86159	45	$\bar{1}$,70581	61	$\bar{1}$,01800	77	$\bar{3}$,56575
14	$\bar{1}$,90888	30	$\bar{1}$,85848	46	$\bar{1}$,68926	62	$\bar{2}$,94045	78	$\bar{3}$,39326
15	$\bar{1}$,90610	31	$\bar{1}$,85504	47	$\bar{1}$,66940	63	$\bar{2}$,85121		

Logarithm of the Carlisle chance of living 30 years at every age *a*.

0	$\bar{1}$,75143	15	$\bar{1}$,87525	30	$\bar{1}$,81003	45	$\bar{1}$,54943	60	$\bar{2}$,59083
1	$\bar{1}$,81960	16	$\bar{1}$,87146	31	$\bar{1}$,79964	46	$\bar{1}$,51231	61	$\bar{2}$,47452
2	$\bar{1}$,85164	17	$\bar{1}$,86790	32	$\bar{1}$,78827	47	$\bar{1}$,47160	62	$\bar{2}$,34422
3	$\bar{1}$,87637	18	$\bar{1}$,86453	33	$\bar{1}$,77614	48	$\bar{1}$,42863	63	$\bar{2}$,21811
4	$\bar{1}$,88879	19	$\bar{1}$,86147	34	$\bar{1}$,76358	49	$\bar{1}$,38467	64	$\bar{2}$,10472
5	$\bar{1}$,89701	20	$\bar{1}$,85854	35	$\bar{1}$,75039	50	$\bar{1}$,33594	65	$\bar{3}$,99740
6	$\bar{1}$,90033	21	$\bar{1}$,85575	36	$\bar{1}$,73665	51	$\bar{1}$,28544	66	$\bar{3}$,90023
7	$\bar{1}$,90109	22	$\bar{1}$,85253	37	$\bar{1}$,72240	52	$\bar{1}$,22930	67	$\bar{3}$,81264
8	$\bar{1}$,90019	23	$\bar{1}$,84892	38	$\bar{1}$,70742	53	$\bar{1}$,17010	68	$\bar{3}$,72321
9	$\bar{1}$,89818	24	$\bar{1}$,84492	39	$\bar{1}$,69164	54	$\bar{1}$,10614	69	$\bar{3}$,63913
10	$\bar{1}$,89520	25	$\bar{1}$,84061	40	$\bar{1}$,67496	55	$\bar{1}$,03845	70	$\bar{3}$,57385
11	$\bar{1}$,89147	26	$\bar{1}$,83594	41	$\bar{1}$,65761	56	$\bar{2}$,96261	71	$\bar{3}$,48774
12	$\bar{1}$,88755	27	$\bar{1}$,83083	42	$\bar{1}$,63729	57	$\bar{2}$,87756	72	$\bar{3}$,36795
13	$\bar{1}$,88344	28	$\bar{1}$,82504	43	$\bar{1}$,61294	58	$\bar{2}$,78093	73	$\bar{3}$,17674
14	$\bar{1}$,87931	29	$\bar{1}$,81819	44	$\bar{1}$,58399	59	$\bar{2}$,68376		

Logarithm of the Carlisle chance of living 35 years for every age *a*.

0	$\bar{1}$,72933	14	$\bar{1}$,84739	28	$\bar{1}$,75476	42	$\bar{1}$,43949	56	$\bar{2}$,41913
1	$\bar{1}$,79743	15	$\bar{1}$,84382	29	$\bar{1}$,74162	43	$\bar{1}$,39642	57	$\bar{2}$,28133
2	$\bar{1}$,82932	16	$\bar{1}$,84065	30	$\bar{1}$,72829	44	$\bar{1}$,35277	58	$\bar{2}$,14784
3	$\bar{1}$,85373	17	$\bar{1}$,83732	31	$\bar{1}$,71448	45	$\bar{1}$,30451	59	$\bar{2}$,02815
4	$\bar{1}$,86565	18	$\bar{1}$,83368	32	$\bar{1}$,70007	46	$\bar{1}$,25462	60	$\bar{3}$,91566
5	$\bar{1}$,87312	19	$\bar{1}$,82964	33	$\bar{1}$,68477	47	$\bar{1}$,19872	61	$\bar{3}$,81506
6	$\bar{1}$,87523	20	$\bar{1}$,82530	34	$\bar{1}$,66850	48	$\bar{1}$,13925	62	$\bar{3}$,72443
7	$\bar{1}$,87458	21	$\bar{1}$,82052	35	$\bar{1}$,65106	49	$\bar{1}$,07432	63	$\bar{3}$,63185
8	$\bar{1}$,87213	22	$\bar{1}$,81522	36	$\bar{1}$,63251	50	$\bar{1}$,00520	64	$\bar{3}$,54405
9	$\bar{1}$,86861	23	$\bar{1}$,80909	37	$\bar{1}$,61078	51	$\bar{2}$,92738	65	$\bar{3}$,47452
10	$\bar{1}$,86435	24	$\bar{1}$,80152	38	$\bar{1}$,58488	52	$\bar{2}$,84025	66	$\bar{3}$,38360
11	$\bar{1}$,85983	25	$\bar{1}$,79216	39	$\bar{1}$,55443	53	$\bar{2}$,74110	67	$\bar{3}$,25633
12	$\bar{1}$,85544	26	$\bar{1}$,78055	40	$\bar{1}$,51858	54	$\bar{2}$,64036	68	$\bar{3}$,05420
13	$\bar{1}$,85123	27	$\bar{1}$,76794	41	$\bar{1}$,48066	55	$\bar{2}$,54237		

TABLE VII.—*continued.*

Logarithm of the Carlisle chance of living 40 years for every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,70544	13	$\bar{1}$,82038	26	$\bar{1}$,69538	39	$\bar{1}$,32320	52	$\bar{2}$,24402
1	$\bar{1}$,77233	14	$\bar{1}$,81557	27	$\bar{1}$,67973	40	$\bar{1}$,27366	53	$\bar{2}$,10801
2	$\bar{1}$,80280	15	$\bar{1}$,81057	28	$\bar{1}$,66340	41	$\bar{1}$,22298	54	$\bar{3}$,98474
3	$\bar{1}$,82567	16	$\bar{1}$,80542	29	$\bar{1}$,64654	42	$\bar{1}$,16661	55	$\bar{3}$,86721
4	$\bar{1}$,83609	17	$\bar{1}$,80001	30	$\bar{1}$,62896	43	$\bar{1}$,10705	56	$\bar{3}$,75967
5	$\bar{1}$,84227	18	$\bar{1}$,79385	31	$\bar{1}$,61034	44	$\bar{1}$,04240	57	$\bar{3}$,66154
6	$\bar{1}$,84359	19	$\bar{1}$,78624	32	$\bar{1}$,58845	45	$\bar{2}$,97377	58	$\bar{3}$,56157
7	$\bar{1}$,84247	20	$\bar{1}$,77684	33	$\bar{1}$,56223	46	$\bar{2}$,89656	59	$\bar{3}$,46748
8	$\bar{1}$,83992	21	$\bar{1}$,76513	34	$\bar{1}$,53130	47	$\bar{2}$,80967	60	$\bar{3}$,39278
9	$\bar{1}$,83669	22	$\bar{1}$,75233	35	$\bar{1}$,49469	48	$\bar{2}$,71025	61	$\bar{3}$,29843
10	$\bar{1}$,83292	23	$\bar{1}$,73882	36	$\bar{1}$,45556	49	$\bar{2}$,60854	62	$\bar{3}$,16813
11	$\bar{1}$,82901	24	$\bar{1}$,72494	37	$\bar{1}$,41298	50	$\bar{2}$,50913	63	$\bar{4}$,96284
12	$\bar{1}$,82486	25	$\bar{1}$,71042	38	$\bar{1}$,36836	51	$\bar{2}$,38390		

Logarithm of the Carlisle chance of living 45 years for every age *a*.

0	$\bar{1}$,67459	12	$\bar{1}$,78755	24	$\bar{1}$,62987	36	$\bar{1}$,19787	48	$\bar{2}$,07716
1	$\bar{1}$,74068	13	$\bar{1}$,78055	25	$\bar{1}$,61109	37	$\bar{1}$,14010	49	$\bar{3}$,95292
2	$\bar{1}$,77070	14	$\bar{1}$,77217	26	$\bar{1}$,59125	38	$\bar{1}$,07899	50	$\bar{3}$,83396
3	$\bar{1}$,79346	15	$\bar{1}$,76212	27	$\bar{1}$,56812	39	$\bar{1}$,01283	51	$\bar{3}$,72444
4	$\bar{1}$,80417	16	$\bar{1}$,75002	28	$\bar{1}$,54086	40	$\bar{2}$,94292	52	$\bar{3}$,62423
5	$\bar{1}$,81084	17	$\bar{1}$,73712	29	$\bar{1}$,50933	41	$\bar{2}$,86492	53	$\bar{3}$,52174
6	$\bar{1}$,81277	18	$\bar{1}$,72357	30	$\bar{1}$,47258	42	$\bar{2}$,77756	54	$\bar{3}$,42408
7	$\bar{1}$,81190	19	$\bar{1}$,70967	31	$\bar{1}$,43339	43	$\bar{2}$,67805	55	$\bar{3}$,34433
8	$\bar{1}$,80907	20	$\bar{1}$,69510	32	$\bar{1}$,39065	44	$\bar{2}$,57662	56	$\bar{3}$,24304
9	$\bar{1}$,80487	21	$\bar{1}$,67996	33	$\bar{1}$,34571	45	$\bar{2}$,47770	57	$\bar{3}$,10524
10	$\bar{1}$,79968	22	$\bar{1}$,66412	34	$\bar{1}$,30007	46	$\bar{2}$,35308	58	$\bar{4}$ 89256
11	$\bar{1}$,79378	23	$\bar{1}$,64745	35	$\bar{1}$,24977	47	$\bar{2}$,21344		

Logarithm of the Carlisle chance of living 50 years for every age *a*.

0	$\bar{1}$,64316	11	$\bar{1}$,73839	22	$\bar{1}$,55251	33	$\bar{1}$,05634	44	$\bar{3}$,92100
1	$\bar{1}$,70987	12	$\bar{1}$,72466	23	$\bar{1}$,52491	34	$\bar{2}$,98970	45	$\bar{3}$,80253
2	$\bar{1}$,74011	13	$\bar{1}$,71028	24	$\bar{1}$,49266	35	$\bar{2}$,91903	46	$\bar{3}$,69362
3	$\bar{1}$,76261	14	$\bar{1}$,69560	25	$\bar{1}$,45471	36	$\bar{2}$,83982	47	$\bar{3}$,59365
4	$\bar{1}$,77234	15	$\bar{1}$,68038	26	$\bar{1}$,41430	37	$\bar{2}$,75105	48	$\bar{3}$,49089
5	$\bar{1}$,77760	16	$\bar{1}$,66486	27	$\bar{1}$,37032	38	$\bar{2}$,65000	49	$\bar{3}$,39225
6	$\bar{1}$,77754	17	$\bar{1}$,64892	28	$\bar{1}$,32434	39	$\bar{2}$,54705	50	$\bar{3}$,31109
7	$\bar{1}$,77458	18	$\bar{1}$,63222	29	$\bar{1}$,27810	40	$\bar{2}$,44685	51	$\bar{3}$,20781
8	$\bar{1}$,76925	19	$\bar{1}$,61459	30	$\bar{1}$,22766	41	$\bar{2}$,32144	52	$\bar{3}$,06793
9	$\bar{1}$,76147	20	$\bar{1}$,59577	31	$\bar{1}$,17570	42	$\bar{2}$,18133	53	$\bar{4}$,85274
10	$\bar{1}$,75123	21	$\bar{1}$,57582	32	$\bar{1}$,11777	43	$\bar{2}$,04495		

TABLE VII.—*continued.*

Logarithm of the Carlisle chance of living 55 years for every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,60991	10	$\bar{1}$,66949	20	$\bar{1}$,43940	30	$\bar{2}$,89693	40	$\bar{3}$,77168
1	$\bar{1}$,67464	11	$\bar{1}$,65322	21	$\bar{1}$,39887	31	$\bar{2}$,81764	41	$\bar{3}$,66198
2	$\bar{1}$,70281	12	$\bar{1}$,63646	22	$\bar{1}$,35471	32	$\bar{2}$,72872	42	$\bar{3}$,56155
3	$\bar{1}$,72278	13	$\bar{1}$,61892	23	$\bar{1}$,30840	33	$\bar{2}$,62734	43	$\bar{3}$,45869
4	$\bar{1}$,72894	14	$\bar{1}$,60051	24	$\bar{1}$,26143	34	$\bar{2}$,52392	44	$\bar{3}$,36033
5	$\bar{1}$,72914	15	$\bar{1}$,58105	25	$\bar{1}$,20979	35	$\bar{2}$,42296	45	$\bar{3}$,27966
6	$\bar{1}$,72215	16	$\bar{1}$,56072	26	$\bar{1}$,15661	36	$\bar{2}$,29634	46	$\bar{3}$,17699
7	$\bar{1}$,71169	17	$\bar{1}$,53730	27	$\bar{1}$,09743	37	$\bar{2}$,15482	47	$\bar{3}$,03735
8	$\bar{1}$,69897	18	$\bar{1}$,50967	28	$\bar{1}$,03497	38	$\bar{2}$,01689	48	$\bar{4}$,82189
9	$\bar{1}$,68490	19	$\bar{1}$,47738	29	$\bar{2}$,96773	39	$\bar{3}$,89144		

Logarithm of the Carlisle chance of living 60 years for every age *a*.

0	$\bar{1}$,56146	9	$\bar{1}$,58982	18	$\bar{1}$,29315	27	$\bar{2}$,70839	36	$\bar{3}$,63689
1	$\bar{1}$,61925	10	$\bar{1}$,57016	19	$\bar{1}$,24615	28	$\bar{2}$,60597	37	$\bar{3}$,53503
2	$\bar{1}$,63992	11	$\bar{1}$,54908	20	$\bar{1}$,19448	29	$\bar{2}$,50196	38	$\bar{3}$,43063
3	$\bar{1}$,65251	12	$\bar{1}$,52484	21	$\bar{1}$,14119	30	$\bar{2}$,40086	39	$\bar{3}$,33077
4	$\bar{1}$,65237	13	$\bar{1}$,49638	22	$\bar{1}$,08183	31	$\bar{2}$,27417	40	$\bar{3}$,24881
5	$\bar{1}$,64740	14	$\bar{1}$,46331	23	$\bar{1}$,01902	32	$\bar{2}$,13249	41	$\bar{3}$,14535
6	$\bar{1}$,63698	15	$\bar{1}$,42467	24	$\bar{2}$,95106	33	$\bar{3}$,99425	42	$\bar{3}$,00524
7	$\bar{1}$,62349	16	$\bar{1}$,38377	25	$\bar{2}$,87906	34	$\bar{3}$,86830	43	$\bar{4}$,78968
8	$\bar{1}$,60761	17	$\bar{1}$,33950	26	$\bar{2}$,79855	35	$\bar{3}$,74779		

Logarithm of the Carlisle chance of living 65 years for every age *a*.

0	$\bar{1}$,47972	8	$\bar{1}$,48507	16	$\bar{1}$,12608	24	$\bar{2}$,48528	32	$\bar{3}$,51270
1	$\bar{1}$,53408	9	$\bar{1}$,45261	17	$\bar{1}$,06662	25	$\bar{2}$,38298	33	$\bar{3}$,40798
2	$\bar{1}$,55171	10	$\bar{1}$,41378	18	$\bar{1}$,00378	26	$\bar{2}$,25507	34	$\bar{3}$,30763
3	$\bar{1}$,56115	11	$\bar{1}$,37213	19	$\bar{2}$,93578	27	$\bar{2}$,11216	35	$\bar{3}$,22492
4	$\bar{1}$,55729	12	$\bar{1}$,32704	20	$\bar{2}$,86374	28	$\bar{3}$,97288	36	$\bar{3}$,12025
5	$\bar{1}$,54807	13	$\bar{1}$,27986	21	$\bar{2}$,78313	29	$\bar{3}$,84634	37	$\bar{4}$,97873
6	$\bar{1}$,53285	14	$\bar{1}$,23208	22	$\bar{2}$,69278	30	$\bar{3}$,72569	38	$\bar{4}$,76162
7	$\bar{1}$,51187	15	$\bar{1}$,17975	23	$\bar{2}$,59002	31	$\bar{3}$,61471		

Logarithm of the Carlisle chance of living 70 years for every age *a*.

0	$\bar{1}$,38039	7	$\bar{1}$,31407	14	$\bar{2}$,92171	21	$\bar{2}$,23965	28	$\bar{3}$,38661
1	$\bar{1}$,42994	8	$\bar{1}$,26855	15	$\bar{2}$,84902	22	$\bar{2}$,09655	29	$\bar{3}$,28567
2	$\bar{1}$,44010	9	$\bar{1}$,22138	16	$\bar{2}$,76802	23	$\bar{3}$,95693	30	$\bar{3}$,20281
3	$\bar{1}$,43861	10	$\bar{1}$,16886	17	$\bar{2}$,67757	24	$\bar{3}$,82967	31	$\bar{3}$,09808
4	$\bar{1}$,42008	11	$\bar{1}$,11445	18	$\bar{2}$,57478	25	$\bar{3}$,70782	32	$\bar{4}$,95640
5	$\bar{1}$,39170	12	$\bar{1}$,05416	19	$\bar{2}$,47001	26	$\bar{3}$,59561	33	$\bar{4}$,73897
6	$\bar{1}$,35590	13	$\bar{2}$,99049	20	$\bar{2}$,36767	27	$\bar{3}$,49237		

TABLE VII.—*continued.*

Logarithm of the Carlisle chance of living 75 years for every age *a*.

a	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.	*a*	λ chance.
0	$\bar{1}$,22402	6	$\bar{1}$,09821	12	$\bar{2}$,66511	18	$\bar{3}$,94169	24	$\bar{3}$,26900
1	$\bar{1}$,25299	7	$\bar{1}$,04119	13	$\bar{2}$,56149	19	$\bar{3}$,81439	25	$\bar{3}$,18494
2	$\bar{1}$,24230	8	$\bar{2}$,97918	14	$\bar{2}$,45593	20	$\bar{3}$,69250	26	$\bar{3}$,07898
3	$\bar{1}$,22209	9	$\bar{2}$,91101	15	$\bar{2}$,35295	21	$\bar{3}$,58019	27	$\bar{4}$,93607
4	$\bar{1}$ 18885	10	$\bar{2}$,83813	16	$\bar{2}$,22455	22	$\bar{3}$,47676	28	$\bar{4}$,71760
5	$\bar{1}$,14678	11	$\bar{2}$,75639	17	$\bar{2}$,08134	23	$\bar{3}$,37066		

Logarithm of the Carlisle chance of living 80 years for every age *a*.

0	$\bar{2}$,97909	5	$\bar{2}$,81604	10	$\bar{2}$,34206	15	$\bar{3}$,67778	20	$\bar{3}$,16963
1	$\bar{2}$,99530	6	$\bar{2}$,74015	11	$\bar{2}$,21291	16	$\bar{3}$,56508	21	$\bar{3}$,06356
2	$\bar{2}$,96941	7	$\bar{2}$,65214	12	$\bar{2}$,06888	17	$\bar{3}$,46155	22	$\bar{4}$,92046
3	$\bar{2}$,93272	8	$\bar{2}$,55018	13	$\bar{3}$,92839	18	$\bar{3}$,35542	23	$\bar{4}$,70166
4	$\bar{2}$,87848	9	$\bar{2}$,44523	14	$\bar{3}$,80031	19	$\bar{3}$,25372		

Logarithm of the Carlisle chance of living 85 years for every age *a*.

0	$\bar{2}$,64836	4	$\bar{2}$,41271	8	$\bar{3}$,91708	12	$\bar{3}$,44909	16	$\bar{3}$,04845
1	$\bar{2}$,63724	5	$\bar{2}$,31997	9	$\bar{3}$,78962	13	$\bar{3}$,34213	17	$\bar{4}$,90525
2	$\bar{2}$,58037	6	$\bar{2}$,19667	10	$\bar{3}$,66689	14	$\bar{3}$,23965	18	$\bar{4}$,68641
3	$\bar{2}$,50372	7	$\bar{2}$,05591	11	$\bar{3}$,55345	15	$\bar{3}$,15490		

Logarithm of the Carlisle chance of living 90 years for every age *a*.

0	$\bar{2}$,15229	3	$\bar{3}$,87062	6	$\bar{3}$,53721	9	$\bar{3}$,22895	12	$\bar{4}$,89279
1	$\bar{2}$,09377	4	$\bar{3}$,75709	7	$\bar{3}$,43612	10	$\bar{3}$,14401	13	$\bar{4}$,67312
2	$\bar{3}$,98414	5	$\bar{3}$,64480	8	$\bar{3}$,33082	11	$\bar{3}$,03682		

Logarithm of the Carlisle chance of living 95 years for every age *a*.

0	$\bar{3}$,47712	2	$\bar{3}$,36435	4	$\bar{3}$,19642	6	$\bar{3}$,02058	8	4,66181
1	$\bar{3}$,43431	3	$\bar{3}$,28436	5	$\bar{3}$,12193	7	$\bar{4}$,87982		

Logarithm of the Carlisle chance of living 100 years for every age *a*.

0	$\bar{4}$,95424	1	$\bar{4}$,91768	2	$\bar{4}$,80805	3	$\bar{4}$,61535

TABLE VIII.—Logarithm of Deparcieux chance of living for every age *a*.

a	10 years.	20 years.	30 years.	40 years.	50 years.	60 years.	70 years.	80 years.	90 years.
0									
1									
2									
3	$\bar{1}$,93450	$\bar{1}$,89763	$\bar{1}$,85126	$\bar{1}$,80346	$\bar{1}$,73957	$\bar{1}$,62634	$\bar{1}$,39967	$\bar{2}$,85126	$\bar{3}$,30103
4	$\bar{1}$,94469	$\bar{1}$,90644	$\bar{1}$,85957	$\bar{1}$,81188	$\bar{1}$,74401	$\bar{1}$,62495	$\bar{1}$,37684	$\bar{2}$,78408	$\bar{3}$,01323
5	$\bar{1}$,95159	$\bar{1}$,91193	$\bar{1}$,86455	$\bar{1}$,81698	$\bar{1}$,74418	$\bar{1}$,61979	$\bar{1}$,34747	$\bar{2}$,70443	
6	$\bar{1}$,95683	$\bar{1}$,91575	$\bar{1}$,86784	$\bar{1}$,82040	$\bar{1}$,74248	$\bar{1}$,61130	$\bar{1}$,31482	$\bar{2}$,61130	
7	$\bar{1}$,96027	$\bar{1}$,91825	$\bar{1}$,86981	$\bar{1}$,82177	$\bar{1}$,73928	$\bar{1}$,59968	$\bar{1}$,27663	$\bar{2}$,50098	
8	$\bar{1}$,96282	$\bar{1}$,91985	$\bar{1}$,87151	$\bar{1}$,82222	$\bar{1}$,73410	$\bar{1}$,58512	$\bar{1}$,23231	$\bar{2}$,38721	
9	$\bar{1}$,96495	$\bar{1}$,92101	$\bar{1}$,87278	$\bar{1}$,82146	$\bar{1}$,72821	$\bar{1}$,56781	$\bar{1}$,18415	$\bar{2}$,25473	
10	$\bar{1}$,96614	$\bar{1}$,92122	$\bar{1}$,87309	$\bar{1}$,81970	$\bar{1}$,72110	$\bar{1}$,54688	$\bar{1}$,12740	$\bar{2}$,09691	
11	$\bar{1}$,96582	$\bar{1}$,92042	$\bar{1}$,87239	$\bar{1}$,81612	$\bar{1}$,71269	$\bar{1}$,52337	$\bar{1}$,06380	$\bar{3}$,90458	
12	$\bar{1}$,96448	$\bar{1}$,91860	$\bar{1}$,87069	$\bar{1}$,81067	$\bar{1}$,70296	$\bar{1}$,49545	$\bar{2}$,99190	$\bar{3}$,66454	
13	$\bar{1}$,96313	$\bar{1}$,91676	$\bar{1}$,86896	$\bar{1}$,80507	$\bar{1}$,69184	$\bar{1}$,46517	$\bar{2}$,91676	$\bar{3}$,36653	
14	$\bar{1}$,96175	$\bar{1}$,91488	$\bar{1}$,86719	$\bar{1}$,79932	$\bar{1}$,68026	$\bar{1}$,43215	$\bar{2}$,83939	$\bar{3}$,06854	
15	$\bar{1}$,96034	$\bar{1}$,91296	$\bar{1}$,86539	$\bar{1}$,79259	$\bar{1}$,66820	$\bar{1}$,39588	$\bar{2}$,75284		
16	$\bar{1}$,95892	$\bar{1}$,91101	$\bar{1}$,86357	$\bar{1}$,78565	$\bar{1}$,65447	$\bar{1}$,35799	$\bar{2}$,65447		
17	$\bar{1}$,95798	$\bar{1}$,90954	$\bar{1}$,86150	$\bar{1}$,77901	$\bar{1}$,63941	$\bar{1}$,31636	$\bar{2}$,54071		
18	$\bar{1}$,95703	$\bar{1}$,90869	$\bar{1}$,85940	$\bar{1}$,77128	$\bar{1}$,62230	$\bar{1}$,26949	$\bar{2}$,42439		
19	$\bar{1}$,95606	$\bar{1}$,90783	$\bar{1}$,85651	$\bar{1}$,76326	$\bar{1}$,60286	$\bar{1}$,21920	$\bar{2}$,28978		
20	$\bar{1}$,95508	$\bar{1}$,90695	$\bar{1}$,85356	$\bar{1}$,75496	$\bar{1}$,58074	$\bar{1}$,16126	$\bar{2}$,13077		
21	$\bar{1}$,95460	$\bar{1}$,90657	$\bar{1}$,85030	$\bar{1}$,74687	$\bar{1}$,55755	$\bar{1}$,09798	$\bar{3}$,93876		
22	$\bar{1}$,95412	$\bar{1}$,90621	$\bar{1}$,84619	$\bar{1}$,73848	$\bar{1}$,53097	$\bar{1}$,02742	$\bar{3}$,70006		
23	$\bar{1}$,95363	$\bar{1}$,90583	$\bar{1}$,84194	$\bar{1}$,72871	$\bar{1}$,50204	$\bar{2}$,95363	$\bar{3}$,40340		
24	$\bar{1}$,95313	$\bar{1}$,90544	$\bar{1}$,83757	$\bar{1}$,71851	$\bar{1}$,47040	$\bar{2}$,87764	$\bar{3}$,10679		
25	$\bar{1}$,95262	$\bar{1}$,90505	$\bar{1}$,83225	$\bar{1}$,70786	$\bar{1}$,43554	$\bar{2}$,79250			
26	$\bar{1}$,95209	$\bar{1}$,90465	$\bar{1}$,82673	$\bar{1}$,69555	$\bar{1}$,39907	$\bar{2}$,69555			
27	$\bar{1}$,95156	$\bar{1}$,90352	$\bar{1}$,82103	$\bar{1}$,68143	$\bar{1}$,35838	$\bar{2}$,58273			
28	$\bar{1}$,95166	$\bar{1}$,90237	$\bar{1}$,81425	$\bar{1}$,66527	$\bar{1}$,31246	$\bar{2}$,46736			
29	$\bar{1}$,95177	$\bar{1}$,90045	$\bar{1}$,80720	$\bar{1}$,64180	$\bar{1}$,26314	$\bar{2}$,33372			
30	$\bar{1}$,95187	$\bar{1}$,89848	$\bar{1}$,79988	$\bar{1}$,62566	$\bar{1}$,20618	$\bar{2}$,17569			
31	$\bar{1}$,95197	$\bar{1}$,89570	$\bar{1}$,79227	$\bar{1}$,60295	$\bar{1}$,14338	$\bar{3}$,98416			
32	$\bar{1}$,95209	$\bar{1}$,89207	$\bar{1}$,78436	$\bar{1}$,57685	$\bar{1}$,07330	$\bar{3}$,74594			
33	$\bar{1}$,95220	$\bar{1}$,88831	$\bar{1}$,77508	$\bar{1}$,54841	$\bar{1}$,00000	$\bar{3}$,44977			
34	$\bar{1}$,95231	$\bar{1}$,88444	$\bar{1}$,76538	$\bar{1}$,51727	$\bar{2}$,92451	$\bar{3}$,15366			
35	$\bar{1}$,95243	$\bar{1}$,87963	$\bar{1}$,75524	$\bar{1}$,48292	$\bar{2}$,83988				
36	$\bar{1}$,95256	$\bar{1}$,87464	$\bar{1}$,74346	$\bar{1}$,44698	$\bar{2}$,74346				
37	$\bar{1}$,95196	$\bar{1}$,86947	$\bar{1}$,72987	$\bar{1}$,40682	$\bar{2}$,63117				
38	$\bar{1}$,95071	$\bar{1}$,86259	$\bar{1}$,71361	$\bar{1}$,36080	$\bar{2}$,51570				
39	$\bar{1}$,94868	$\bar{1}$,85543	$\bar{1}$,69503	$\bar{1}$,31137	$\bar{2}$,38195				
40	$\bar{1}$,94661	$\bar{1}$,84801	$\bar{1}$,67379	$\bar{1}$,25431	$\bar{2}$,22382				
41	$\bar{1}$,94373	$\bar{1}$,84030	$\bar{1}$,65098	$\bar{1}$,19141	$\bar{2}$,03219				
42	$\bar{1}$,93998	$\bar{1}$,83227	$\bar{1}$,62476	$\bar{1}$,12121	$\bar{3}$,79385				
43	$\bar{1}$,93611	$\bar{1}$,82288	$\bar{1}$,59621	$\bar{1}$,04780	$\bar{3}$,49757				
44	$\bar{1}$,93213	$\bar{1}$,81307	$\bar{1}$,56496	$\bar{2}$,97220	$\bar{3}$,20135				
45	$\bar{1}$,92720	$\bar{1}$,80281	$\bar{1}$,53049	$\bar{2}$,88745					
46	$\bar{1}$,92208	$\bar{1}$,79090	$\bar{1}$,49442	$\bar{2}$,79090					
47	$\bar{1}$,91751	$\bar{1}$,77791	$\bar{1}$,45486	$\bar{2}$,67921					
48	$\bar{1}$,91188	$\bar{1}$,76290	$\bar{1}$,41009	$\bar{2}$,56499					
49	$\bar{1}$,90675	$\bar{1}$,74635	$\bar{1}$,36269	$\bar{2}$,43327					
50	$\bar{1}$,90140	$\bar{1}$,72718	$\bar{1}$,30770	$\bar{2}$,27721					
51	$\bar{1}$,89657	$\bar{1}$,70725	$\bar{1}$,24768	$\bar{2}$,08846					
52	$\bar{1}$,89229	$\bar{1}$,68478	$\bar{1}$,18123	$\bar{3}$,85387					

[*continued.*

TABLE VIII. *continued.*—Logarithm of Deparcieux chance of living for every age *a*.

a	10 years.	20 years.	30 years.	40 years.	50 years.	60 years.	70 years.	80 years.	90 years
53	$\bar{1}$,88677	$\bar{1}$,66010	$\bar{1}$,11169	$\bar{3}$,56146					
54	$\bar{1}$,88094	$\bar{1}$,63283	$\bar{1}$,04007	$\bar{3}$,26922					
55	$\bar{1}$,87561	$\bar{1}$,60329	$\bar{2}$,96025						
56	$\bar{1}$,86882	$\bar{1}$,57234	$\bar{2}$,86882						
57	$\bar{1}$,86040	$\bar{1}$,53735	$\bar{2}$,76170						
58	$\bar{1}$,85102	$\bar{1}$,49821	$\bar{2}$,65311						
59	$\bar{1}$,83960	$\bar{1}$,45594	$\bar{2}$,52652						
60	$\bar{1}$,82578	$\bar{1}$,40630	$\bar{2}$,37581						
61	$\bar{1}$,81068	$\bar{1}$,35111	$\bar{2}$,19189						
62	$\bar{1}$,79249	$\bar{1}$,28894	$\bar{3}$,96158						
63	$\bar{1}$,77333	$\bar{1}$,22492	$\bar{3}$,67469						
64	$\bar{1}$,75189	$\bar{1}$,15913	$\bar{3}$,38828						
65	$\bar{1}$,72768	$\bar{1}$,08464							
66	$\bar{1}$,70352	$\bar{1}$,00000							
67	$\bar{1}$,67695	$\bar{2}$,90130							
68	$\bar{1}$,64719	$\bar{2}$,80209							
69	$\bar{1}$,61634	$\bar{2}$,68692							
70	$\bar{1}$,58052	$\bar{2}$,55003							
71	$\bar{1}$,54043	$\bar{2}$,38121							
72	$\bar{1}$,49645	$\bar{2}$,16909							
73	$\bar{1}$,45159	$\bar{3}$,90136							
74	$\bar{1}$,40724	$\bar{3}$,63639							
75	$\bar{1}$,35696								
76	$\bar{1}$,29648								
77	$\bar{1}$,22435								
78	$\bar{1}$,15490								
79	$\bar{1}$,07058								
80	$\bar{2}$,96951								
81	$\bar{2}$,84078								
82	$\bar{2}$,67264								
83	$\bar{2}$,44977								
84	$\bar{2}$,22915								

TABLE IX.—Logarithm of the Northampton chance for living at every age *a*.

a	10 years.	20 years.	30 years.	40 years.	50 years.	60 years.	70 years.	80 years.	90 years.
0	$\bar{1},68764$	$\bar{1},64396$	$\bar{1},57564$	$\bar{1},49417$	$\bar{1},38958$	$\bar{1},24287$	$\bar{1},02428$	$\bar{2},60484$	$\bar{3},59643$
1	$\bar{1},81295$	$\bar{1},76713$	$\bar{1},69746$	$\bar{1},61431$	$\bar{1},50640$	$\bar{1},35435$	$\bar{1},12443$	$\bar{2},67151$	$\bar{3},59446$
2	$\bar{1},88378$	$\bar{1},83536$	$\bar{1},76454$	$\bar{1},67952$	$\bar{1},56809$	$\bar{1},41046$	$\bar{1},16788$	$\bar{2},67677$	$\bar{3},51790$
3	$\bar{1},91089$	$\bar{1},85979$	$\bar{1},78780$	$\bar{1},70070$	$\bar{1},58568$	$\bar{1},42229$	$\bar{1},16522$	$\bar{2},62961$	$\bar{3},37283$
4	$\bar{1},92894$	$\bar{1},87511$	$\bar{1},80190$	$\bar{1},71263$	$\bar{1},59383$	$\bar{1},42421$	$\bar{1},15070$	$\bar{2},55993$	$\bar{3},14495$
5	$\bar{1},93843$	$\bar{1},88180$	$\bar{1},80733$	$\bar{1},71581$	$\bar{1},59300$	$\bar{1},41691$	$\bar{1},12431$	$\bar{2},47370$	$\bar{4},80625$
6	$\bar{1},94739$	$\bar{1},88788$	$\bar{1},81211$	$\bar{1},71823$	$\bar{1},59118$	$\bar{1},40806$	$\bar{1},09339$	$\bar{2},37854$	
7	$\bar{1},95322$	$\bar{1},89101$	$\bar{1},81390$	$\bar{1},71755$	$\bar{1},58601$	$\bar{1},39522$	$\bar{1},05661$	$\bar{2},27263$	
8	$\bar{1},95660$	$\bar{1},89203$	$\bar{1},81352$	$\bar{1},71459$	$\bar{1},57827$	$\bar{1},37909$	$\bar{1},01505$	$\bar{2},15453$	
9	$\bar{1},95739$	$\bar{1},89080$	$\bar{1},81084$	$\bar{1},70923$	$\bar{1},56781$	$\bar{1},35940$	$\bar{2},96901$	$\bar{2},03386$	
10	$\bar{1},95632$	$\bar{1},88800$	$\bar{1},80653$	$\bar{1},70194$	$\bar{1},55523$	$\bar{1},33664$	$\bar{2},91720$	$\bar{3},90879$	
11	$\bar{1},95418$	$\bar{1},88451$	$\bar{1},80136$	$\bar{1},69345$	$\bar{1},54140$	$\bar{1},31148$	$\bar{2},85856$	$\bar{3},78151$	
12	$\bar{1},95158$	$\bar{1},88076$	$\bar{1},79574$	$\bar{1},68431$	$\bar{1},52668$	$\bar{1},28410$	$\bar{2},79299$	$\bar{3},63412$	
13	$\bar{1},94890$	$\bar{1},87691$	$\bar{1},78981$	$\bar{1},67479$	$\bar{1},51140$	$\bar{1},25433$	$\bar{2},71872$	$\bar{3},46194$	
14	$\bar{1},94617$	$\bar{1},87296$	$\bar{1},78369$	$\bar{1},66489$	$\bar{1},49527$	$\bar{1},22176$	$\bar{2},63099$	$\bar{3},21602$	
15	$\bar{1},94337$	$\bar{1},86890$	$\bar{1},77738$	$\bar{1},65457$	$\bar{1},47848$	$\bar{1},18588$	$\bar{2},53527$	$\bar{4},86782$	
16	$\bar{1},94049$	$\bar{1},86472$	$\bar{1},77084$	$\bar{1},64379$	$\bar{1},46067$	$\bar{1},14600$	$\bar{2},43115$		
17	$\bar{1},93779$	$\bar{1},86068$	$\bar{1},76433$	$\bar{1},63279$	$\bar{1},44200$	$\bar{1},10339$	$\bar{2},31941$		
18	$\bar{1},93543$	$\bar{1},85692$	$\bar{1},75799$	$\bar{1},62167$	$\bar{1},42249$	$\bar{1},05845$	$\bar{2},19793$		
19	$\bar{1},93341$	$\bar{1},85345$	$\bar{1},75184$	$\bar{1},61042$	$\bar{1},40201$	$\bar{1},01162$	$\bar{2},07647$		
20	$\bar{1},93168$	$\bar{1},85021$	$\bar{1},74562$	$\bar{1},59891$	$\bar{1},38032$	$\bar{2},96088$	$\bar{3},95247$		
21	$\bar{1},93033$	$\bar{1},84718$	$\bar{1},73927$	$\bar{1},58722$	$\bar{1},35730$	$\bar{2},90438$	$\bar{3},82733$		
22	$\bar{1},92918$	$\bar{1},84417$	$\bar{1},73274$	$\bar{1},57511$	$\bar{1},33253$	$\bar{2},84141$	$\bar{3},68255$		
23	$\bar{1},92801$	$\bar{1},84091$	$\bar{1},72589$	$\bar{1},56250$	$\bar{1},30543$	$\bar{2},76982$	$\bar{3},51304$		
24	$\bar{1},92679$	$\bar{1},83752$	$\bar{1},71872$	$\bar{1},54910$	$\bar{1},27559$	$\bar{2},68482$	$\bar{3},26984$		
25	$\bar{1},92553$	$\bar{1},83401$	$\bar{1},71120$	$\bar{1},53511$	$\bar{1},24251$	$\bar{2},59191$	$\bar{4},92445$		
26	$\bar{1},92423$	$\bar{1},83035$	$\bar{1},70330$	$\bar{1},52018$	$\bar{1},20551$	$\bar{2},49066$			
27	$\bar{1},92289$	$\bar{1},82654$	$\bar{1},69500$	$\bar{1},50421$	$\bar{1},16560$	$\bar{2},38162$			
28	$\bar{1},92149$	$\bar{1},82256$	$\bar{1},68624$	$\bar{1},48706$	$\bar{1},12302$	$\bar{2},26250$			
29	$\bar{1},92004$	$\bar{1},81843$	$\bar{1},67701$	$\bar{1},46860$	$\bar{1},07821$	$\bar{2},14306$			
30	$\bar{1},91853$	$\bar{1},81394$	$\bar{1},66723$	$\bar{1},44864$	$\bar{1},02920$	$\bar{2},02079$			
31	$\bar{1},91685$	$\bar{1},80894$	$\bar{1},65689$	$\bar{1},42697$	$\bar{2},97405$	$\bar{3},89700$			
32	$\bar{1},91498$	$\bar{1},80355$	$\bar{1},64592$	$\bar{1},40334$	$\bar{2},91223$	$\bar{3},75336$			
33	$\bar{1},91290$	$\bar{1},79788$	$\bar{1},63449$	$\bar{1},37742$	$\bar{2},84181$	$\bar{3},58503$			
34	$\bar{1},91073$	$\bar{1},79193$	$\bar{1},62231$	$\bar{1},34880$	$\bar{2},75802$	$\bar{3},34305$			
35	$\bar{1},90848$	$\bar{1},78567$	$\bar{1},60958$	$\bar{1},31698$	$\bar{2},66637$	$\bar{4},99892$			
36	$\bar{1},90612$	$\bar{1},77907$	$\bar{1},59595$	$\bar{1},28128$	$\bar{2},56643$				
37	$\bar{1},90365$	$\bar{1},77211$	$\bar{1},58132$	$\bar{1},24271$	$\bar{2},45873$				
38	$\bar{1},90107$	$\bar{1},76475$	$\bar{1},56557$	$\bar{1},20153$	$\bar{2},34101$				
39	$\bar{1},89839$	$\bar{1},75697$	$\bar{1},54856$	$\bar{1},15817$	$\bar{2},22302$				
40	$\bar{1},89541$	$\bar{1},74870$	$\bar{1},53011$	$\bar{1},11067$	$\bar{2},10226$				
41	$\bar{1},89209$	$\bar{1},74004$	$\bar{1},51012$	$\bar{1},05720$	$\bar{3},98015$				
42	$\bar{1},88857$	$\bar{1},73094$	$\bar{1},48836$	$\bar{2},99725$	$\bar{3},83838$				
43	$\bar{1},88498$	$\bar{1},72159$	$\bar{1},46452$	$\bar{2},92891$	$\bar{3},67213$				
44	$\bar{1},88120$	$\bar{1},71158$	$\bar{1},43807$	$\bar{2},84730$	$\bar{3},43232$				
45	$\bar{1},87719$	$\bar{1},70110$	$\bar{1},40850$	$\bar{2},75789$	$\bar{3},09044$				
46	$\bar{1},87295$	$\bar{1},68983$	$\bar{1},37516$	$\bar{2},66031$					
47	$\bar{1},86846$	$\bar{1},67767$	$\bar{1},33906$	$\bar{2},55508$					
48	$\bar{1},86368$	$\bar{1},66450$	$\bar{1},30046$	$\bar{2},43994$					
49	$\bar{1},85858$	$\bar{1},65017$	$\bar{1},25978$	$\bar{2},32463$					
50	$\bar{1},85329$	$\bar{1},63470$	$\bar{1},21526$	$\bar{2},20685$					
51	$\bar{1},84795$	$\bar{1},61803$	$\bar{1},16511$	$\bar{2},08806$					
52	$\bar{1},84237$	$\bar{1},59979$	$\bar{1},10868$	$\bar{3},94981$					

[*continued.*

TABLE IX. *continued.*—Logarithm of the Northampton chance for living at every age *a*.

a	10 years.	20 years.	30 years.	40 years.	50 years.	60 years.	70 years.	80 years.	90 years.
53	$\bar{1},83661$	$\bar{1},57954$	$\bar{1},04393$	$\bar{3},78715$					
54	$\bar{1},83038$	$\bar{1},55687$	$\bar{2},96610$	$\bar{3},55112$					
55	$\bar{1},82391$	$\bar{1},53131$	$\bar{2},88070$	$\bar{3},21325$					
56	$\bar{1},81688$	$\bar{1},50221$	$\bar{2},78736$						
57	$\bar{1},80921$	$\bar{1},47060$	$\bar{2},68662$						
58	$\bar{1},80082$	$\bar{1},43678$	$\bar{2},57626$						
59	$\bar{1},79159$	$\bar{1},40120$	$\bar{2},46605$						
60	$\bar{1},78141$	$\bar{1},36197$	$\bar{2},35356$						
61	$\bar{1},77008$	$\bar{1},31716$	$\bar{2},24011$						
62	$\bar{1},75742$	$\bar{1},26631$	$\bar{2},10744$						
63	$\bar{1},74293$	$\bar{1},20732$	$\bar{3},95054$						
64	$\bar{1},72649$	$\bar{1},13572$	$\bar{3},72074$						
65	$\bar{1},70740$	$\bar{1},05679$	$\bar{3},38934$						
66	$\bar{1},68533$	$\bar{2},97048$							
67	$\bar{1},66139$	$\bar{2},87741$							
68	$\bar{1},63596$	$\bar{2},77544$							
69	$\bar{1},60961$	$\bar{2},67446$							
70	$\bar{1},58056$	$\bar{2},57215$							
71	$\bar{1},54708$	$\bar{2},47003$							
72	$\bar{1},50889$	$\bar{2},35002$							
73	$\bar{1},46439$	$\bar{2},20761$							
74	$\bar{1},40923$	$\bar{3},99425$							
75	$\bar{1},34939$	$\bar{3},68194$							
76	$\bar{1},28515$								
77	$\bar{1},21602$								
78	$\bar{1},13948$								
79	$\bar{1},06485$								
80	$\bar{2},99159$								
81	$\bar{2},92295$								
82	$\bar{2},84113$								
83	$\bar{2},74322$								
84	$\bar{2},58502$								
85	$\bar{2},33255$								

How the value of particular assurances may be determined from the value of annuities, is shown in my Paper in the Philosophical Transactions for the year 1820, many of the cases of which are solved by methods essentially the same as those which have been long adopted; but when such assurances are but for terms, which are not of great extension, very near approximations may be had by using a geometrical progression, without confining the arithmetical operations to the same route, since the chance of extinction of the joint lives of the present age a, b, c, &c. taking place between the period commencing with the time $n+t-1$, and finishing with the time $n+t$, from the present, is $= (L_{n+t-1:a,b,c,\&c.} - L_{n+t:a,b,c,\&c.}) \div L_{a,b,c,\&c.}$; it follows that if r be the present value of unity, to be received certain in the time 1, and $L_{n+t-1:a,b,c,\&c.} = L_{n-1:a,b,c,} \times \pi^t$, whatever t may be, that $\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{n}}}\underline{\big| a, b, c, \&c.}$ or the assurance of unity to be received at the first of the equal periods 1, from the commencement of the time $n-1$ to the expiration of the time m, which shall happen after the extinction of the joint lives, is equal to $\frac{L_{n-1:a,b,c,\&c.}}{L_{a,b,c,\&c.}} \times \left\{ r^n \times (1-\pi) + r^{n+1} \times (\pi - \pi^2) + r^{n+2} (\pi^2 - \pi^3) \ldots\ldots r^m \times (\pi^{m-n-1} - \pi^{m-n}) \right\} = (1-\pi) \times \frac{L_{n-1:a,b,c,\&c.}}{L_{a,b,c,\&c.}} \times \left\{ r^n + \pi r^{n+1} + \pi^2 r^{n+2} + \pi^3 r^{n+3} \ldots . r^m . \pi^{m-n-1} \right\} = \frac{(1-\pi) r}{L_{a,b,c,\&c.}} \times \left\{ r^{n-1} L_{n-1:a,b,c,\&c.} + r^n . L_{n:a,b,c,\&c.} + \ldots . r^{m-1} . L_{m-1:a,b,c,\&c.} \right\} = (1-\pi) . r \times \overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{n-1}}}\underline{\big| a, b, c, \&c.}$

If the assurance be not deferred, n will be equal to 1, and we shall have, according to the hypothesis, $\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big| a, b, c, \&c.} = (1-\pi) . r \times \overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{0}}}\underline{\big| a, b, c, \&c.}$; and also $= \frac{1-\pi}{\pi} . \overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big| a, b, c, \&c.}$ If t be taken equal to 1, we shall have from the equation $L_{n+t-1:a,b,c,\&c.} = L_{n-1:a,b,c,\&c.} \times \pi^{t}$, $\pi = \frac{L_{n:a,b,c,\&c.}}{L_{n-1:a,b,c,\&c.}}$, and this would be the real value which should be taken for π, if the geometrical progression coincided perfectly with the fact; and it would be indifferent whether we made it equal to $\frac{L_{n+t:a,b,c,\&c}}{L_{n-1+t:a,b,c,\&c.}}$, or $\frac{L_{n:a,b,c,\&c.}}{L_{n-1:a,b,c,\&c.}}$, as the two would be the same; but this not being the case, there will be a preference; and generally, if not always, π should be taken an intermediate value between the two; and when the term is not very long, it will answer a good purpose to take it about the middle between them, inclining generally, though perhaps not always, rather nearer the last than the first, as the first terms are generally of more consequence than the last. If the said assurance be not deferred, and instead of being paid for immediately, be to be paid for by equal periodic payments, at an unite of time from each other, up to the time $m-1$ inclusive, and the first payment be to be made immediately, then will the present value of such periodic payment be ${}^{\overset{r}{\frown}}_{}\!\overset{1}{\underset{m-1}{0}}\big|\underline{a, b, c, \&c.}$, and consequently each payment, from what is shown above, is equal to ${}^{\overset{r}{\frown}}_{}\!\overset{1}{\underset{m}{1}}\big|\underline{a, b, c, \&c.} \div {}^{\overset{r}{\frown}}_{}\!\overset{1}{\underset{m-1}{0}}\big|\underline{a, b, c, \&c.} = (1-\pi).r.$ From whence we may draw an inference worthy of remark, namely; when an assurance of joint lives is meant to commence immediately, and to continue for a term of t years, which is not large, and to be paid for by t annual payments, that those payments will not differ much with the increase of the time t, provided, as I have said, that t be not large, and the ages be not at the extremes of life, a consequence which follows from the near agreement to a geometrical progression which takes place in the number of living at each small equal increment of time; that is to say, from the near coincidence of $\overset{\mathrm{L}}{\frac{n\,:\,a,\,b,\,c,\,\&c.}{n-1\,:\,a,\,b,\,c,\,\&c.}}$ with $\overset{\mathrm{L}}{\frac{n+t\,:\,a,\,b,\,c,\,\&c.}{n+1\,:\,a,\,b,\,c,\,\&c.}}$, or the small variation of π for the different values of t: and also, that when the number of years for which an assurance continues be not very long, and the ages be not at the extremes of life, the annual premiums will not differ widely from the premiums to be paid for an assurance of one year of a life older than the proposed life by about half the term: thus, according to the Northampton table, at three per cent. to assure 100 *l.* at the

Age	15	20	30	40	50	60	64
For 7 years, the annual premium by the common modes of calculation	£1..2..11	1.. 9.. 5	1..14..11	2.. 4.. 1	3.. 0.. 8	4.. 7.. 1	5.. 4..10
And the premium for one year assurance for an age 3 years older . . .	1..3.. 3	1.. 9.. 8	1..15.. 0	2.. 4.. 6	3.. 1.. 0	4.. 7.. 8	5 5.. 6

the difference of which is very small.—As another example, let

Age	10	20	30	40	50	60
For 10 years, the annual premium will be, by common modes of calculation	£0..19.. 2	1..9.. 1	1..15.. 8	2.. 5.. 8	3.. 3.. 4	4..12.. 6
Premium for one year assurance, age 5 years older	0..17..11	1..10.. 7	1..16.. 4	2.. 6.. 8	3.. 5.. 1	4..15.. 2

Here, except at the age 10, the excess is rather more in the approximation than in the first set of examples; but it should be recollected, that we took the exact middle, instead of inclining to the early age.

According to the Carlisle table of mortality at 3 per cent. to assure 100*l.* at the

Age	10	20	30	40	50	60
For 7 years, the annual premium, by common modes of calculation .	£0 10 5	0 13 10	0 19 10	1 7 8	1 11 0	3 13 8
For one year, the premium	0 10 5	0 13 9	0 19 2	1 8 6	1 12 1	3 15 9
For 10 years, the annual premium, by common modes of calculation .	0 11 3	0 14 7	1 0 4	1 7 7	1 14 11	3 17 8
For one year, at an age 5 years older	0 12 0	0 14 2	0 19 11	1 9 0	1 14 10	3 19 9

Moreover, because $\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big|a, b, c, \&c.}$, or the single premium for the assurance of unity, on the joint lives a, b, c, &c. for m years, is $= \overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.}\,.\,r - \overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big|a, b, c, \&c.} = \overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.}\,.\,r + 1 - \frac{L_{m:\,a,\,b,\,c,\,\&c.}}{L_{a,b,c,\&c.}}\,r^{m} - \overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.} = 1 - \frac{L_{m:\,a,\,b,\,c,\,\&c.}}{L_{a,\,b,\,c,\,\&e.}}\,.\,r^{m} - (1-r)\,.\,\overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a,b,c, \&c.}$; if this be divided by $\overset{\overset{r}{\smile}}{\underset{m\;1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.}$, we shall have the annual premium for such assurance; that is, $\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big|a, b, c, \&c} \div \overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.} = \dfrac{1-\dfrac{L_{m:\,a,b,c,\&c.}}{L_{a,\,b,\,c,\,\&c.}}\,.\,r^{m}}{\overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.}} - 1 + r.$ The said annual premium may be expressed by

$$\left(1 - \frac{L_{m,\,a,\,b,\,c,\,\&c.}}{L_{a,\,b,\,c,\,\&c.}}\,.\,r^{m}\right) \div \left(\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big|a-1, b-1, c-1, \&c.} \times \frac{L_{a-1,\,b-1,\,c-1,\&c.}}{r\,L_{a,\,b,\,c,\,\&c.}}\right) - 1 + r.$$

This last mode is well adapted to logarithms in the use of our general tables; and this method, supposing the annuities were accurately determinable by our general tables, would be accurate. The last formula is derived from that immediately before, in consequence of $\overset{\overset{r}{\smile}}{\underset{m-1}{\overset{1}{0}}}\underline{\big|a, b, c, \&c.}$ being identical with $\overset{\overset{r}{\smile}}{\underset{m}{\overset{1}{1}}}\underline{\big|a-1, b-1, c-1, \&c.} \times \dfrac{L_{a-1,\,b-1,\,c-1,\,\&c.}}{r\,L_{a,\,b,\,c,\,\&c.}}$

Example. To find the annual premium to assure a life, at the age a years, for 10 years, according to the Carlisle mortality, and three per cent. interest.

$a =$	20	30	40	50	60	70
Log. of the accommoda. chance for living 10 yrs. at the age $a-1$, Tab. V.	$\bar{1}.9690$	$\bar{1}.9556$	$\bar{1}.9406$	$\bar{1}.9328$	$\bar{1}.8435$	$\bar{1}.7005$
$\lambda\, 1{,}03^{-1} =$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$	$\bar{1}.8716$
Sum . . . =	$\bar{1}.8406$	$\bar{1}.8272$	$\bar{1}.8122$	$\bar{1}.8044$	$\bar{1}.7151$	$\bar{1}.5721$
Corresponding . . .	.91443	.90407	.89892	.89379	.84846	.78092
To this we get from Ta. I.	31	362	103	205	248	94
		10	10	21	5	5
$\lambda\, \overbrace{1}^{r}{}^{1}_{10}\lfloor\overline{a-1}$ . . . . =	.91474	.90779	.90005	.89605	.85099	.78191
Therefore, $\lambda \frac{L_{a+10}}{L_a}$ (T. VII.)	$\bar{1}.96682$	$\bar{1}.95400$	$\bar{1}.93772$	$\bar{1}.91830$	$\bar{1}.81893$	$\bar{1}.59873$
$\lambda\, 1{,}03^{-10} =$	$\bar{1}.87163$	$\bar{1}.87163$	$\bar{1}.87163$	$\bar{1}.87163$	$\bar{1}.87163$	$\bar{1}.87163$
Sum = the log. . . .	$\bar{1}.83845$	$\bar{1}.82563$	$\bar{1}.80935$	$\bar{1}.78993$	$\bar{1}.69056$	$\bar{1}.47036$
The N° corresponding =	.68937	.66932	.64469	.61650	.49041	.29536
Its complement to unity	.31063	.33068	.35531	.38350	.50959	.70464
The log. of the last . =	$\bar{1}.49224$	$\bar{1}.51941$	$\bar{1}.55061$	$\bar{1}.58377$	$\bar{1}.70722$	$\bar{1}.84797$
Complement of $\lambda\, \overbrace{1}^{r}{}^{1}_{10}\lfloor\overline{a-1}$ =	$\bar{1}.08526$	$\bar{1}.09221$	$\bar{1}.09995$	$\bar{1}.10395$	$\bar{1}.14901$	$\bar{1}.21809$
$\lambda \frac{L_a}{L_{a-1}}$ . . . . . . =	$\bar{1}.99694$	$\bar{1}.99571$	$\bar{1}.99481$	$\bar{1}.99402$	$\bar{1}.98754$	$\bar{1}.97813$
$\lambda\, r^{-1}$ . . . . . =	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$	$\bar{1}.98716$
Sum = logarithm . . .	$\bar{2}.56160$	$\bar{2}.59449$	$\bar{2}.63253$	$\bar{2}.66890$	$\bar{2}.83093$	$\bar{1}.03135$
Number corresponding =	.03644	.03931	.04291	.04666	.06775	.10749
$1{,}03^{-1} - 1$ . . . =	−.02913	−.02913	−.02913	−.02913	−.02913	−.02913
Ann. premium for an assurance of 1*l*. =	.00732	.01018	.01378	.01753	.03862	.07836
Ditto for 100 *l*. . . .	£0..14..8	1.. 0.. 4	1.. 7.. 7	1..15.. 1	3..1 .. 3	7..16.. 9

for annual premiums.

The reader has here an opportunity of comparing the results from my tables, with those above calculated by Mr. MILNE's Carlisle tables.—I may probably be able at a future period to add examples, which I regret time will not at present permit.